

# Recombination ...

FP I ZS 2024 XE 19. 12.

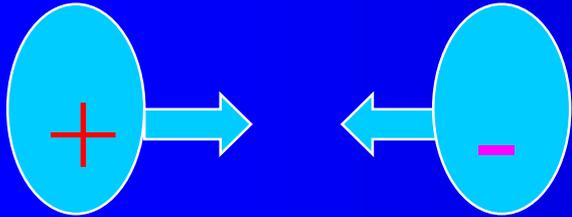
electron –ion recombination

atomic ions

molecular ions

ion –ion recombination

# Recombination

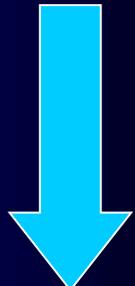
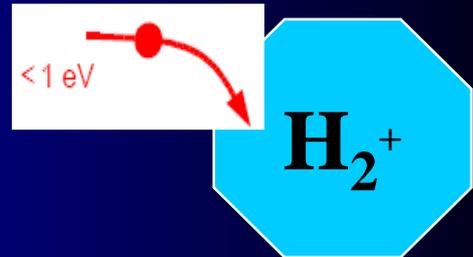


## Radiative recombination



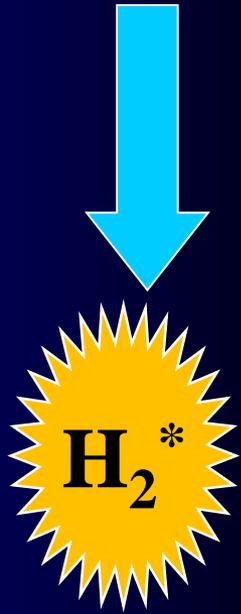
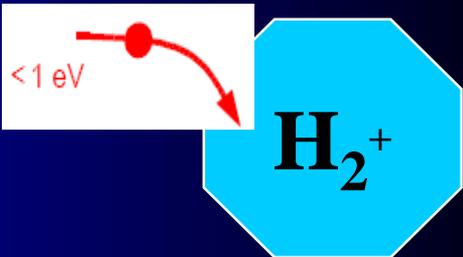
## Dissociative recombination







Capture





Capture

Auto ionization

$AB^*$  resonant state(s)

predissociation

To get high recombination rate, we need

(a) efficient capture

(b) predissociation faster than auto-ionization

# Electron –ion recombination



## Processes: at low impact energies

Elastic scattering



Electronic excitation



Vibrational excitation



Rotational excitation



Dissociative attachment /



Impact dissociation



All go via  $(AB^-\dots)**$

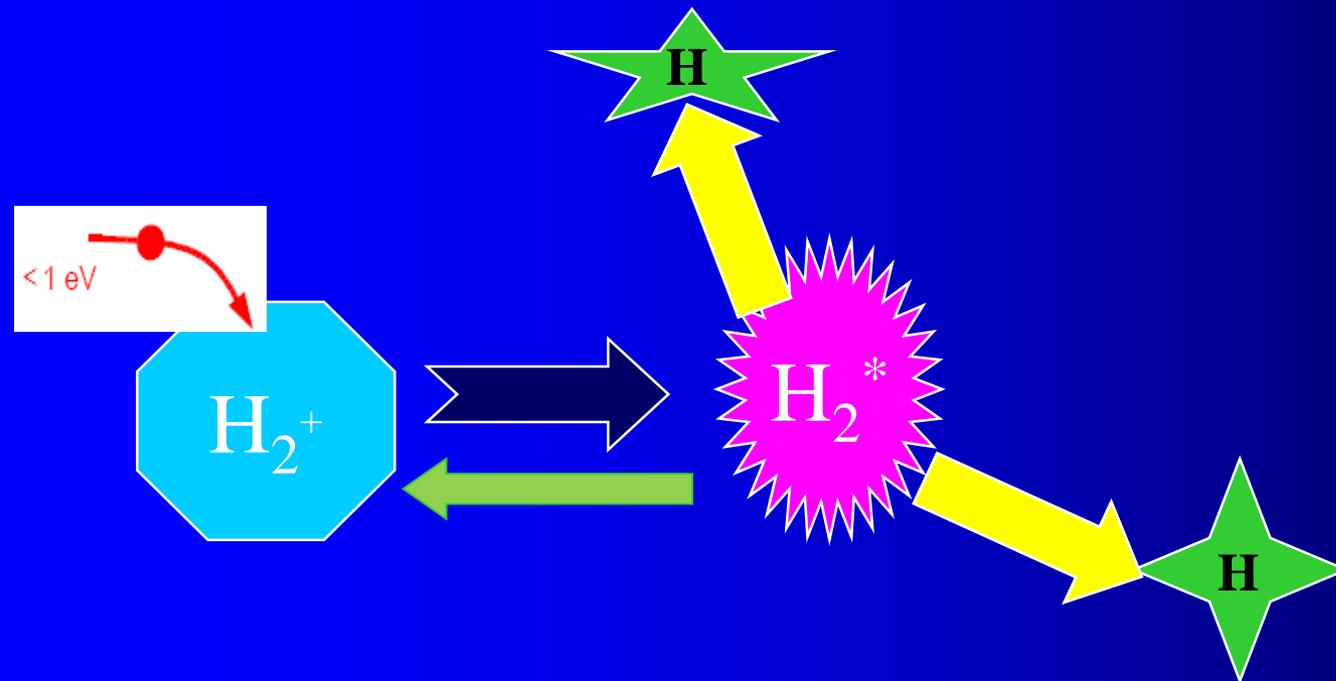
Dissociative recombination



Go via  $(AB\dots)**$



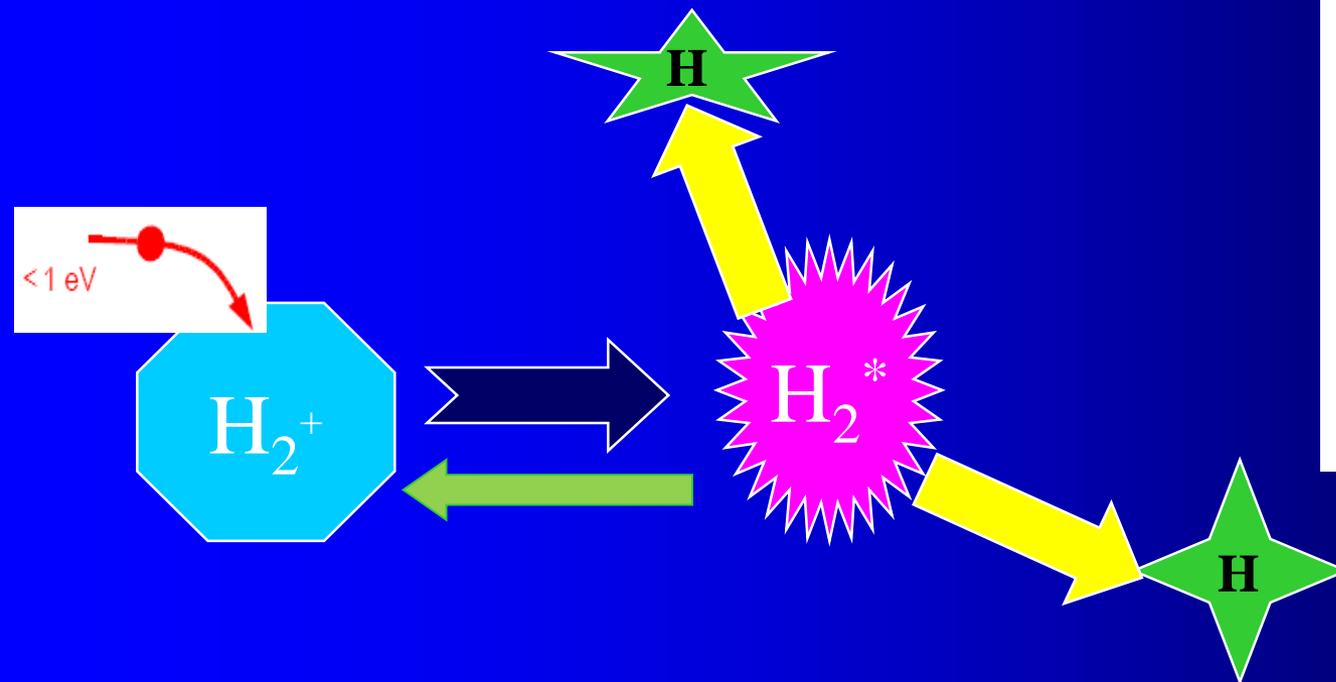
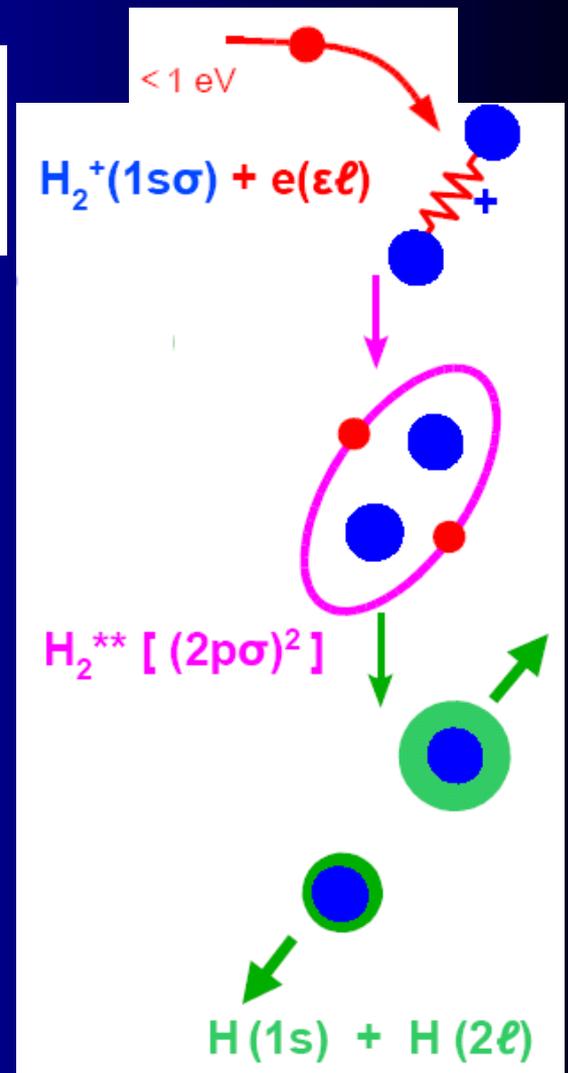
Dissociative Recombination - DR



Electron collisions with  $\text{H}_2^+$  - how to describe ????

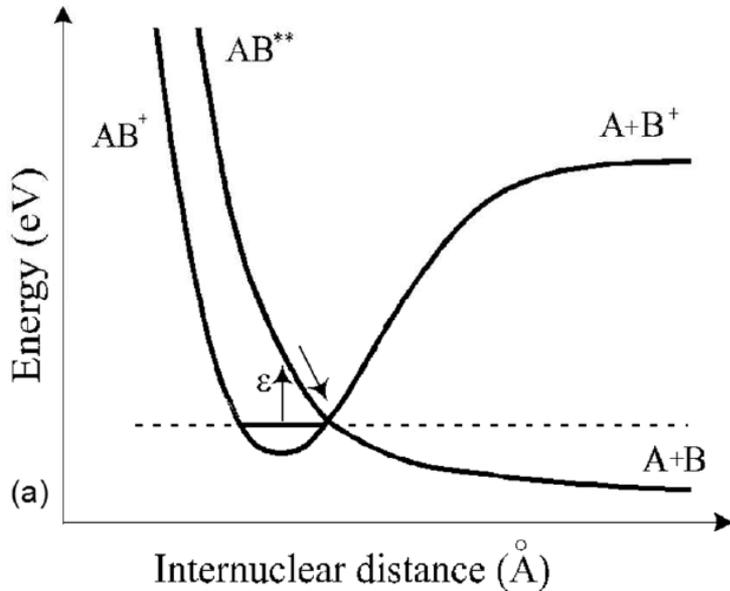


## Dissociative Recombination - DR



Electron collisions with  $\text{H}_2^+$  - how to describe ????

## Direct DR process

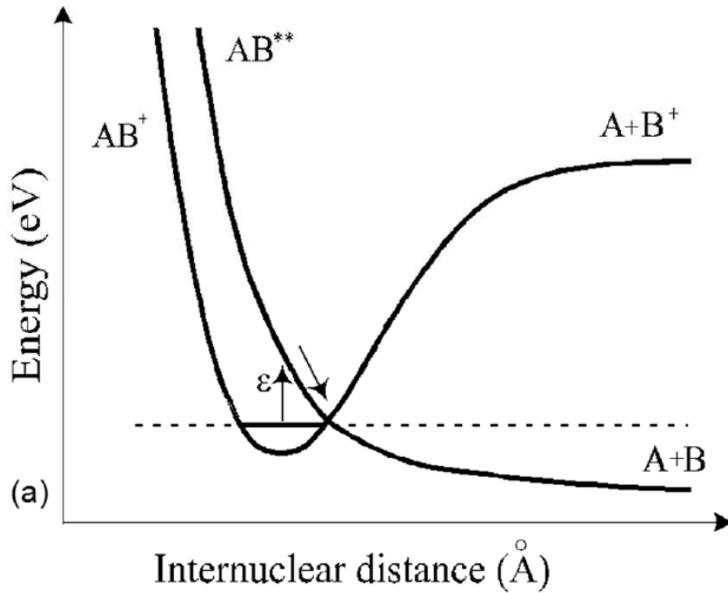


$$\alpha_{dr} \approx T_e^{-0.5}$$

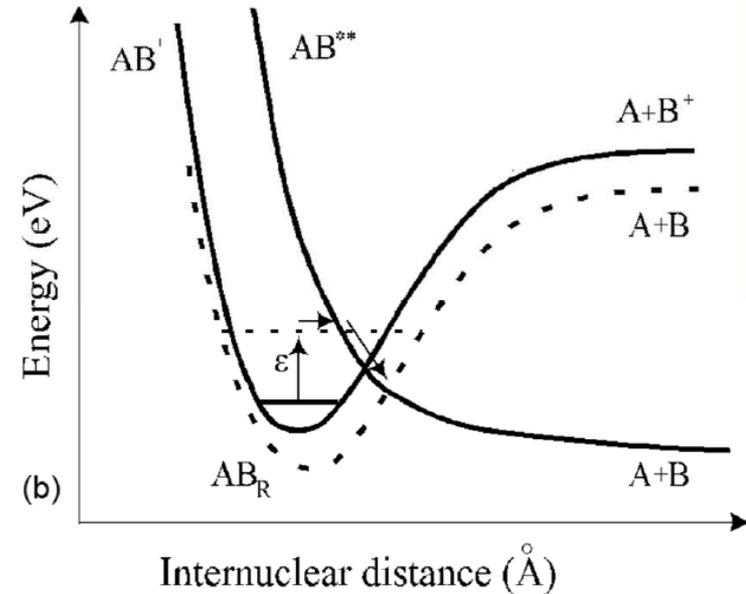
Ions:  $Ar_2^+$ ,  $N_2^+$ ,  $CH_4^+$ ,  $NH_4^+(NH_3)_2^-$  -  $\alpha \sim 10^{-7} - 10^{-6} \text{ cm}^3 \text{ s}^{-1}$

Theoretical calculation:  $H_2^+$ ,  $HD^+$ ,  $D_2^+$  -  $\alpha = 2.3 \times 10^{-8}$ ,  $2.2 \times 10^{-8}$ ,  $4 \times 10^{-9} \text{ cm}^3 \text{ s}^{-1}$ , respectively

## Direct DR process



## Indirect DR process



$$\alpha_{dr} \approx T_e^{-0.5}$$

$$\alpha_{idr} \approx T_e^{-1.5}$$

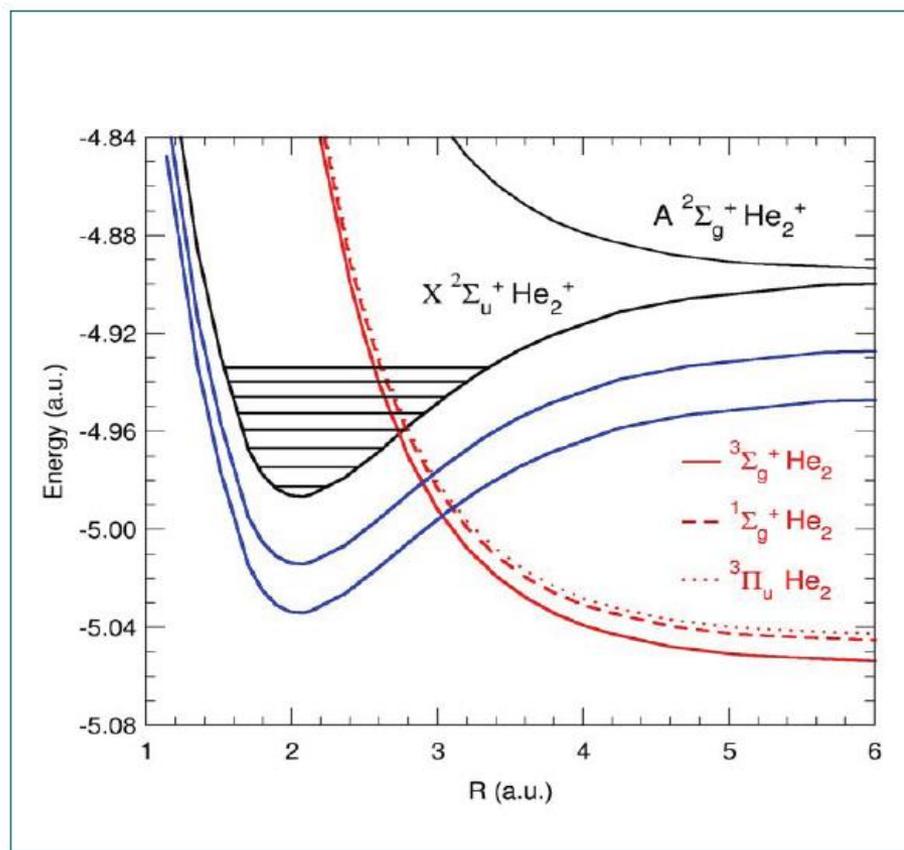
$$\alpha(T_e, T_v) \approx T_e^{-0.5} T_v^{-1}$$

Ions:  $Ar_2^+$ ,  $N_2^+$ ,  $CH_4^+$ ,  $NH_4^+(NH_3)_2^-$  -  $\alpha \sim 10^{-7} - 10^{-6} \text{ cm}^3 \text{ s}^{-1}$

Theoretical calculation:  $H_2^+$ ,  $HD^+$ ,  $D_2^+$  -  $\alpha = 2.3 \times 10^{-8}$ ,  $2.2 \times 10^{-8}$ ,  $4 \times 10^{-9} \text{ cm}^3 \text{ s}^{-1}$ , respectively

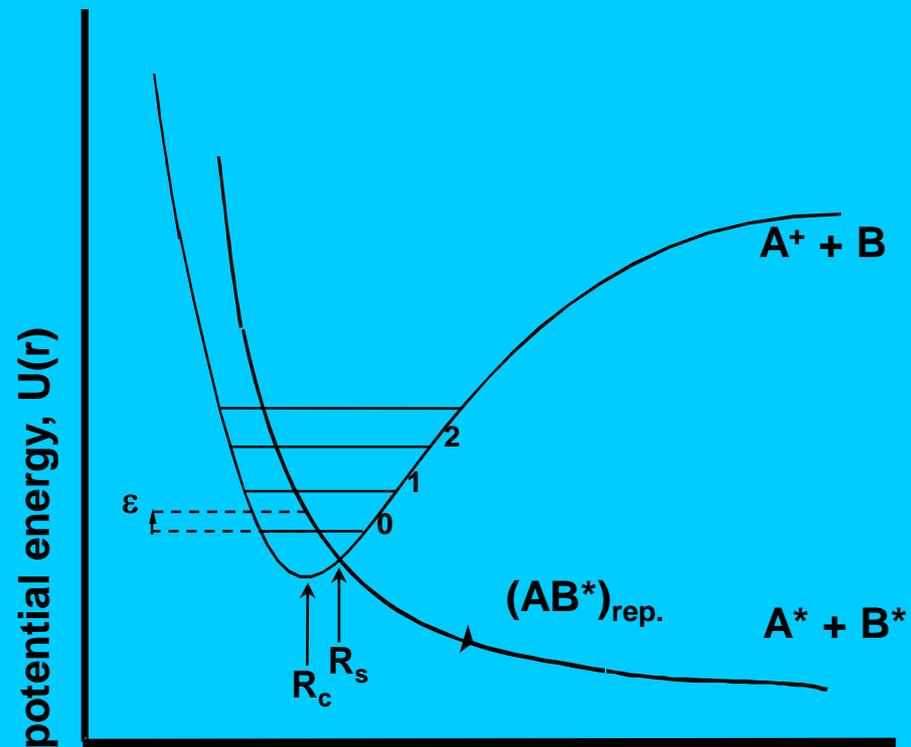
# THEORETICAL FRAMEWORK

The states involved: exemple for  $\text{He}_2^+/\text{He}_2$  system

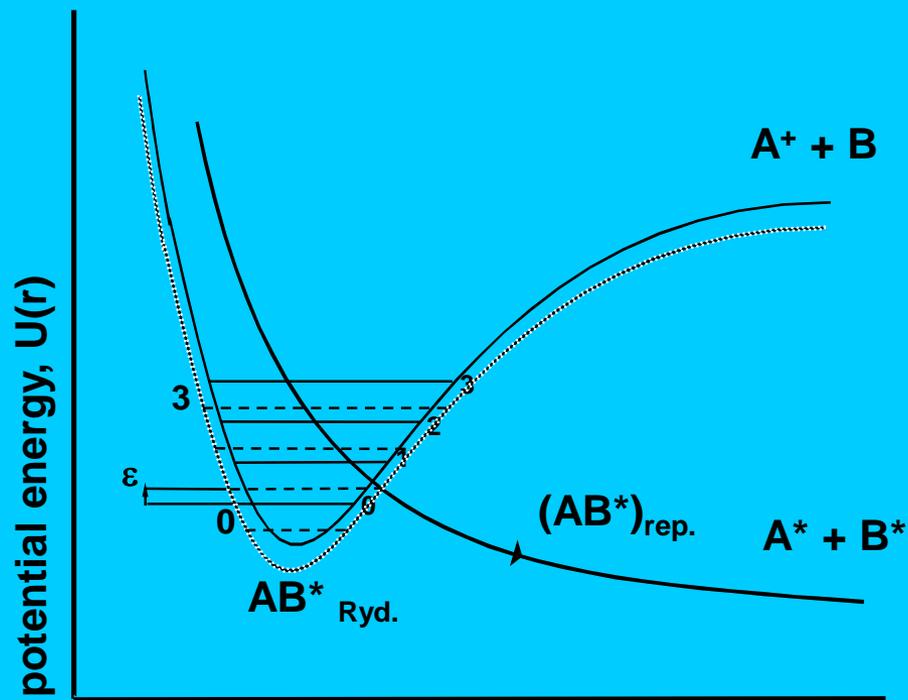


2004 DR6 Mosbach

I. Schneider, et al., DR2004 Mosbach

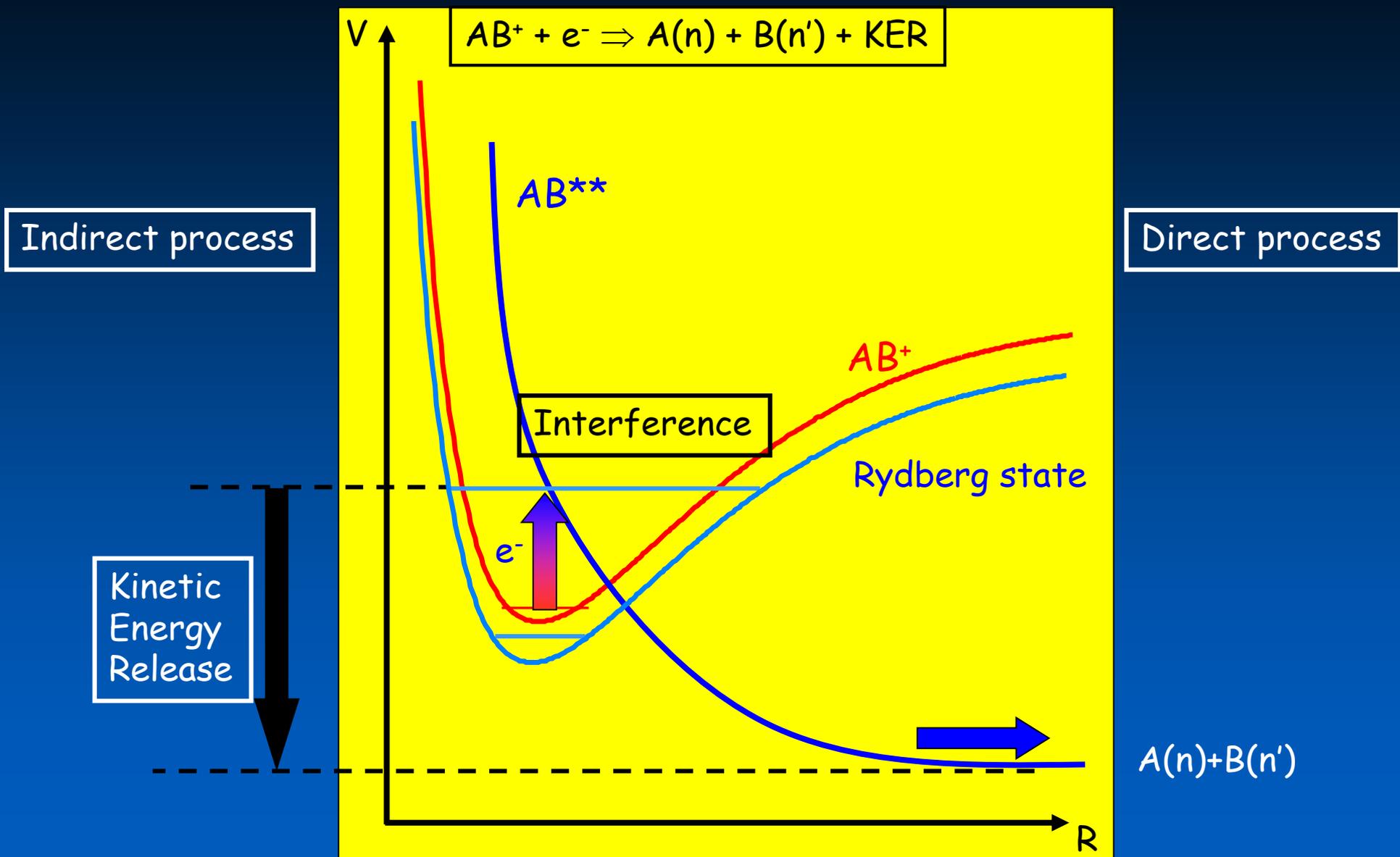


Direct mechanism

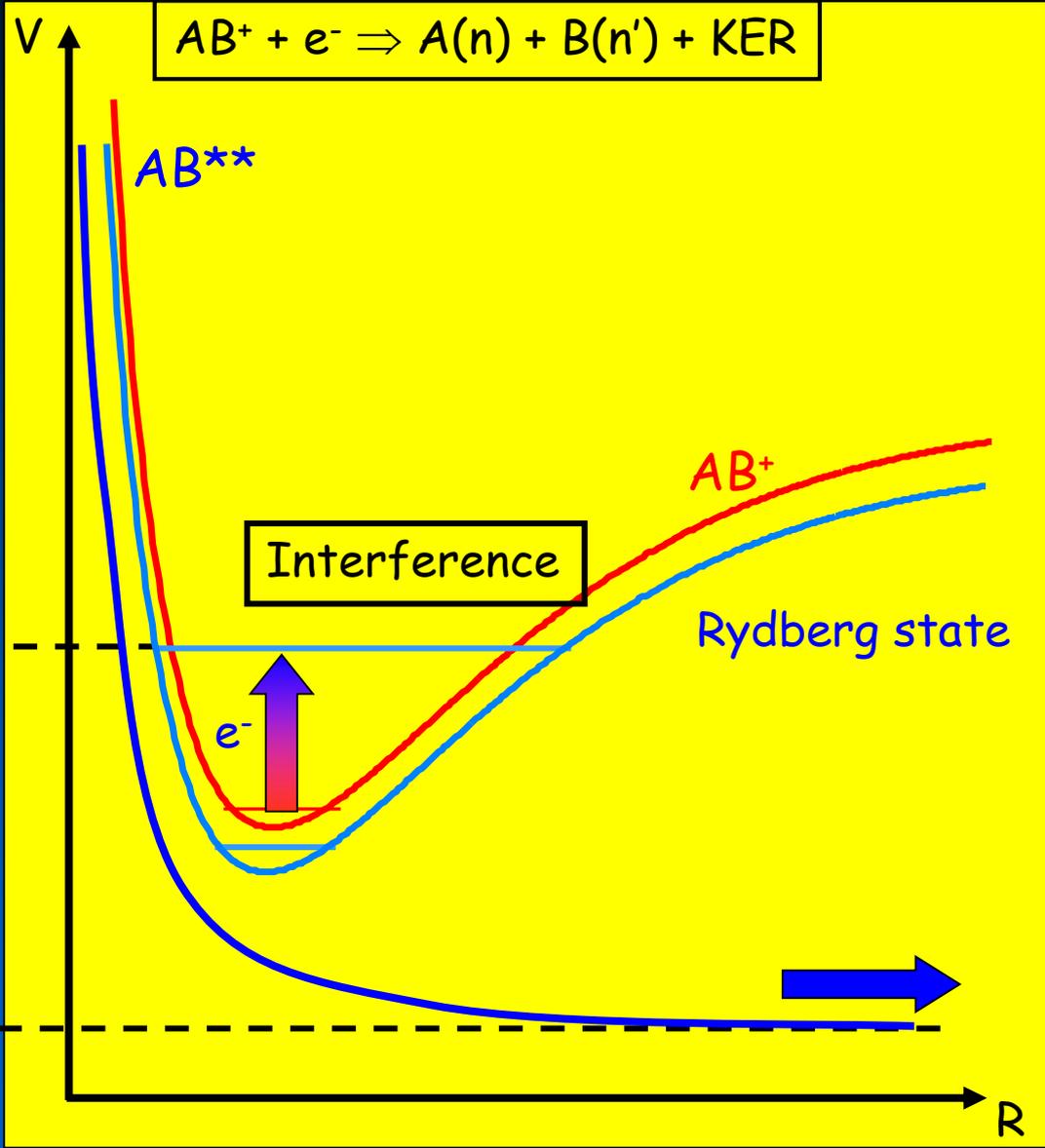


Indirect mechanism

# Electron-cold molecular ion reaction: Dissociative Recombination



Recombination of  $H_3^+$  : No ion-neutral crossing

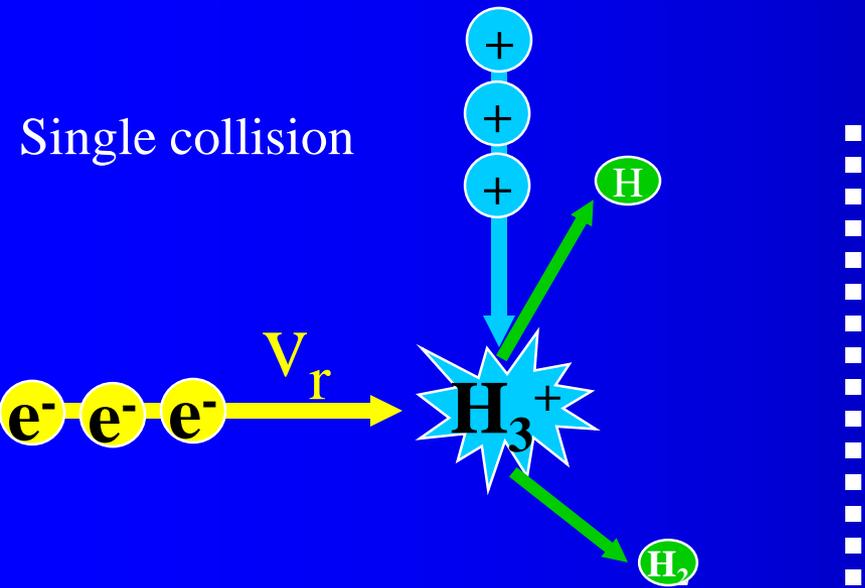
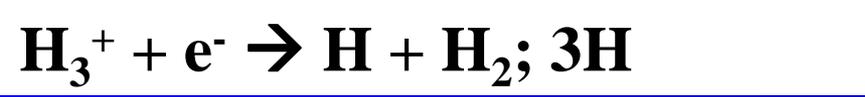


Indirect process

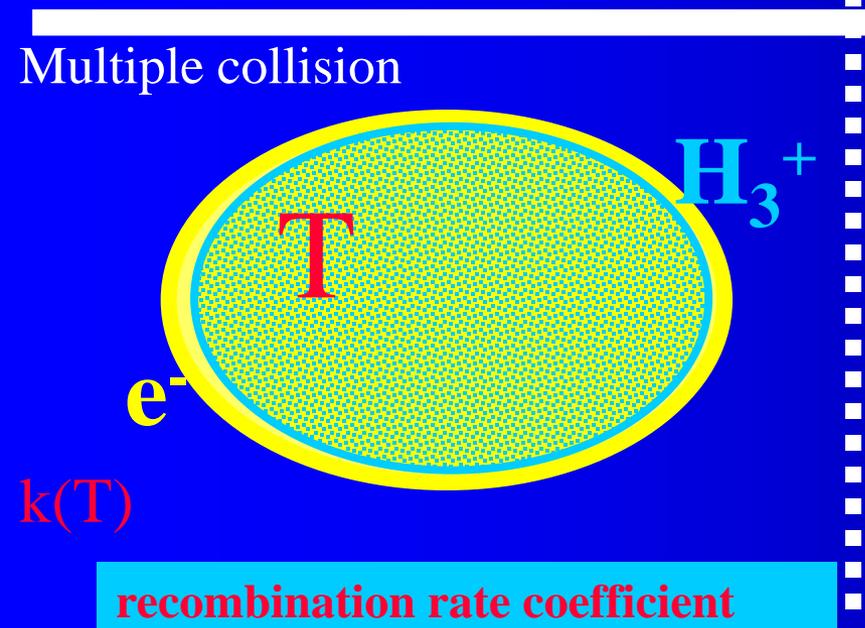
~~Direct process~~

Kinetic Energy Release

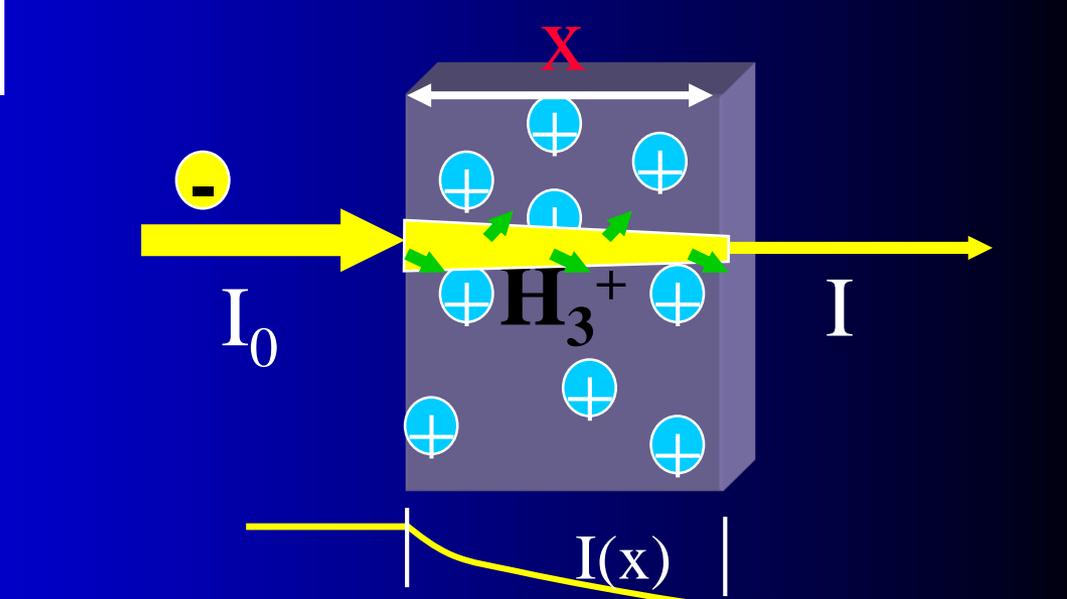
$A(n)+B(n')$



$\sigma(v_r)$  recombination cross section

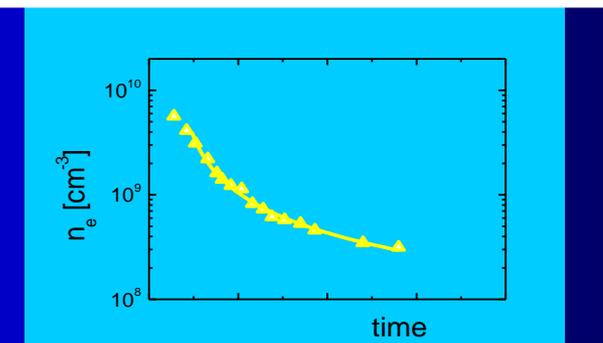


$k(T)$  recombination rate coefficient



$I = I_0 \exp(-\sigma n_i x)$

$k(T) = \langle v\sigma \rangle$



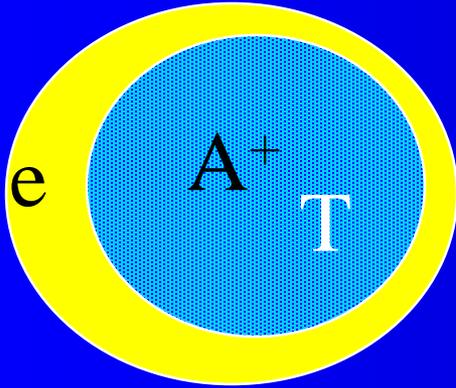
$\alpha$

$dn_i/dt = -kn_i n_e$

$dn_e/dt = -kn_e^2$

# Concept of recombination rate coefficient (plasma binary reactions)

at T



$$dN_A/dt = -\alpha n_e N_A$$

**RECOMBINATION RATE COEFFICIENT**

$$\alpha = \alpha(T)$$

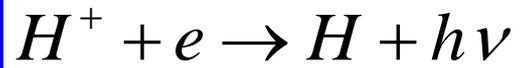
$$\sigma = \sigma(v) = \sigma(\epsilon)$$

**Collision rate coefficient, Recombination rate coefficient**

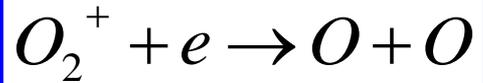
$$\alpha = \langle \sigma u_r \rangle$$

# Recombination processes in plasma

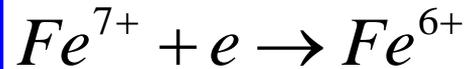
## Binary Recombination



RR



DR

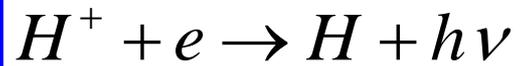


DiR

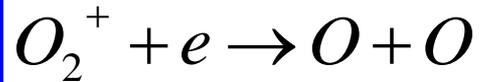
$$\frac{dn_e}{dt} = \frac{d[O_2^+]}{dt} = -\alpha[O_2^+]n_e = -\alpha n_e^2$$

# Recombination processes in plasma

## Binary Recombination



RR



DR

$$\frac{dn_e}{dt} = \frac{d[O_2^+]}{dt} = -\alpha[O_2^+]n_e = -\alpha n_e^2$$



DiR

## Ternary electron assisted recombination



$$\frac{dn_e}{dt} = \frac{d[Ar^+]}{dt} = -K_e[Ar^+]n_e^2 = -\alpha_{eff}[Ar^+]n_e$$

Collisional Radiative Recombination CRR

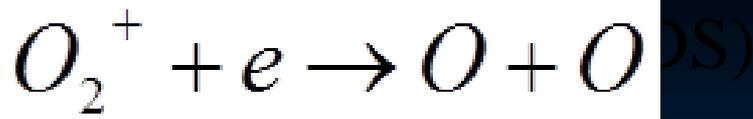
$$\alpha_{eff} = K_e n_e$$

## Ternary neutral assisted recombination



$$\frac{dn_e}{dt} = \frac{d[Ar^+]}{dt} = -K_M[Ar^+]n_e[He] = -\alpha_{eff}[Ar^+]n_e$$

$$\alpha_{eff} = K_M [He]$$



234311-2 Petrignani *et al.*

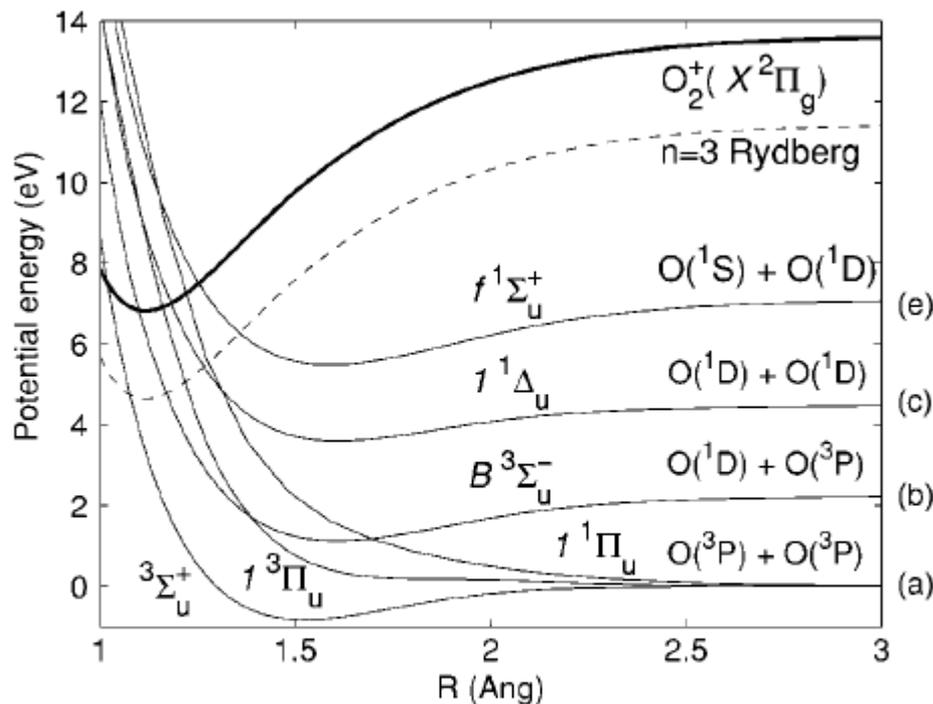
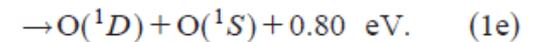
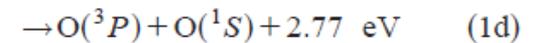
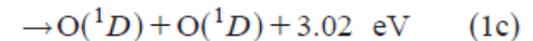
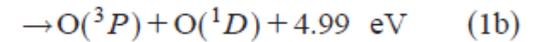
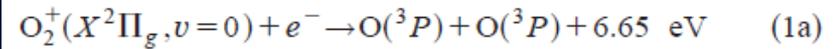


FIG. 1. Schematic of the diabatic potential curves relevant for the DR of  $O_2^+$ . The dissociation limits connected with each valence capture state are given on the right. The labels (a)–(c), and (e) refer to Eqs. (1a)–(1c) and (1e), respectively.

Five exothermic channels are available for vibrational ground state  $O_2^+$  ions in zero relative energy collisions with electrons. They are summarized as follows with the associated kinetic energy releases:



6682 J. Chem. Phys., Vol. 114, No. 15, 15 April 2001

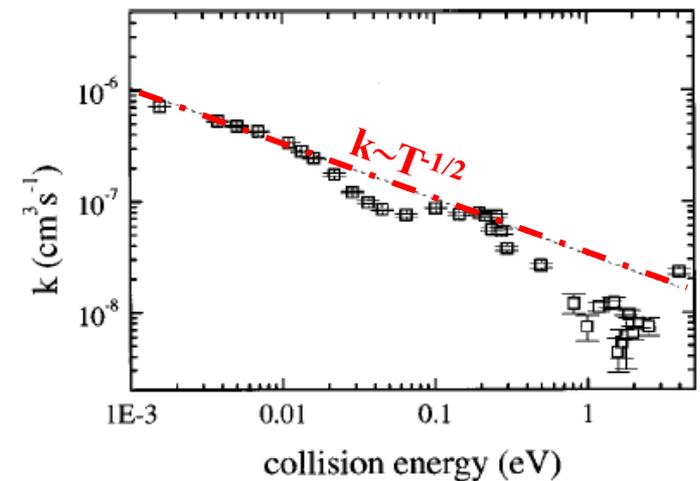
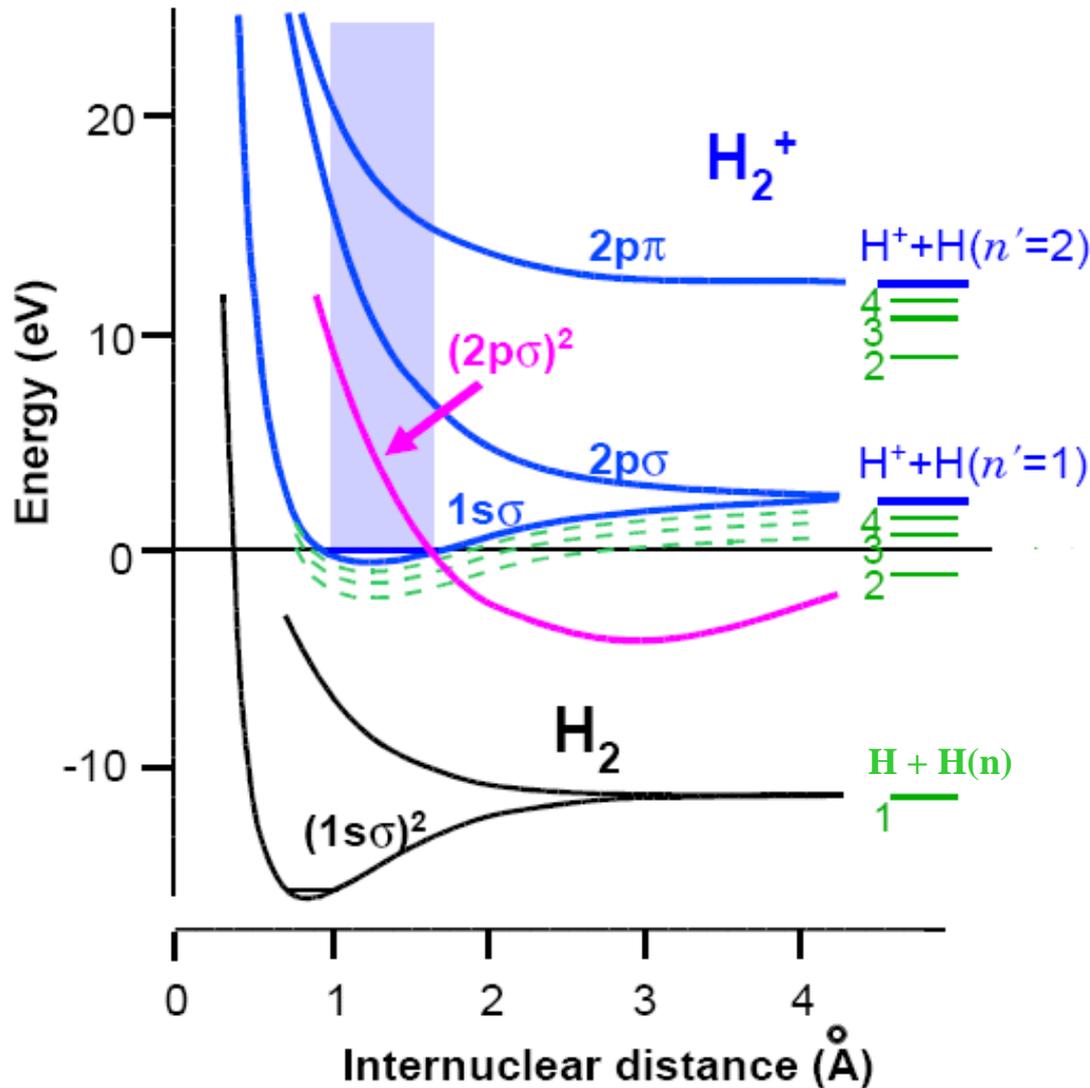


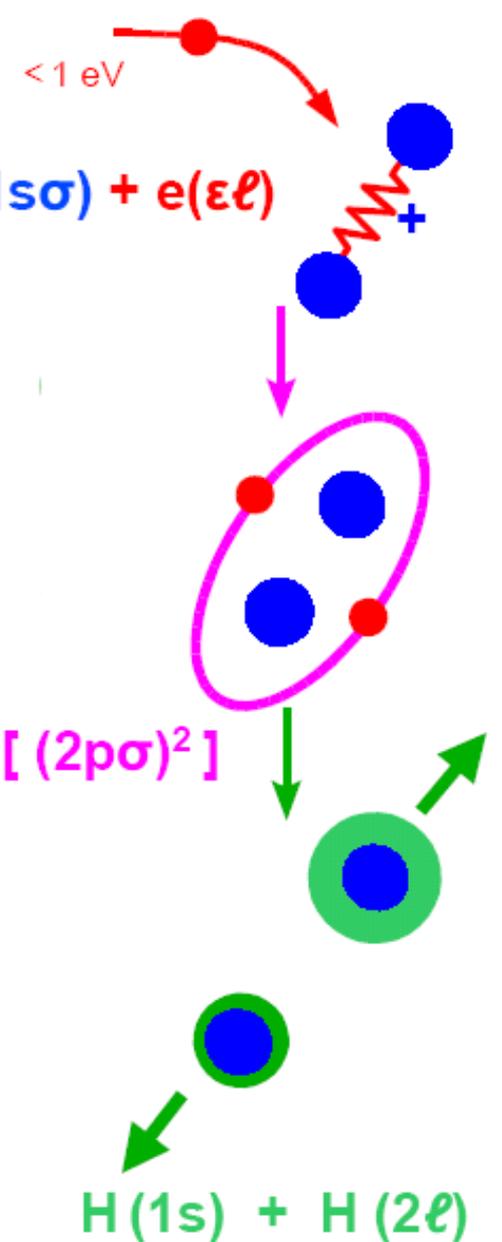
FIG. 2. DR rate coefficient  $k$  as a function of electron collision energy from 1 meV to 5 eV. Statistical errors are shown at the  $1\sigma$  level. The dotted line shows the threshold  $E^{-1/2}$  behavior. Both the rate coefficient and the energy are shown on a logarithmic scale.

# Electron - Ion Recombination

## Electron collisions with $H_2^+$



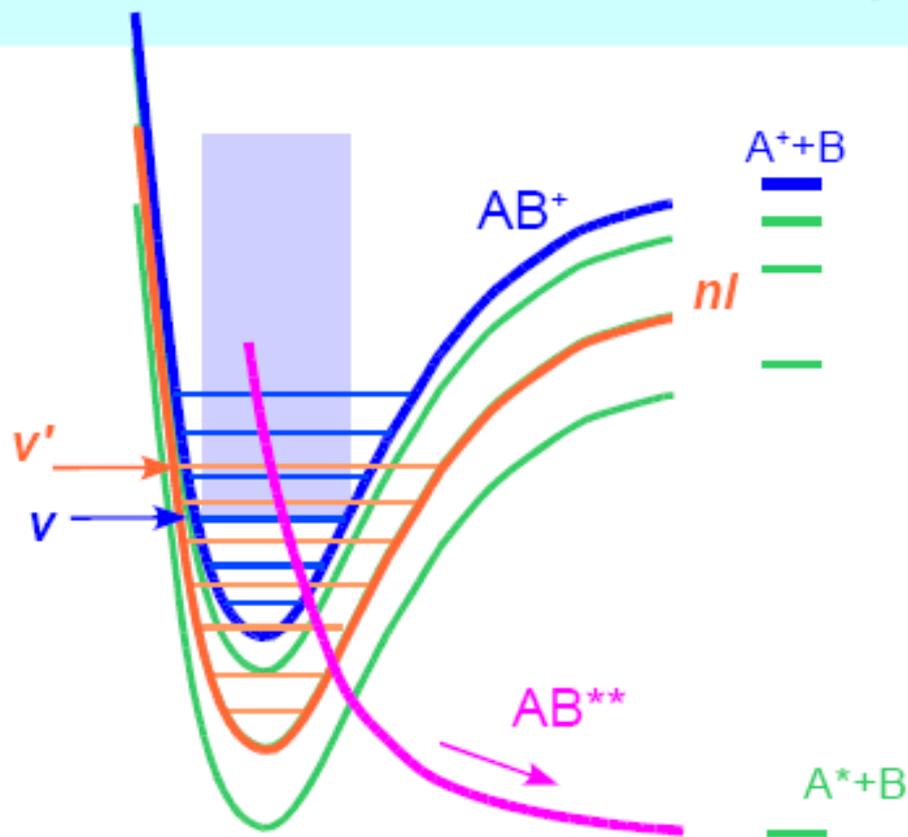
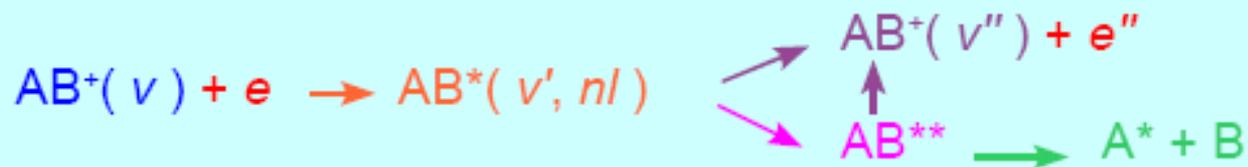
<1 eV



# Resonances

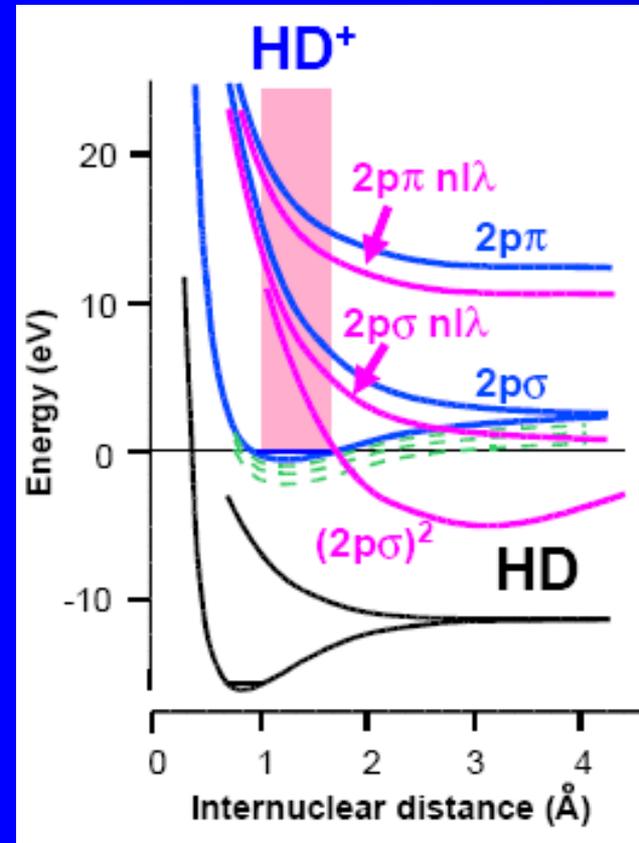
## Resonances

### Autoionizing and pre-dissociating Rydberg states

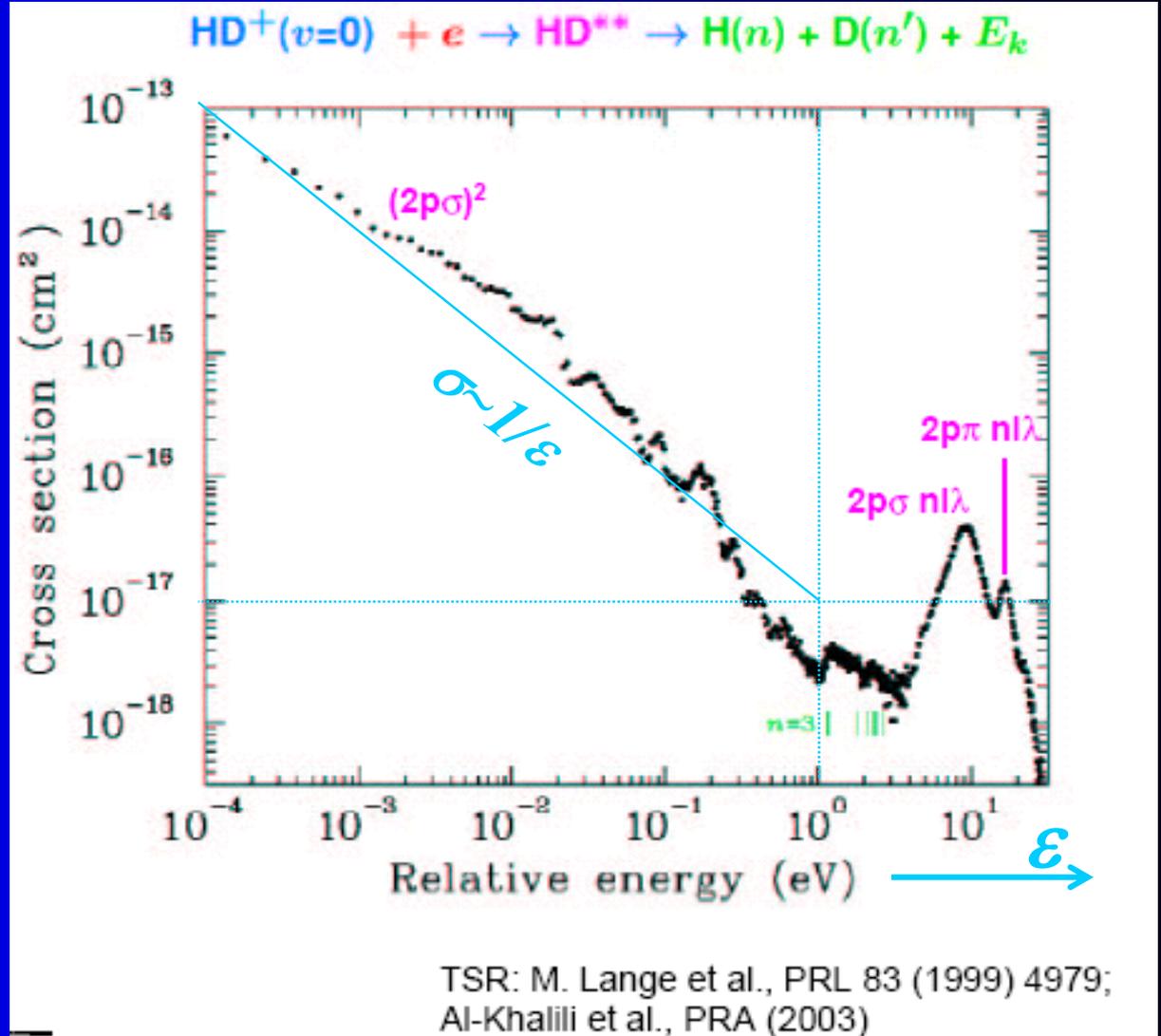
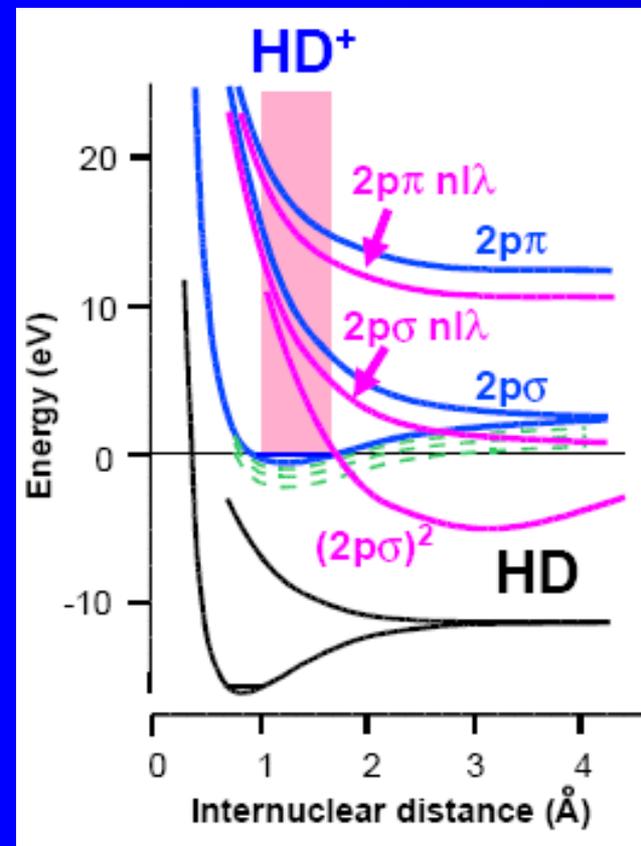


# Dissociative recombination

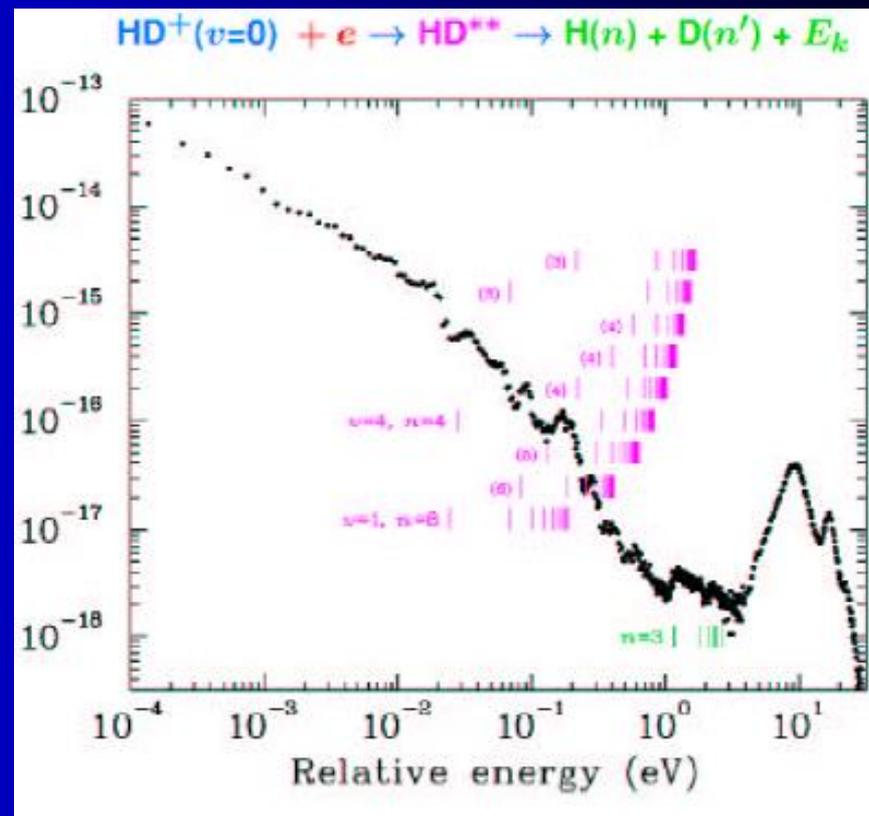
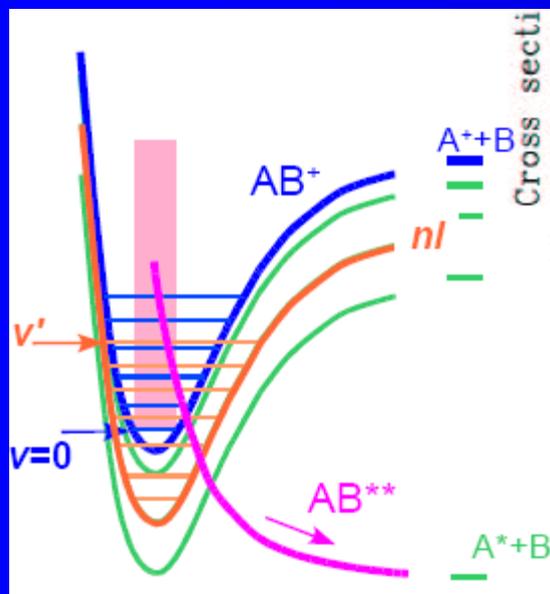
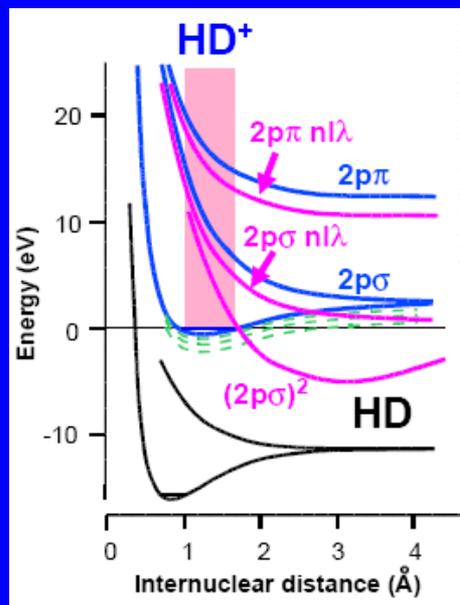
# Resonances



# Dissociative recombination



# Dissociative recombination HD+



Scan of electron ion relative energy  $E$

Electron temperature  $kT_{\text{Per}}=4\text{meV}$  ( $30\text{meV}$  for  $E>0.3\text{eV}$ )

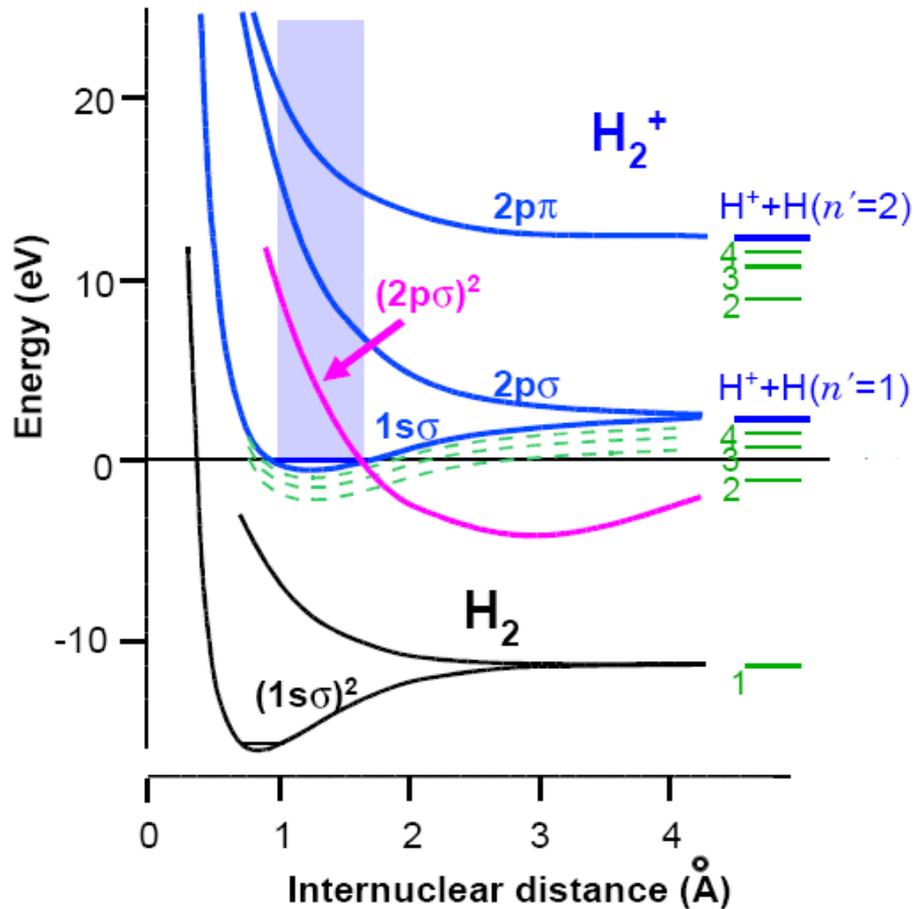
$kT_{\text{Par}}=0.1\text{meV}$

Energy resolution  $\sim 4\dots 8\text{meV}$  ( $E<0.08\text{eV}$ )

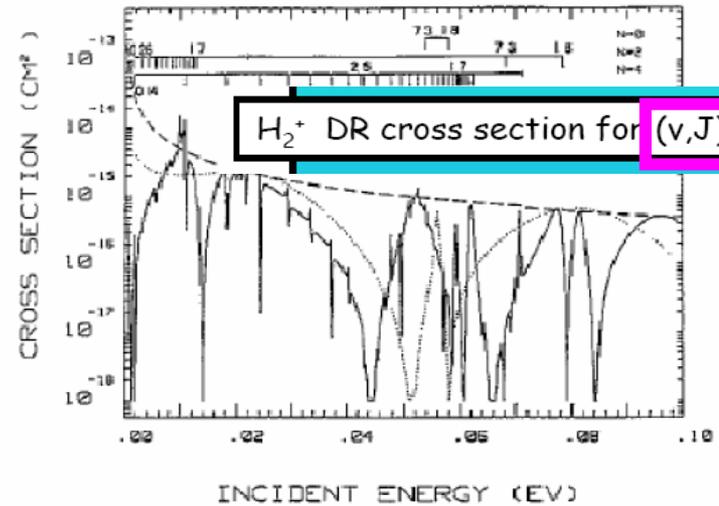
Absolute accuracy of cross section ca.  $\pm 30\%$

# Recombination $H_2^+$

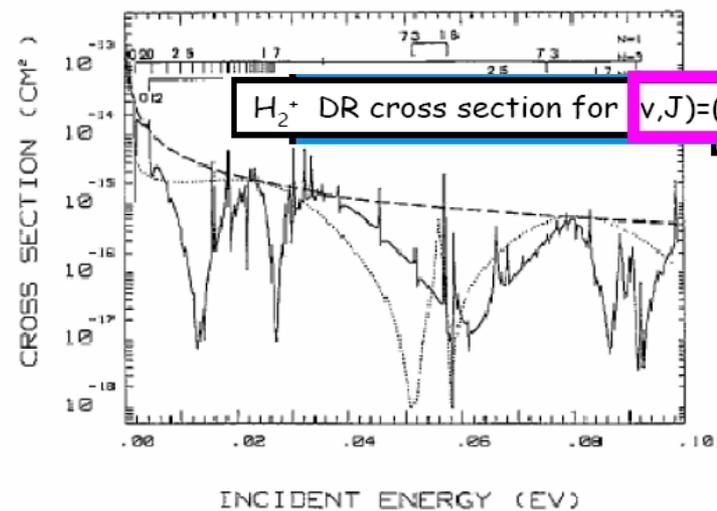
## Electron collisions with $H_2^+$



H. Takagi, J. Phys. B, 26, 4815 (1993)

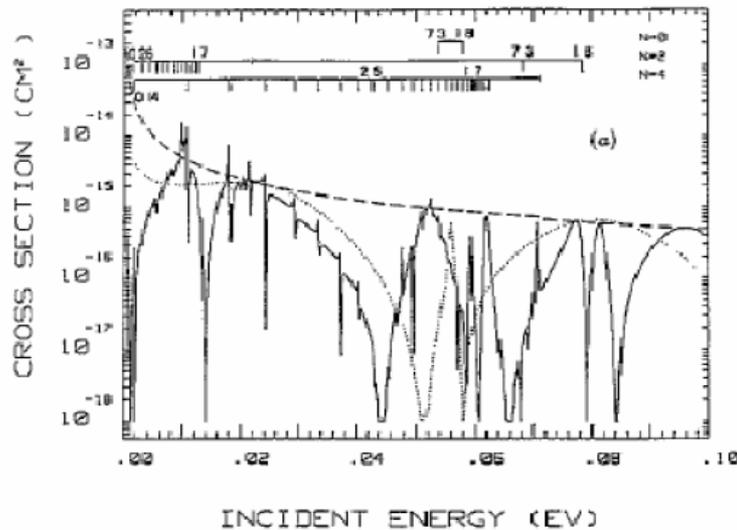


$H_2^+$  DR



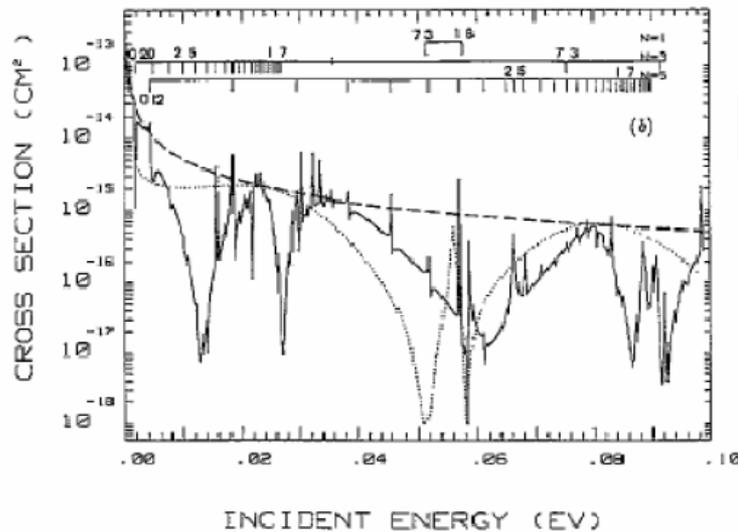
# Recombination only one rotational quanta change the whole spectra

H. Takagi, J. Phys. B, 26, 4815 (1993)



$H_2^+$  DR cross section for  $(v,J)=(0,0)$

Only one rotational quanta of excitation changes the whole spectra!!



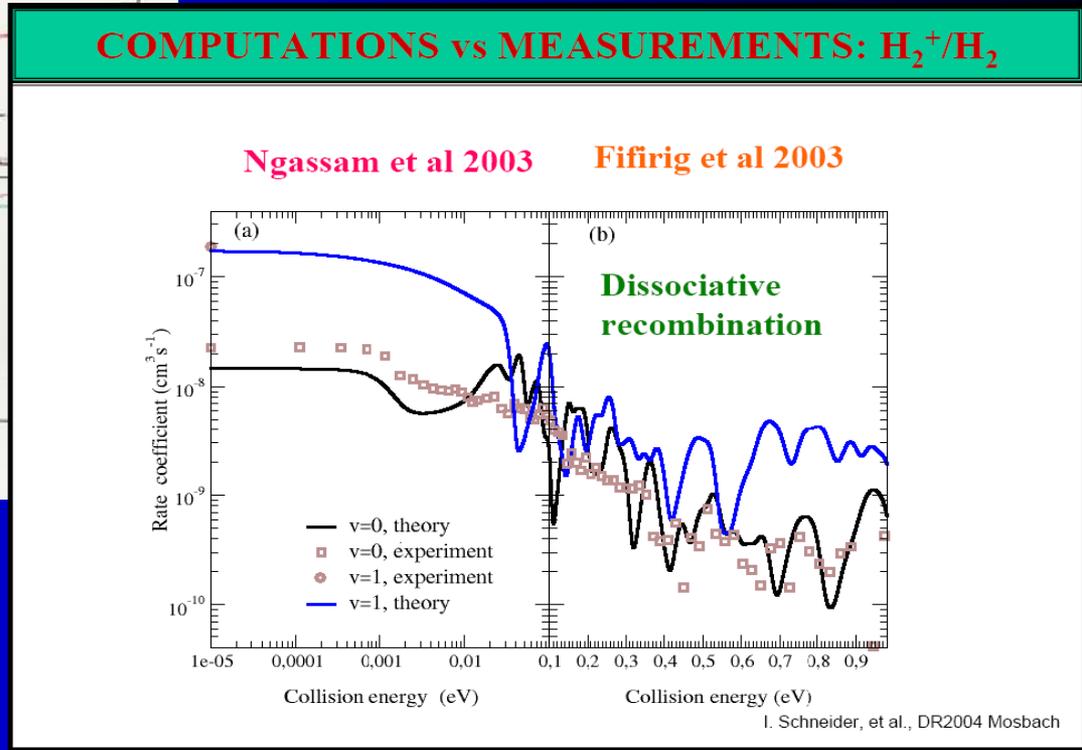
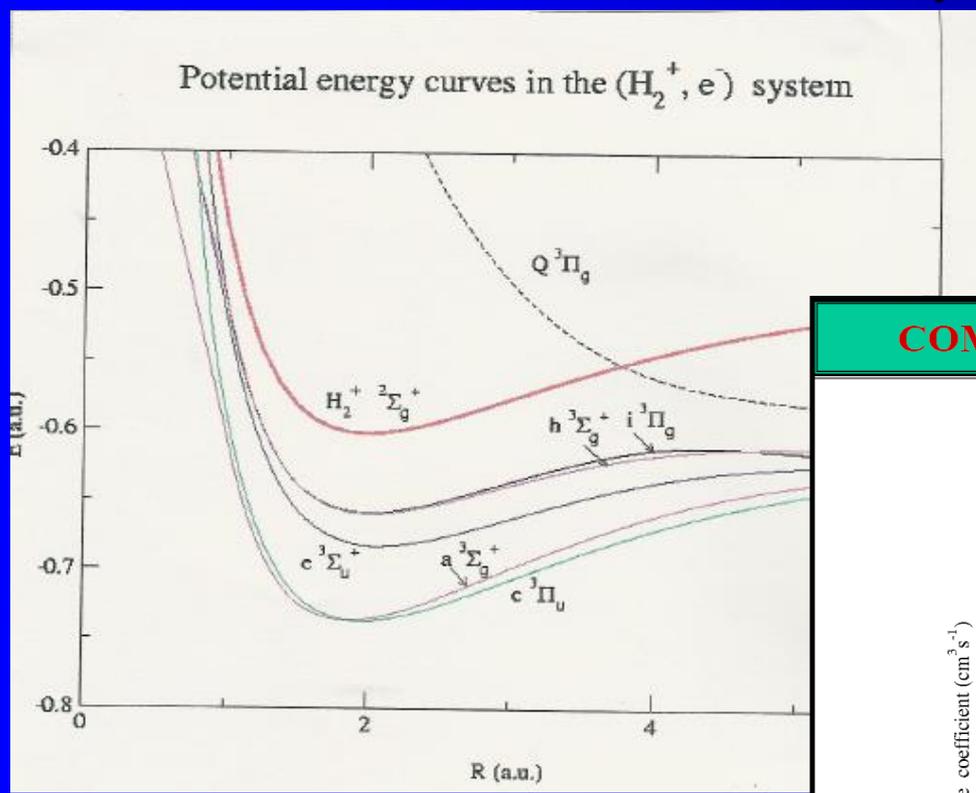
$H_2^+$  DR cross section for  $(v,J)=(0,1)$

In fact, these resonances have never been individually observed!

- Position
  - Depth
  - Shape
- teach everything about the dynamics taking place during the dissociation.

D. Zaitman, et al., DR2004, Mosbach

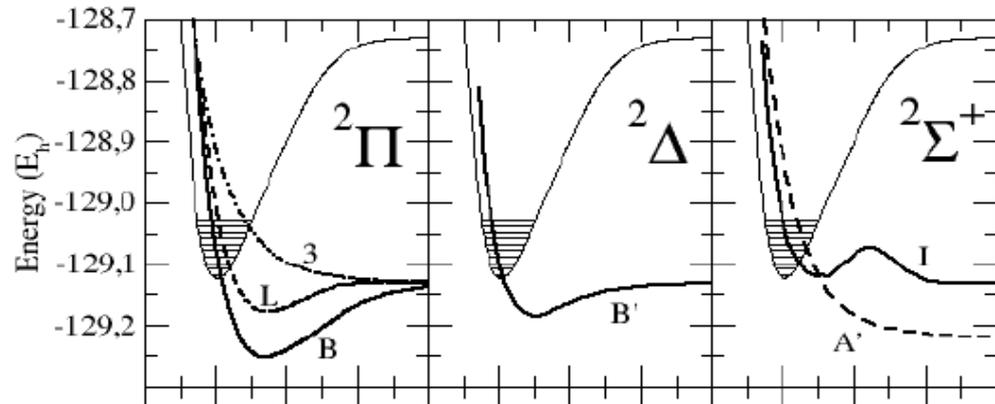
# Recombination calculation and theory $H_2^+$ .....vibrational excitation



Different energy region

# Recombination $\text{NO}^+$

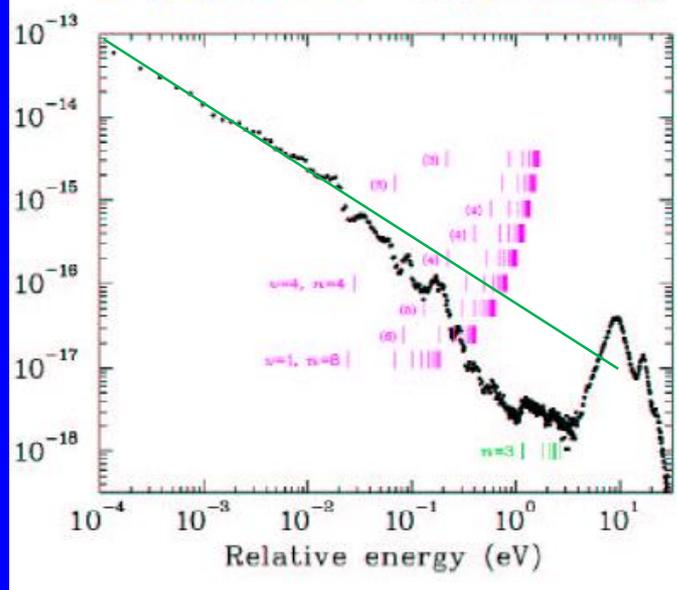
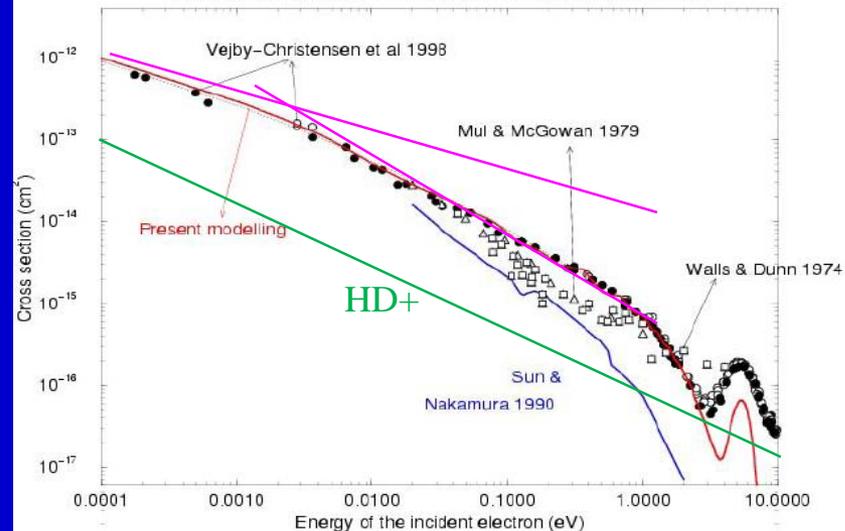
## Tennyson et al 1996-2000



## Comparison with ASTRID

### Schneider et al 2000

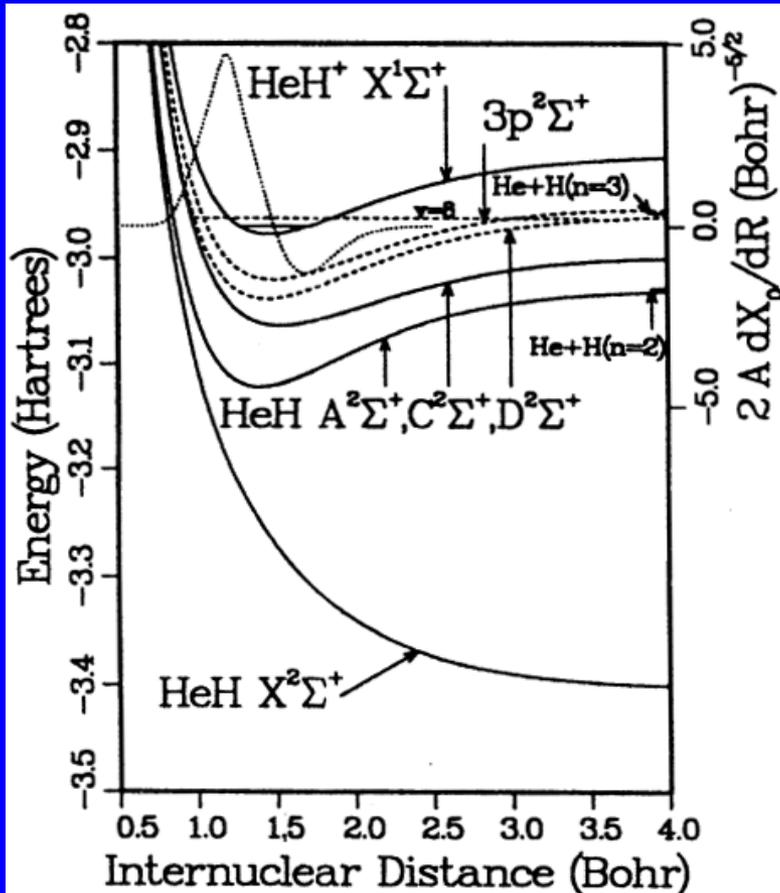
$\text{NO}^+(\text{X}^1\Sigma^+ v_r=0)$  dissociative recombination  
MQDT modelling based on R-matrix molecular data v. experiment



# Theoretical background

## Dissociative Recombination without a Curve Crossing

Theory predicted: DR rate coefficient is vary small  $\sim 10^{-11} \text{ cm}^3\text{s}^{-1}$



HeH<sup>+</sup> and HCO<sup>+</sup> ions-  
examples of a non-crossing case.  
However, experiments gave  
 $\alpha \approx 2 \times 10^{-8}$  and  $\alpha \approx 2 \times 10^{-7} \text{ cm}^3\text{s}^{-1}$

**A new mechanism has been proposed!**

Multi-step indirect  
dissociative recombination  
("tunneling mode" recombination)

2019

Cite as: O. Novotný *et al.*, *Science*  
10.1126/science.aax5921 (2019).

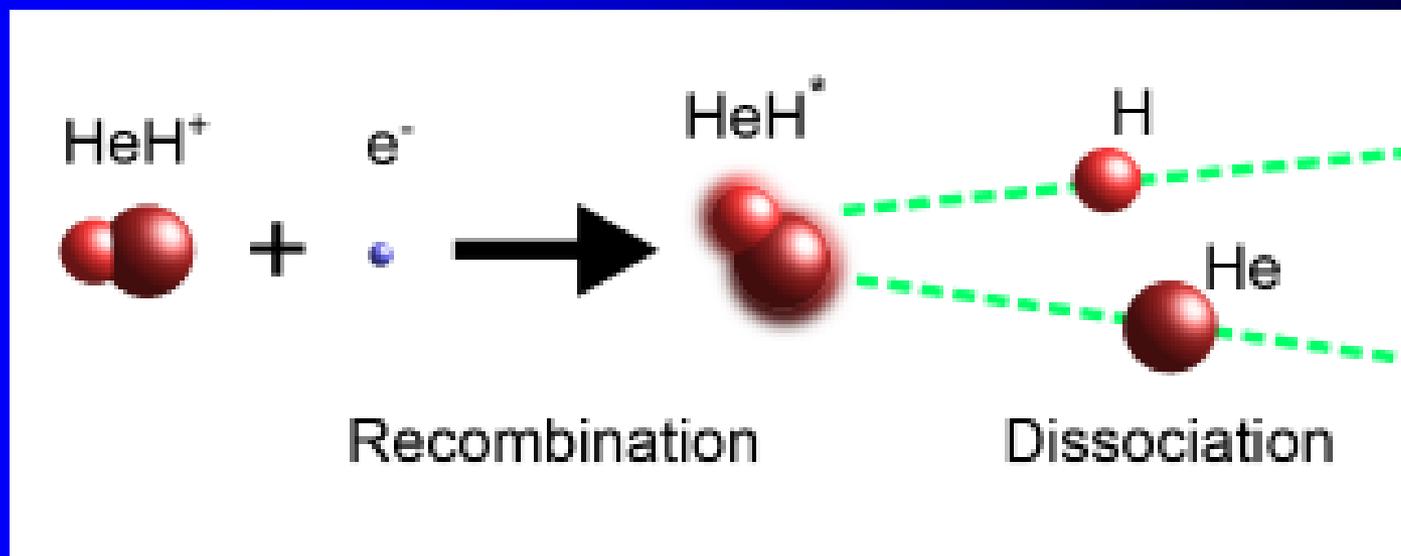
## Quantum-state-selective electron recombination studies suggest enhanced abundance of primordial HeH<sup>+</sup>

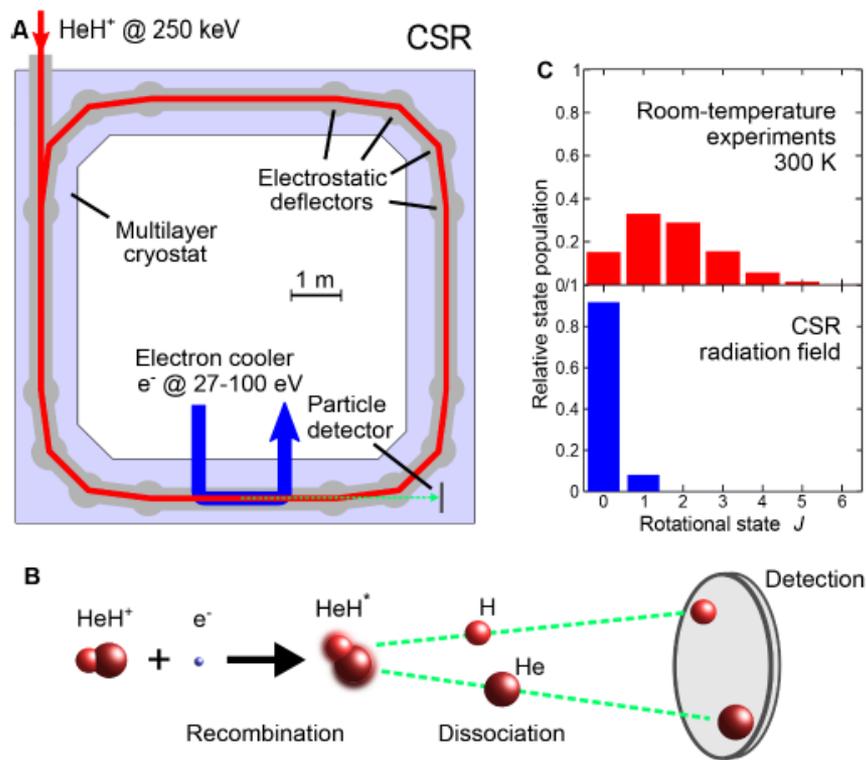
Oldřich Novotný<sup>1\*</sup>, Patrick Wilhelm<sup>1</sup>, Daniel Paul<sup>1</sup>, Ábel Kálósi<sup>1,2</sup>, Sunny Saurabh<sup>1</sup>, Arno Becker<sup>1</sup>, Klaus Blaum<sup>1</sup>, Sebastian George<sup>1,3</sup>, Jürgen Göck<sup>1</sup>, Manfred Grieser<sup>1</sup>, Florian Grussie<sup>1</sup>, Robert von Hahn<sup>1</sup>, Claude Krantz<sup>1</sup>, Holger Kreckel<sup>1</sup>, Christian Meyer<sup>1</sup>, Preeti M. Mishra<sup>1</sup>, Damian Muell<sup>1</sup>, Felix Nuesslein<sup>1</sup>, Dmitry A. Orlov<sup>1</sup>, Marius Rimmler<sup>1</sup>, Viviane C. Schmidt<sup>1</sup>, Andrey Shornikov<sup>1</sup>, Aleksandr S. Terekhov<sup>4</sup>, Stephen Vogel<sup>1</sup>, Daniel Zajfman<sup>5</sup>, Andreas Wolf<sup>1</sup>

<sup>1</sup>Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany. <sup>2</sup>Charles University, 18000 Praha, Czech Republic. <sup>3</sup>Universität Greifswald, Institut für Physik, 17487 Greifswald, Germany. <sup>4</sup>Rzhanov Institute of Semiconductor Physics, Novosibirsk 630090, Russia. <sup>5</sup>Weizmann Institute of Science, Rehovot 76100, Israel.

\*Corresponding author. Email: oldrich.novotny@mpi-hd.mpg.de

The epoch of first star formation in the early universe was dominated by simple atomic and molecular species consisting mainly of two elements: hydrogen and helium. Gaining insight into this constitutive era requires thorough understanding of molecular reactivity under primordial conditions. We used a cryogenic ion storage ring combined with a merged electron beam to measure state-specific rate coefficients of dissociative recombination, a process by which electrons destroy molecular ions. We found a dramatic decrease of the electron recombination rates for the lowest rotational states of HeH<sup>+</sup>, compared to previous measurements at room temperature. The reduced destruction of cold HeH<sup>+</sup> translates into an enhanced abundance of this primordial molecule at redshifts of first star and galaxy formation.





**Fig. 1. Dissociative recombination in the cryogenic storage ring CSR.** (A) Scheme of the CSR ring structure with injected and stored HeH<sup>+</sup> ion beam (red), merged electron beam (blue), reaction products (green) and particle detector. (B) Reaction scheme and position-sensitive detection of coincident fragments. (C) Equilibrium rotational state populations of HeH<sup>+</sup> for previous studies (300 K) and the estimated radiation field in the CSR.

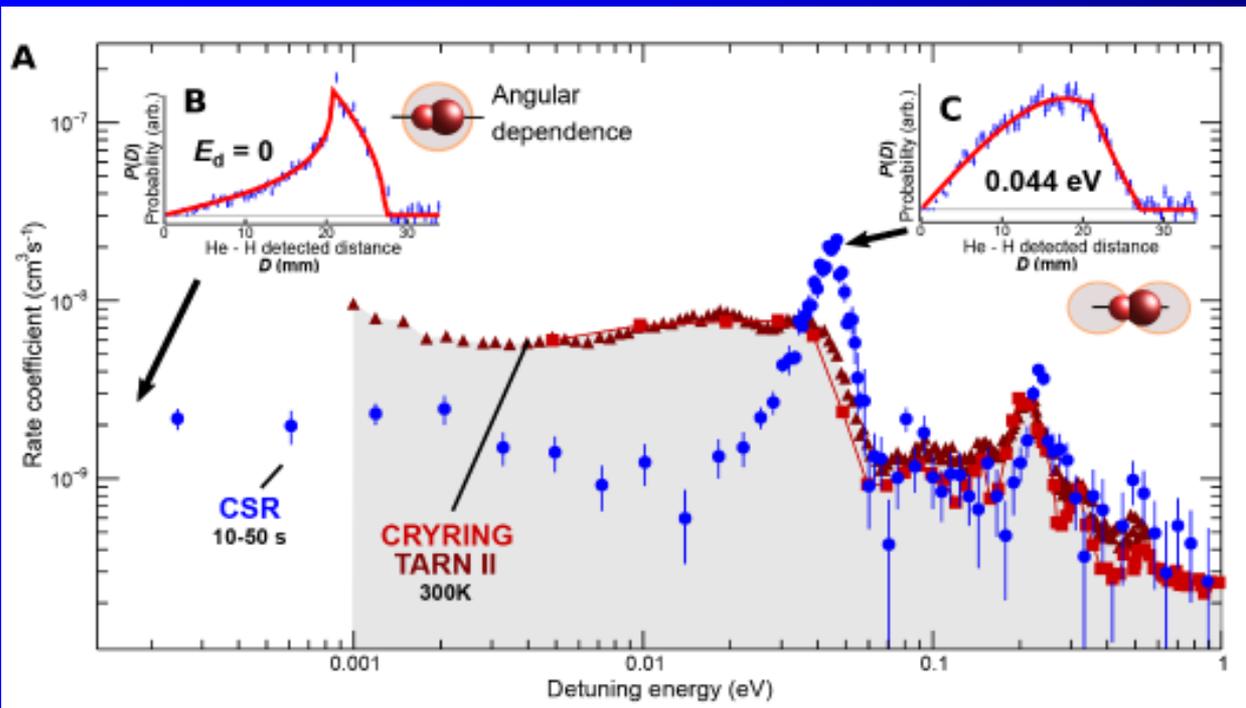
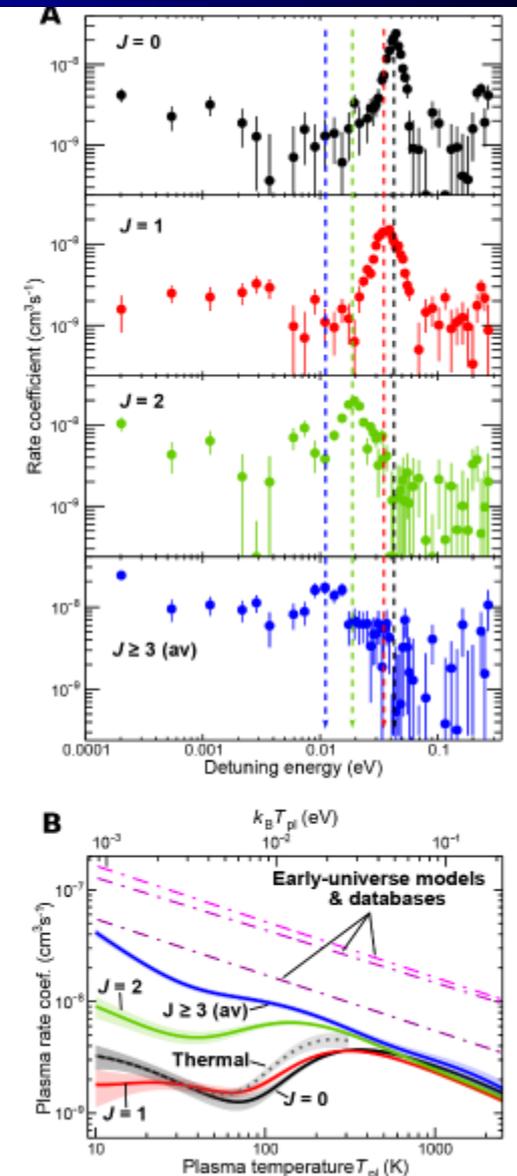


Fig. 2. DR for rotationally cold HeH<sup>+</sup>. (A) Blue dots: merged-beams rate coefficient  $\alpha_{DR}$  as a function of the detuning energy  $E_d$  after relaxation to >50%  $J = 0$  (this experiment, 10 s < t < 50 s, mean  $\pm$  SD); absolute scaling uncertainty  $\pm 20\%$  (SEM). Red symbols: room-temperature data from Ref. (11) (squares, absolute scaling uncertainty  $\pm 10\%$  SEM) and from Ref. (12) (triangles, scaled to Ref. (11) at 0.03 eV). (B) Fragment distance distribution projected into the detector plane for  $E_d = 0$  (blue) with fit (19) for isotropic angular distribution (red). (C) Projected fragment distance distribution for  $E_d = 0.044$  eV (blue) with fit (19) for a  $|Y_{10}|^2$  angular distribution of the fragments (red). The angular dependences in (B) and (C) are indicated schematically.

Fig. 4. Rotational-state selective DR rates for HeH<sup>+</sup>. (A) Merged-beams rate coefficients  $\alpha_{\text{DR}}^J(E_d)$  for  $J \leq 2$  and average for  $J \geq 3$  (mainly 3 and 4; mean  $\pm$  SD). The dashed lines mark the shift of the maximum as  $J$  increases. (B) Full lines: single- $J$  plasma rate coefficients  $\alpha_{\text{DR,pl}}^J(T_{\text{pl}})$  for  $J \leq 2$  and average for  $J \geq 3$  (mainly 3 and 4; mean with shaded areas as  $\pm$  SD). Dotted: fully thermal rate coefficient  $\alpha_{\text{DR,therm}}(T_{\text{rot}} = T_{\text{pl}})$ . Dashed-dotted: values applied in early-universe models (21, 22) and astrochemistry databases (23–25). See (19) for further discussion, numerical fitting functions and parameters.

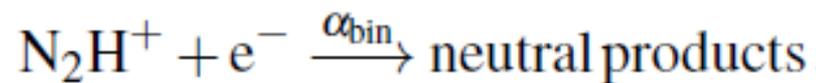


# Dissociative recombination of $\text{N}_2\text{H}^+$ ions with electrons in the temperature range of 80–350 K

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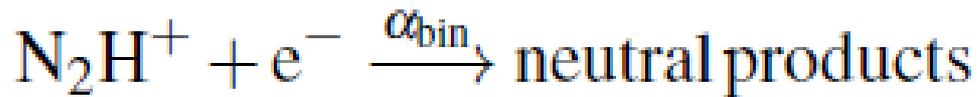
Dmytro Shapko, Petr Dohnal , Miroslava Kassayová, Ábel Kálosi , Serhiy Rednyk , Štěpán Roučka, Radek Plašil , Lucie D. Augustovičová, Rainer Johnsen , Vladimír Špirko , and Juraj Glošík



Recombination of  $\text{N}_2\text{H}^+$  ions with electrons was studied using a stationary afterglow with cavity ring-down spectrometer. We probed in situ the time evolutions of number densities of different rotational and vibrational states of recombining  $\text{N}_2\text{H}^+$  ions and determined the thermal recombination rate coefficients for  $\text{N}_2\text{H}^+$  in the temperature range of 80 – 350 K. The newly calculated vibrational transition moments of  $\text{N}_2\text{H}^+$  are used to explain the different values of recombination rate coefficients obtained in some of the previous studies. No statistically significant dependence of the measured recombination rate coefficient on the buffer gas number density was observed.

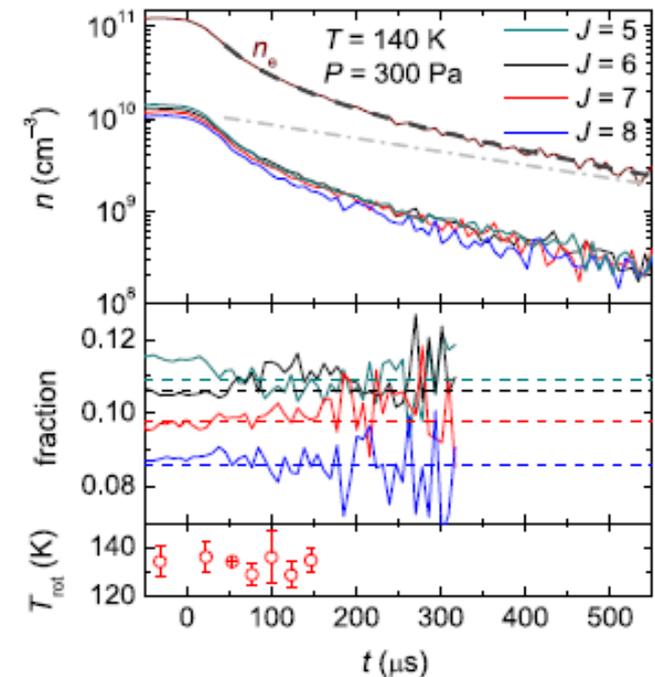
## I. INTRODUCTION

$\text{N}_2\text{H}^+$ , an important interstellar ion, has been observed in different interstellar environments such as dark and translucent clouds<sup>1,2</sup>, protostellar cores<sup>3</sup>, protoplanetary disks<sup>4</sup> and is considered to play a role in the atmospheric chemistry of Titan<sup>5</sup>.  $\text{N}_2\text{H}^+$  serves as an important tracer for  $\text{N}_2$  in dark clouds, therefore detailed information on production and destruction processes of  $\text{N}_2\text{H}^+$  could help with the prediction of  $\text{N}_2$  abundance in this environment.  $\text{N}_2\text{H}^+$  in the interstellar medium is mainly produced in proton transfer from  $\text{H}_3^+$  to  $\text{N}_2$  and its main destruction mechanisms are proton transfer to CO and dissociative recombination with electrons<sup>6</sup>.



## II. EXPERIMENT

The recombination rate coefficients<sup>7,32</sup> are measured in a stationary afterglow (SA) in conjunction with cavity ring-down spectroscopy (CRDS) to monitor the decay of the densities of different rotational and vibrational states of  $\text{N}_2\text{H}^+$  ions. The plasma is generated in a pulsed microwave discharge in a fused silica tube (inner diameter  $\approx 1.3$  cm). The microwave generator is equipped with an external fast high-voltage switch to cut off the power to the magnetron within a fall time of less than  $30 \mu\text{s}$ . A low microwave power in the range of  $10 - 25$  W, with  $\approx 40\%$  duty cycle, is used to avoid excessive heating of the gas during the discharge. The discharge tube temperature ( $T_{\text{tec}}$ ) is measured by a thermocouple outside of the discharge and can be varied between  $80$  and  $350$  K.



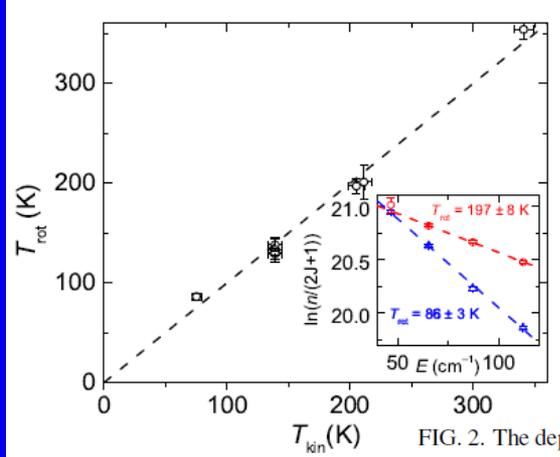
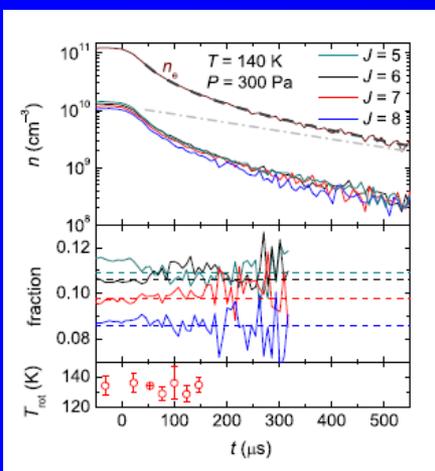


FIG. 2. The dependence of the rotational temperature measured during the discharge on kinetic temperature. All the displayed data were obtained in helium buffer gas. Insert: An example of the Boltzmann plots used for determination of the rotational temperature obtained at  $T = 200$  K and  $T = 78$  K.

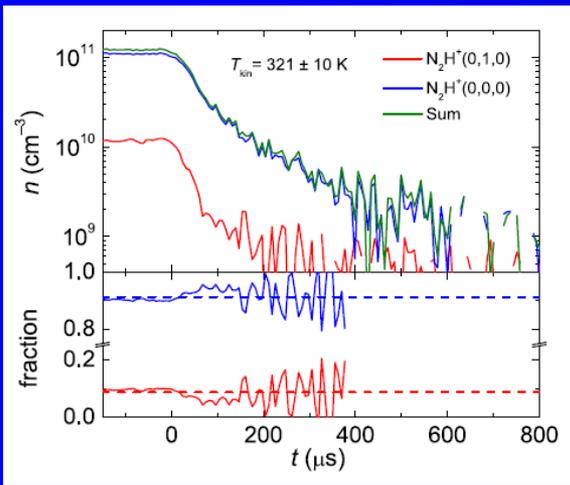
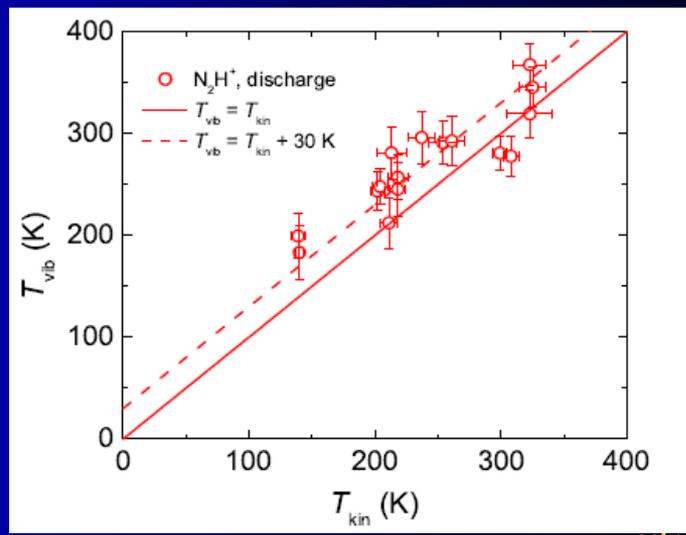


FIG. 3. An example of measured time evolutions of number densities of  $N_2H^+$  ions in the ground and the first excited vibrational state. The lower panel shows the relative fractions of the vibrational states and the dashed lines denote the corresponding fraction in thermal equilibrium at temperature of 321 K. The particular vibrational states number densities were calculated from the measured number densities of the  $J = 6$  rotational state of the ground vibrational state and of  $J = 9$  state of the  $(01^1_0)$  vibrational state under the assumption of the same rotational temperature in both vibrational states.

FIG. 4. Dependence of the measured vibrational temperature  $T_{vib}$  on kinetic temperature  $T_{kin}$  of the  $N_2H^+$  ions measured in the discharge. The kinetic temperature was obtained from the Doppler broadening of the P(6) line of the  $(200) \leftarrow (000)$  vibrational band of  $N_2H^+$ . It was assumed that the rotational temperature of  $(000)$  and  $(010)$  states is equal to  $T_{kin}$ . The vibrational temperature was then evaluated from the P(6) line of the  $(200) \leftarrow (000)$  vibrational band and from the R(9)<sup>f</sup> line of the  $(210) \leftarrow (010)$  vibrational band of the  $N_2H^+$  ion. The full line denotes equality of  $T_{vib} = T_{kin}$  and the dashed line indicates  $T_{vib} = T_{kin} + 30$  K. The displayed errors are statistical errors of the fits.



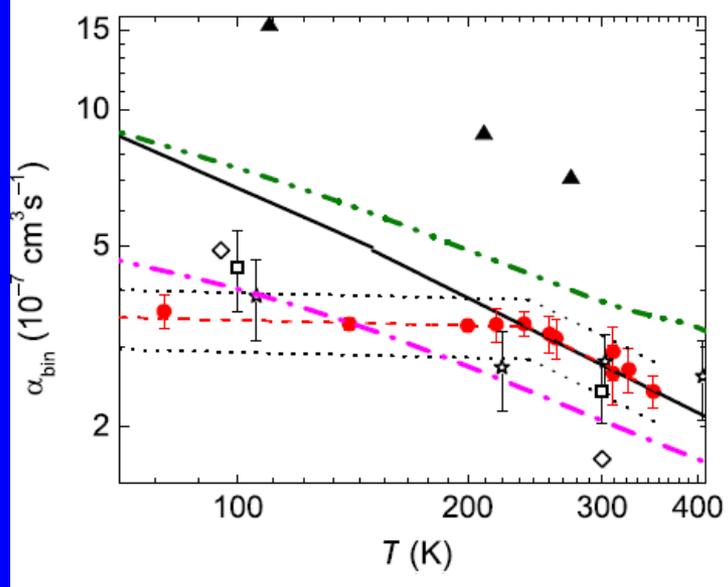


FIG. 8. The temperature dependence of the measured recombination rate coefficients of  $\text{N}_2\text{H}^+$  (full circles, the value of  $\alpha_{\text{bin}}$  at 350 K was obtained in  $\text{H}_2$  buffer gas, for the rest of the data points, helium buffer gas was used) compared to values obtained in previous experiments. Rhomboids: FALP<sup>11</sup>, squares: FALP<sup>13</sup>, stars: FALP<sup>14</sup>, triangles: stationary afterglow with absorption spectroscopy<sup>17</sup>, full line: ion storage ring<sup>6</sup>, double-dot-dashed line: merged beams<sup>8</sup> and to recent theoretical calculations by Fonseca dos Santos<sup>21</sup> (dot-dashed line, the rate coefficient was calculated from the cross sections for the direct and indirect recombination process in ref.<sup>21</sup>). The dashed line denotes fit to the data:  $\alpha_{\text{N}_2\text{H}^+} = (2.81 \pm 0.04) \times 10^{-7} (T/300)^{-(0.81 \pm 0.10)} \text{ cm}^3 \text{ s}^{-1}$  for  $T > 240 \text{ K}$  and  $\alpha_{\text{N}_2\text{H}^+} = (3.29 \pm 0.04) \times 10^{-7} (T/300)^{-(0.06 \pm 0.02)} \text{ cm}^3 \text{ s}^{-1}$  otherwise. The dotted lines show 15% deviation from the fitted value (estimated systematic error of the measurement reflects mainly the uncertainty in the effective discharge column length and in the calculated vibrational transition moments).

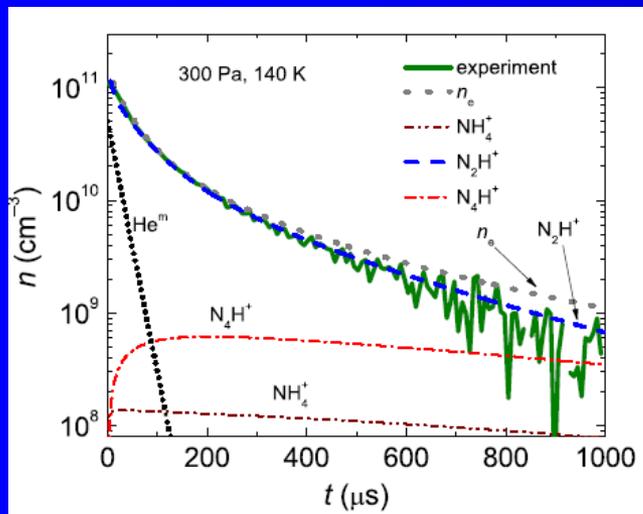


FIG. 9. Time evolution of the measured overall number density of  $\text{N}_2\text{H}^+$  ions (full line) compared to the results obtained from the model of chemical kinetics. The data were obtained at  $T = 140 \text{ K}$ ,  $[\text{He}] = 1.5 \times 10^{17} \text{ cm}^{-3}$ ,  $[\text{Ar}] = 2.5 \times 10^{14} \text{ cm}^{-3}$ ,  $[\text{H}_2] = 5 \times 10^{14} \text{ cm}^{-3}$  and  $[\text{N}_2] = 4 \times 10^{13} \text{ cm}^{-3}$  (same as in Figure 1) and  $[\text{NH}_3] = 5 \times 10^{11} \text{ cm}^{-3}$ .  $[\text{He}^{\text{m}}](t=0) = 1/3 n_e(t=0)$ .

## Ternary recombination

### Ternary electron assisted recombination



$$\frac{dn_e}{dt} = \frac{d[Ar^+]}{dt} = -K_e [Ar^+] n_e^2 = -\alpha_{eff} [Ar^+] n_e$$

Collisional Radiative Recombination CRR

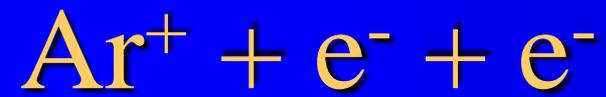
$$\alpha_{eff} = K_e n_e$$

### Ternary neutral assisted recombination



$$\frac{dn_e}{dt} = \frac{d[Ar^+]}{dt} = -K_M [Ar^+] n_e [He] = -\alpha_{eff} [Ar^+] n_e$$

$$\alpha_{eff} = K_M [He]$$



Collisional Radiative Recombination -CRR

$$\frac{dn_e}{dt} = -K_{CRR} [\text{Ar}^+] n_e^2 - \frac{n_e}{\tau_D} = -K_{CRR} n_e^3 - \frac{n_e}{\tau_D}$$

$$\alpha_{CRR} = K_{CRR} n_e$$

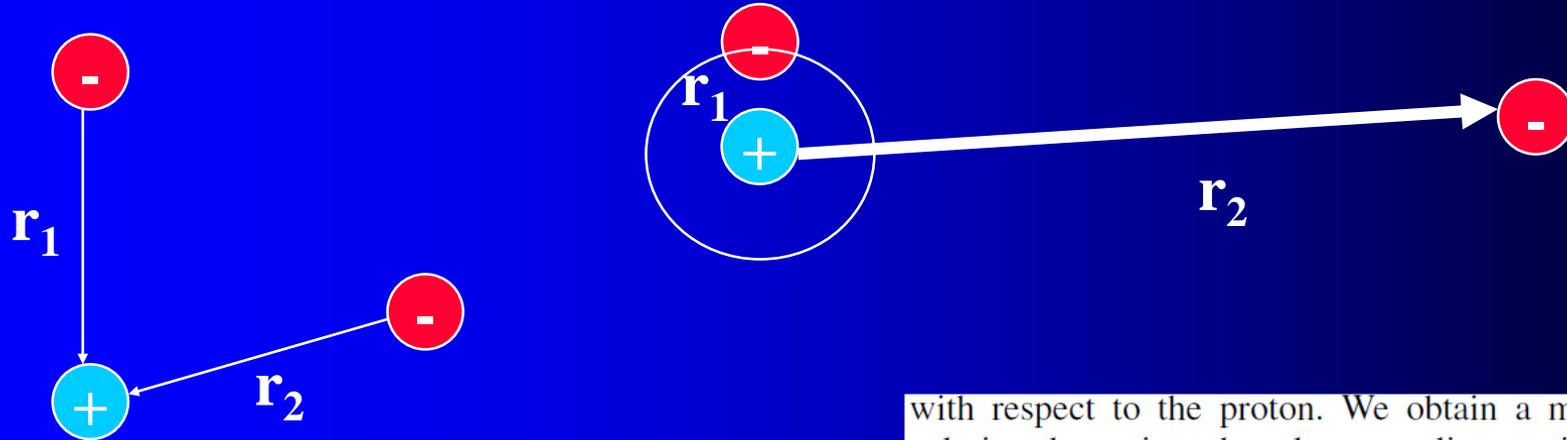


Anti hydrogen formation

Three-Body Recombination of Atomic Ions with Slow Electrons

S. X. Hu

Laboratory for Laser Energetics, University of Rochester, 250 East River Road, Rochester, New York 14623, USA



We consider the simplest TBR in the case of hydrogen formation, in which two free electrons interact with a proton. To investigate the three-body interaction dynamics, we numerically solve the six-dimensional (6D) time-dependent Schrödinger equation, which has the following form (atomic units are used throughout):

$$i \frac{\partial}{\partial t} \Phi(\mathbf{r}_1, \mathbf{r}_2, t) = \left[ -\frac{1}{2} (\Delta_{\mathbf{r}_1} + \Delta_{\mathbf{r}_2}) - \frac{1}{r_1} - \frac{1}{r_2} + \frac{1}{|\mathbf{r}_1 - \mathbf{r}_2|} \right] \Phi(\mathbf{r}_1, \mathbf{r}_2, t), \quad (1)$$

where  $\mathbf{r}_1$  and  $\mathbf{r}_2$  are the position vectors of each electron, with respect to the proton. We obtain a more tractable

solution by using the close-coupling recipe [12]: expanding the 6D wave function  $\Phi(\mathbf{r}_1, \mathbf{r}_2|t)$  in terms of bipolar spherical harmonics  $Y_{l_1 l_2}^{LS}(\Omega_1, \Omega_2)$ ,  $\Phi(\mathbf{r}_1, \mathbf{r}_2|t) = \sum_{LS} \sum_{l_1 l_2} [\Psi_{l_1 l_2}^{(LS)}(r_1, r_2|t)/r_1 r_2] Y_{l_1 l_2}^{LS}(\Omega_1, \Omega_2)$ , for a specific symmetry ( $LS$ ). We can also expand the Coulomb repulsion term  $1/|\mathbf{r}_1 - \mathbf{r}_2|$  in terms of spherical harmonics. Substituting these expansions into the above Schrödinger Eq. (1) and integrating over the angles  $\Omega_1$  and  $\Omega_2$  yields a set of coupled partial differential equations with only two radial variables  $r_1$  and  $r_2$  left:

$$i \frac{\partial}{\partial t} \Psi_j(r_1, r_2|t) = [\hat{T}_1 + \hat{T}_2 + \hat{V}_c] \Psi_j(r_1, r_2|t) + \sum_k \hat{V}_{j,k}^I(r_1, r_2|t) \Psi_k(r_1, r_2|t), \quad (2)$$

where the partial-wave index  $j$  runs from 1 to the total number  $N$  of partial waves used for expansion. In Eq. (2),

# Kvantovka na každý deň

$$i\frac{\partial}{\partial t}\Psi_j(r_1, r_2|t) = [\hat{T}_1 + \hat{T}_2 + \hat{V}_c]\Psi_j(r_1, r_2|t) + \sum_k \hat{V}_{j,k}^I(r_1, r_2|t)\Psi_k(r_1, r_2|t), \quad (2)$$



$$P_{nl}(E_2) = 2 \sum_{LS} \sum_{l_2} \left| \int dr_1 \int dr_2 \phi_{nl}^*(r_1) \phi_{k_2 l_2}^*(r_2) \Psi_{ll_2}^{(LS)}(r_1, r_2, t = t_f) \right|^2,$$

$K_E = 0.1 \text{ eV}$

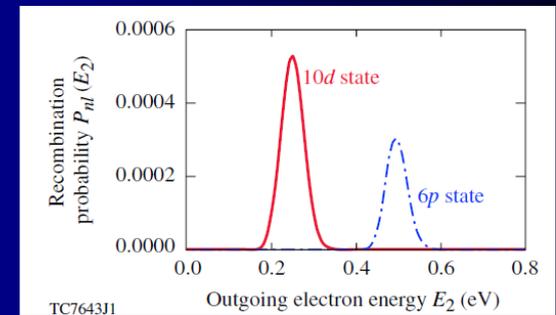
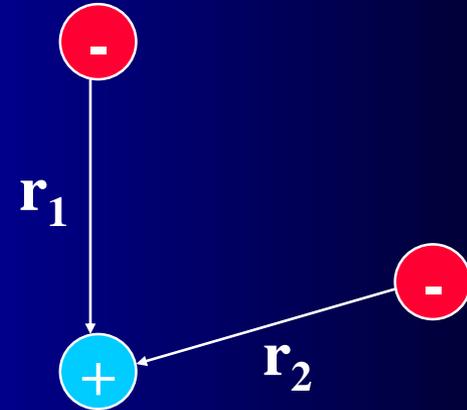
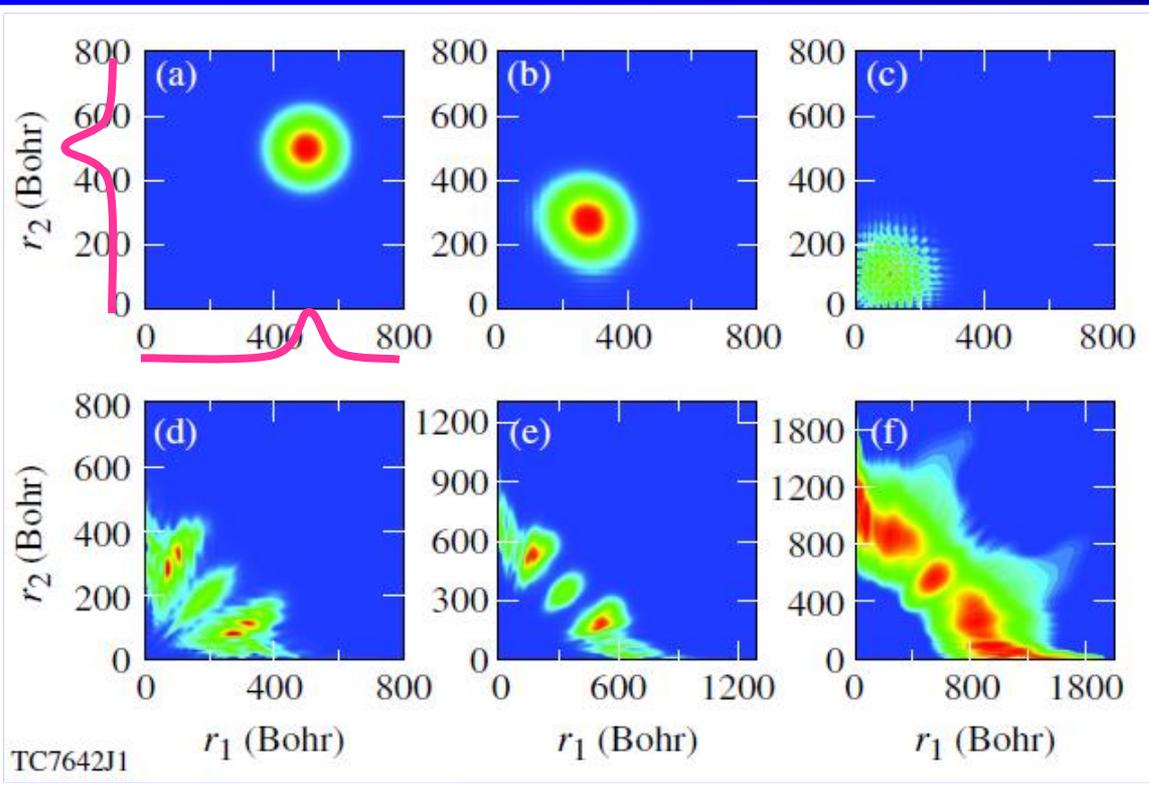


FIG. 1 (color online). Snapshots of electron probability distribution on the plane spanned by the radial coordinates  $r_1$  and  $r_2$  for different times: (a)  $t = 0.0 \text{ fs}$ , (b)  $t = 60 \text{ fs}$ , (c)  $t = 100 \text{ fs}$ , (d)  $t = 150 \text{ fs}$ , (e)  $t = 194 \text{ fs}$ , and (f) (in log scale)  $t = 260 \text{ fs}$ .

Thus, for the case of  $K_E = 0.1 \text{ eV}$  considered in Figs. 1 and 2, the total system energy is about  $E_{\text{tot}} \sim 0.12 \text{ eV}$  instead of  $2K_E$ . Hence, when one electron recombines to the  $10d$  state ( $|E_{10d}| \approx 0.136 \text{ eV}$ ) of the H atom, the outgoing electron takes an initial total energy of  $0.12 \text{ eV}$  plus  $|E_{10d}|$ , thereby  $P_{10d}(E_2)$  peaks at  $E_2 \sim 0.256 \text{ eV}$ , as shown by the red solid line of Fig. 2. Similar energy conservation is also well satisfied for the recombination to the  $6p$  state, as is illustrated by the blue dash-dotted line in Fig. 2. Our quantum calculations unambiguously reveal the essential feature of a TBR process.

Kvantovka na každý deň



$K_E = 0.1 \text{ eV}$

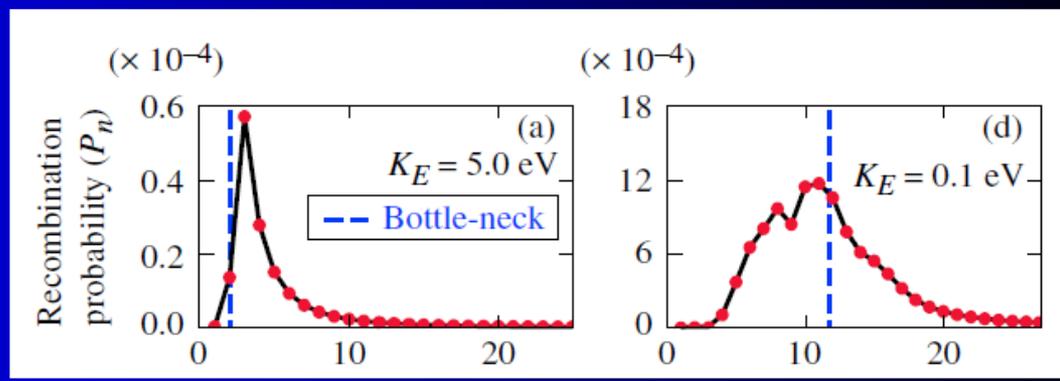


FIG. 3 (color online). The recombination probability  $P_n$  as a function of the energy level  $n$ , for different electron kinetic energies  $K_E$  marked in each panel.

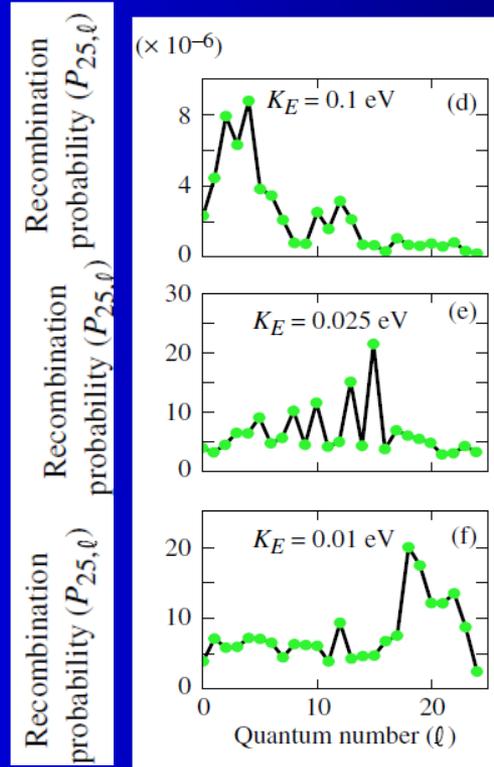
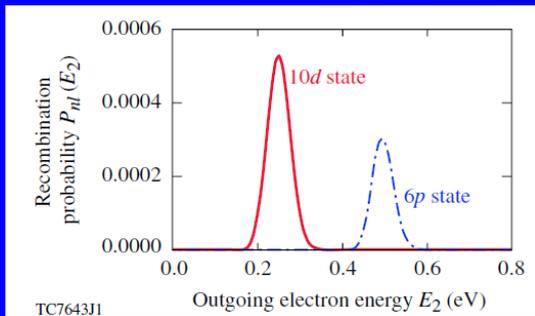
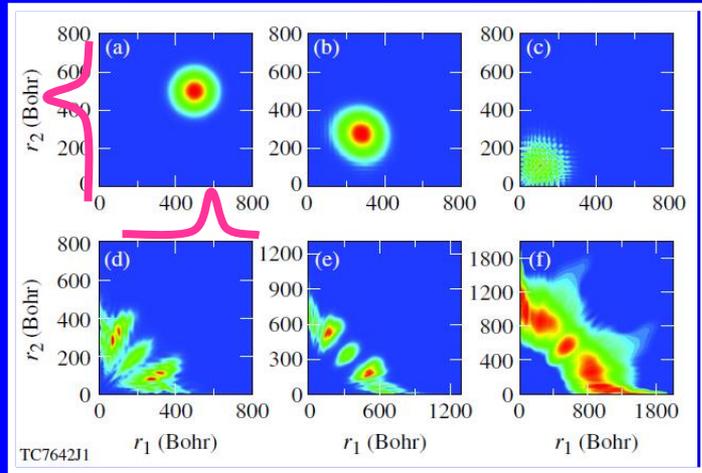


FIG. 4 (color online). The recombination probability  $P_{n=25,l}$  as a function of the angular-momentum quantum number  $l$ , for different electron kinetic energies  $K_E$  marked in each panel.

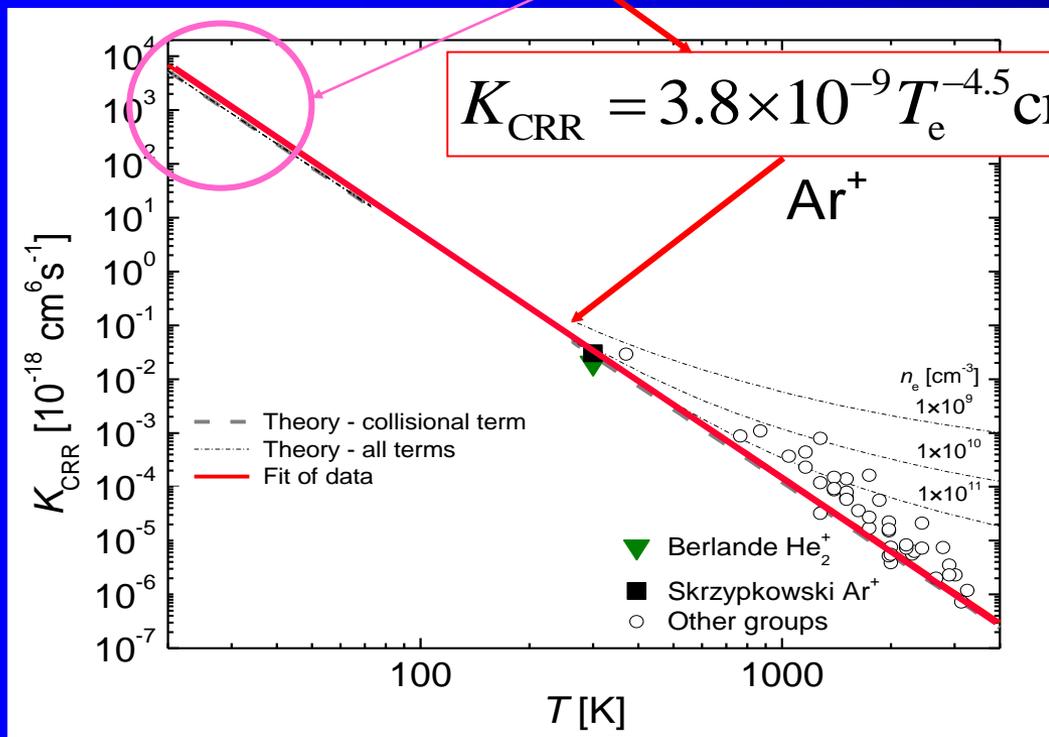


$$\frac{dn_e}{dt} = -K_{CRR} [\text{Ar}^+] n_e^2 - \frac{n_e}{\tau_D} = -K_{CRR} n_e^3 - \frac{n_e}{\tau_D}$$

$$\alpha_{CRR} = 3.8 \times 10^{-9} T_e^{-4.5} n_e + 1.55 \times 10^{-10} T_e^{-0.63} + 6 \times 10^{-9} T_e^{-2.18} n_e^{0.37} \text{ cm}^3 \text{ s}^{-1}$$



Anti hydrogen formation

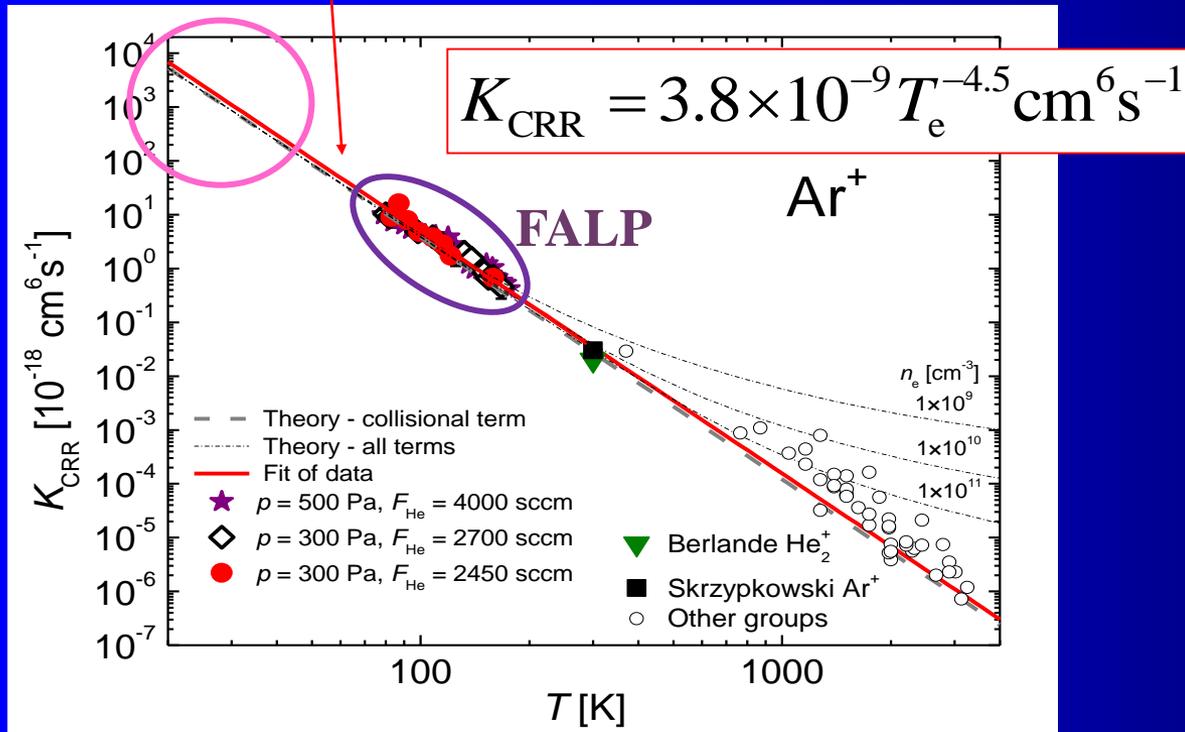


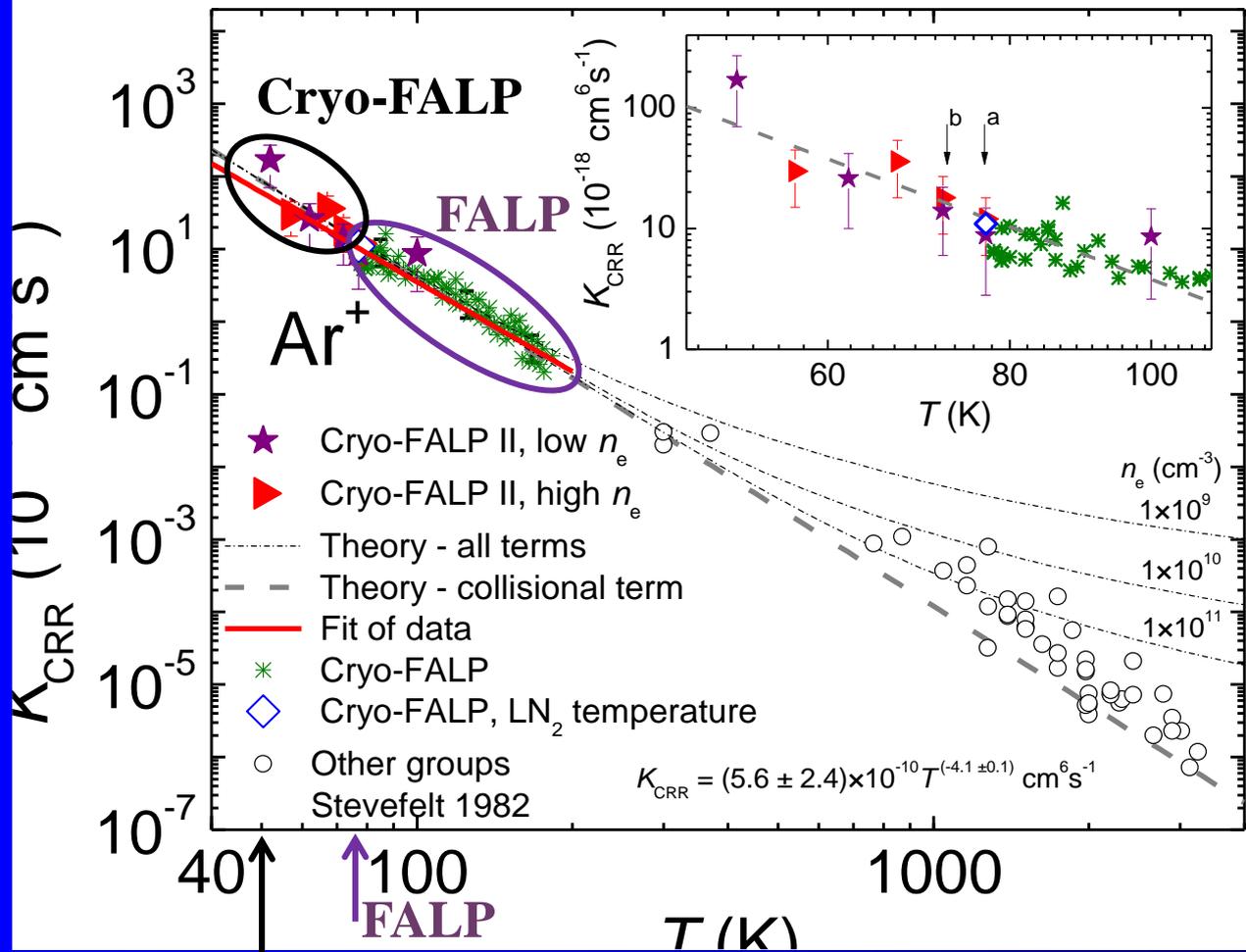
$$\alpha_{CRR} = K_{CRR} n_e$$

# Ar<sup>+</sup> + e<sup>-</sup> + e<sup>-</sup>

$$\frac{dn_e}{dt} = -K_{CRR} [Ar^+] n_e^2 - \frac{n_e}{\tau_D} = -K_{CRR} n_e^3 - \frac{n_e}{\tau_D}$$

$$\alpha_{CRR} = 3.8 \times 10^{-9} T_e^{-4.5} n_e + 1.55 \times 10^{-10} T_e^{-0.63} + 6 \times 10^{-9} T_e^{-2.18} n_e^{0.37} \text{ cm}^3 \text{ s}^{-1}$$

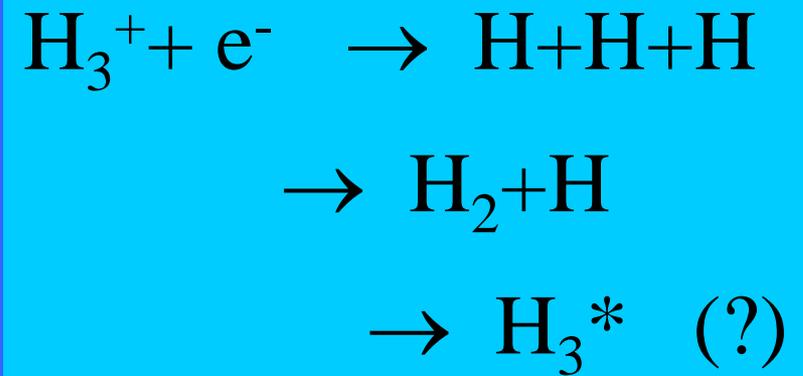
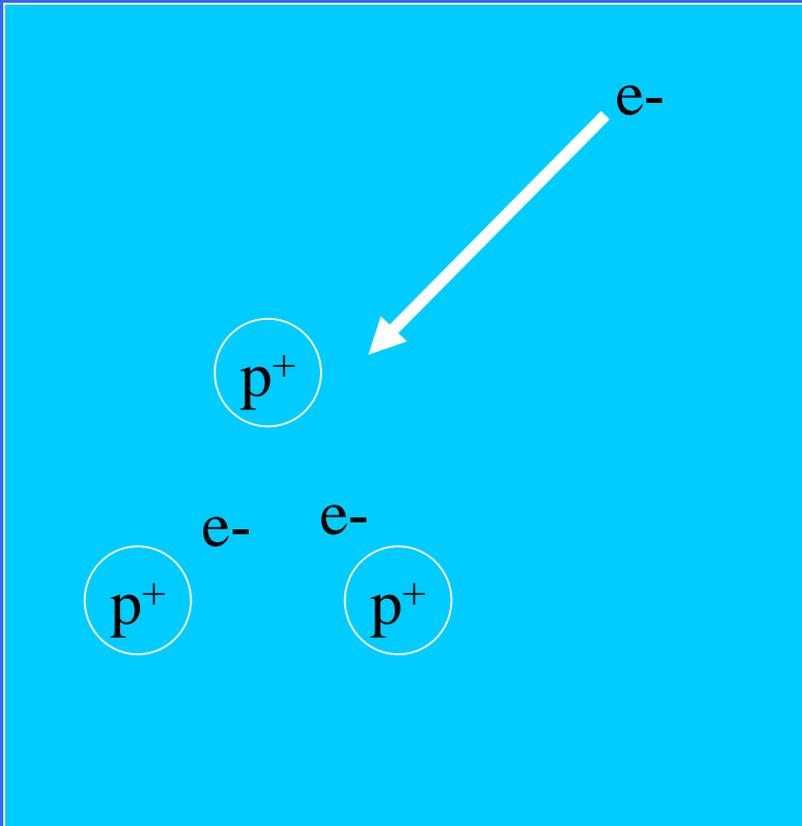




**Cryo-FALP**



# Recombination of $H_3^+$



# Tunneling dissociative recombination

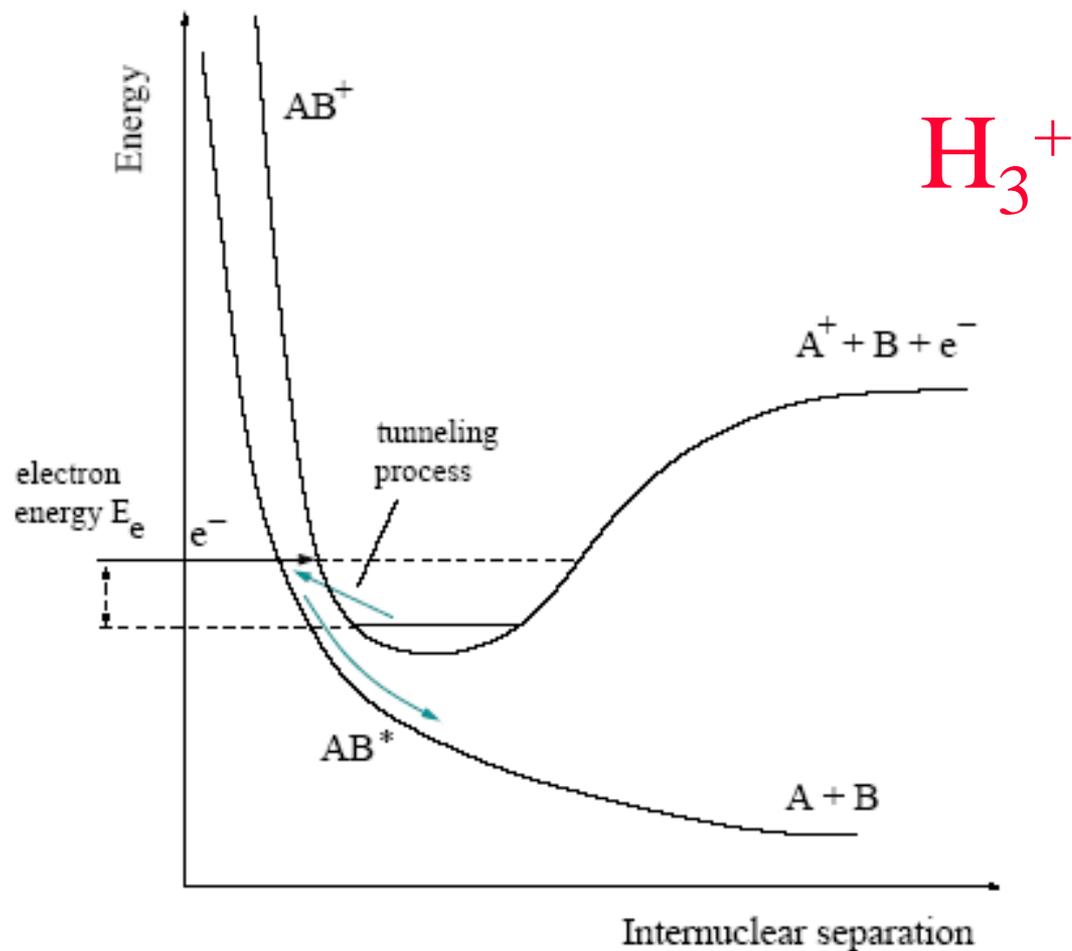


Figure 4.3: Sketch of tunneling mode dissociative recombination.

# Tunneling dissociative recombination

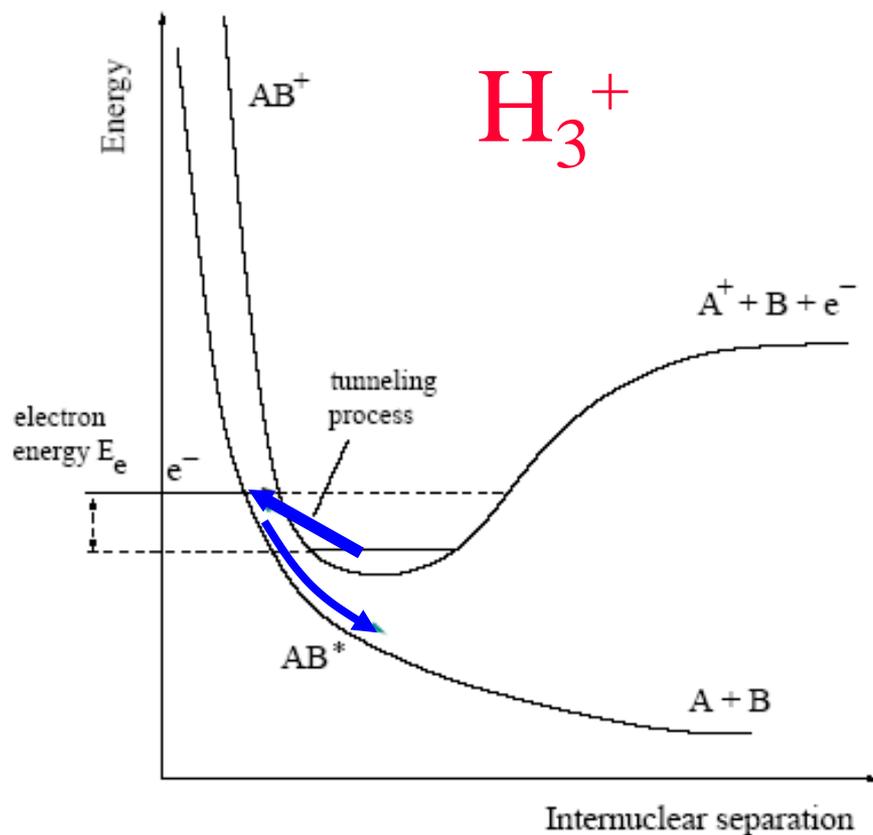
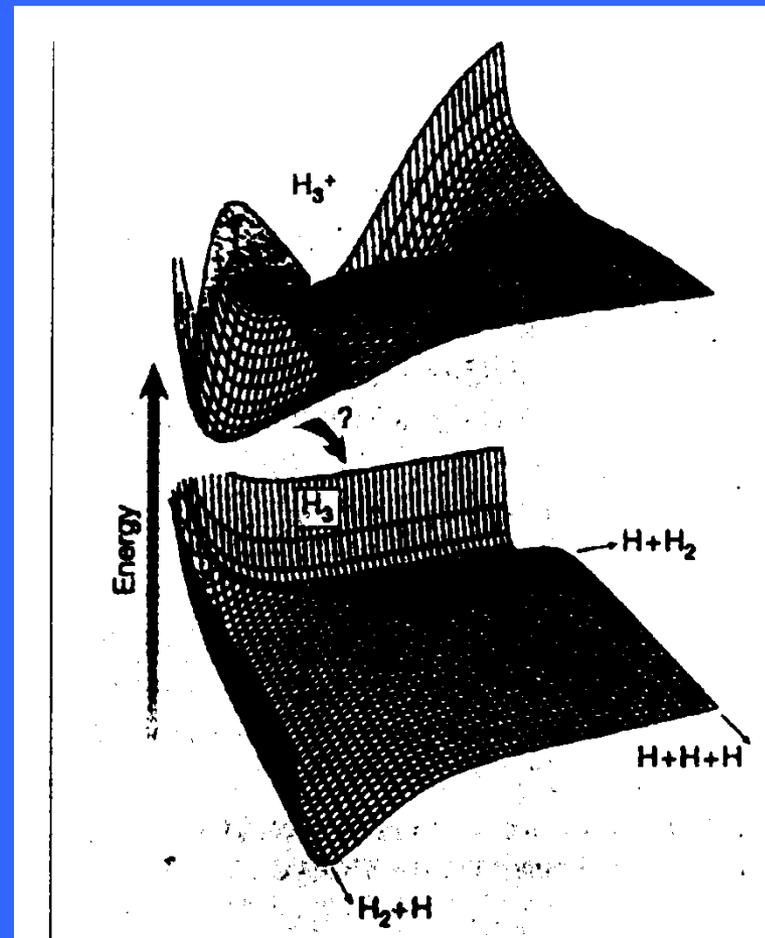
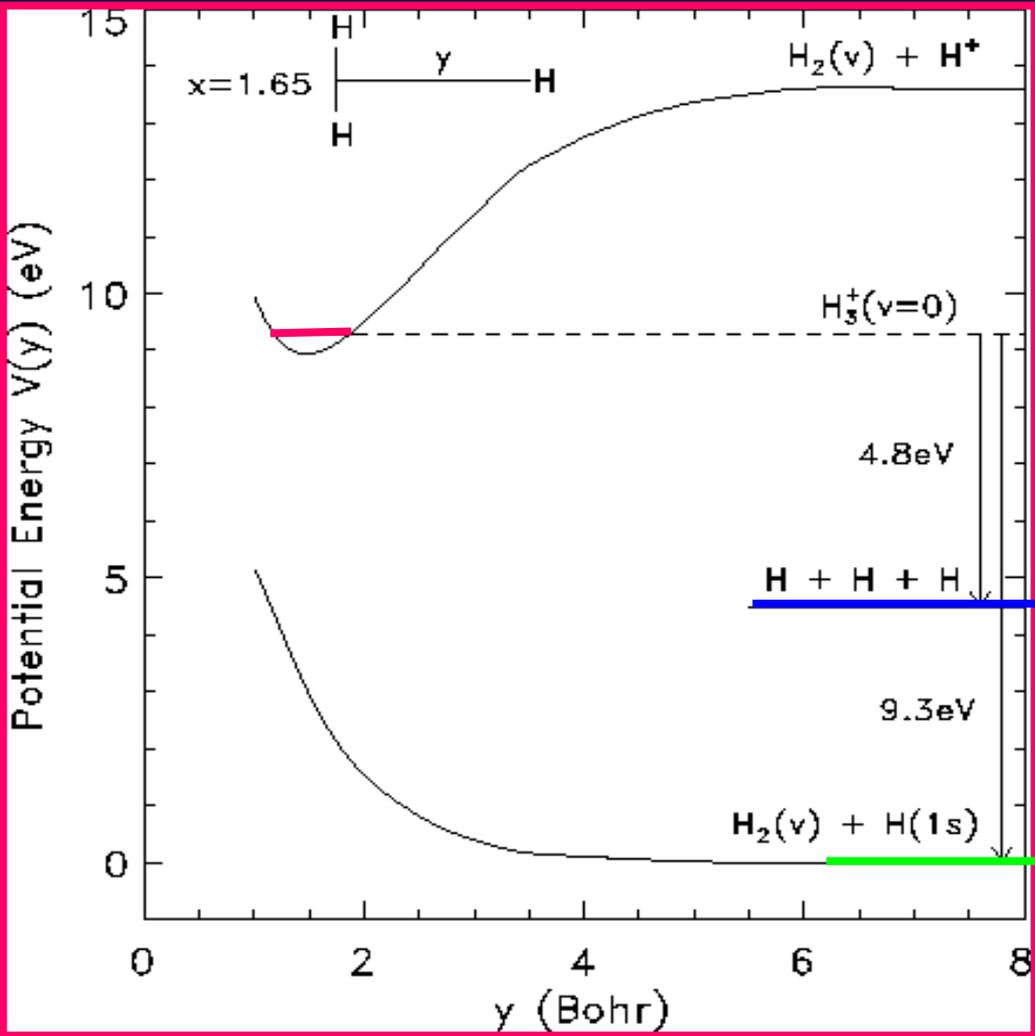


Figure 4.3: Sketch of tunneling mode dissociative recombination.



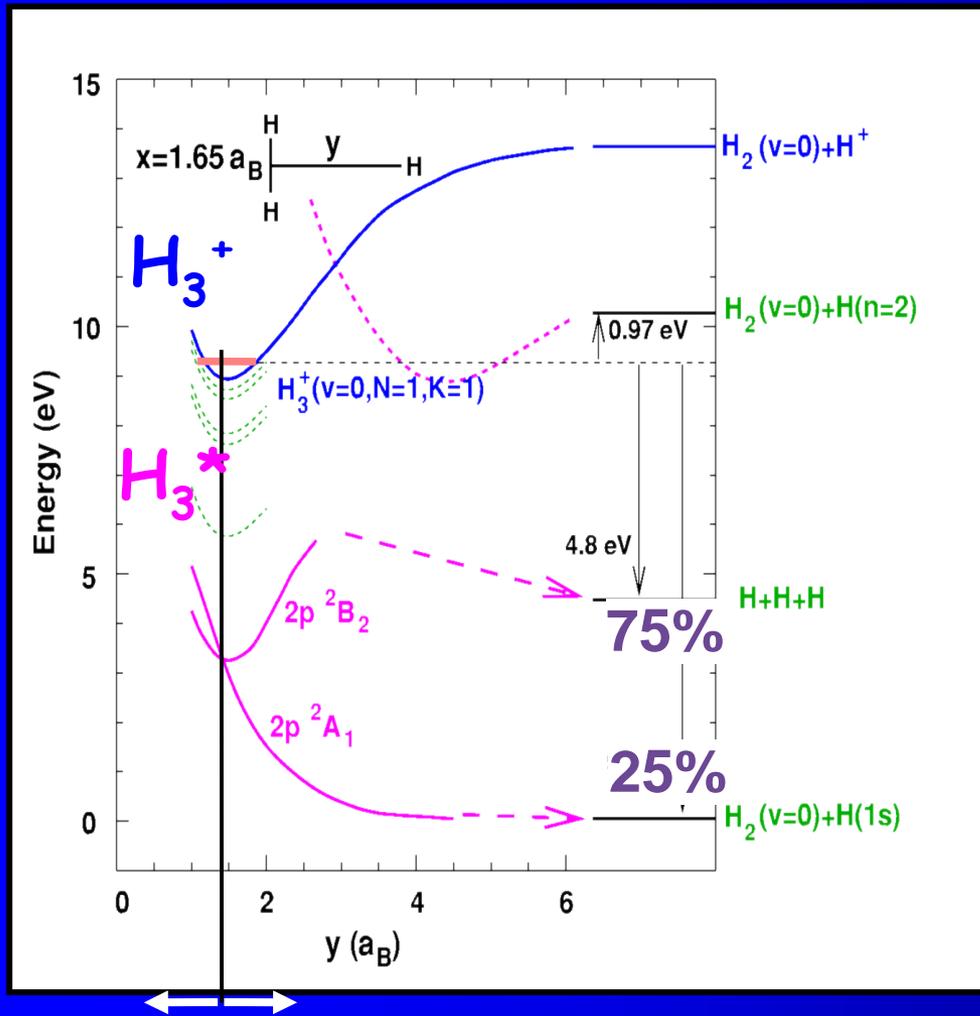
Dissociative recombination of  $H_3^+$ .  
Relevant potential curves



3-body decay

2-body decay

# Dissociative recombination of $H_3^+$



Remote curve crossing

Electron capture via Jahn-Teller coupling of electronic and ro-vibrational motion

Symmetric deformation

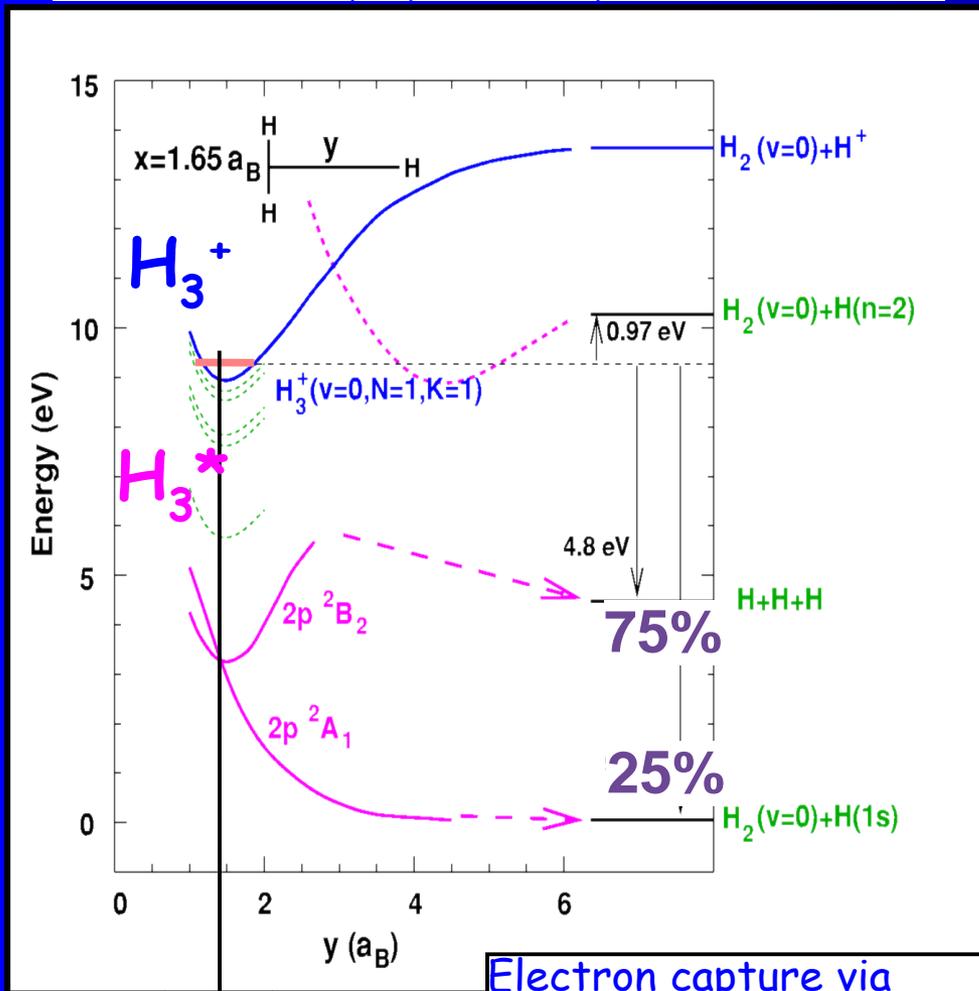


Prototype system for electron capture and dissociation mechanisms in polyatomic species

# Three atomic ions

# Dissociative recombination of $H_3^+$

Prototype system for electron capture and dissociation mechanisms in polyatomic species



Electron capture via Jahn-Teller coupling of electronic and ro-vibrational motion

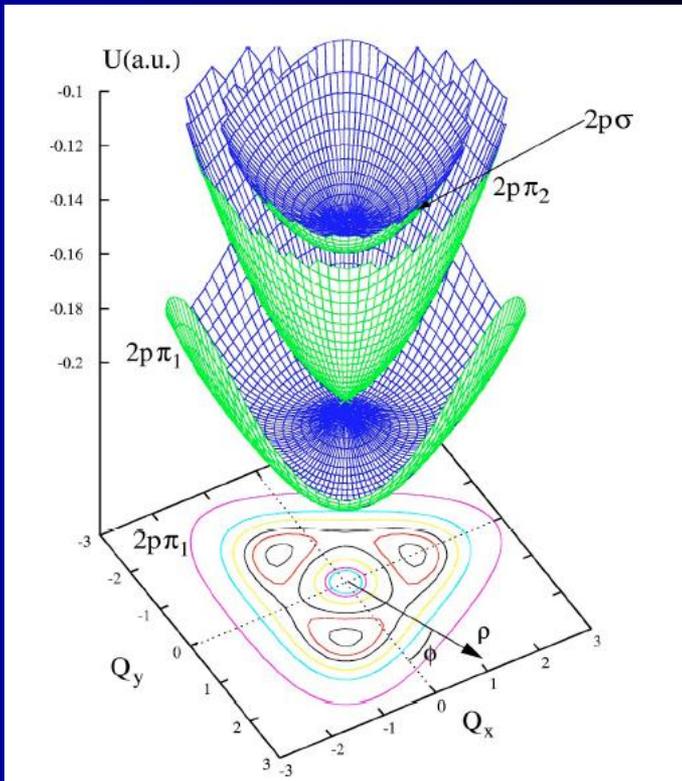


FIG. 4. The figure demonstrates how the Jahn-Teller effect produces a high rate of dissociative recombination. One  $2p\sigma$  potential surface and two  $2p\pi$  potential surfaces [47] of the neutral molecule are shown. The conical intersection is produced by Jahn-Teller coupling. When an electron arrives, it scatters first into a low-lying vibrationally excited Rydberg state  $\{01^1\}$ . Then, after the nuclei vibrate, the system finds its way with high probability into a  $2p\pi$  state having high vibrational excitation, near the point of conical intersection. The contour plot at the bottom of the figure represents the lowest  $2p\pi_1$  surface. All three potential surfaces are shown in the reduced 2D space of dimensionless normal coordinates. The coordinates used here are the normal asymmetric  $Q_x$ ,  $Q_y$  coordinate, with  $\rho$  and  $\phi$  their polar components [17,18]. The third vibrational coordinate—the symmetric stretch coordinate  $Q_1$ —is kept constant for this graph.

Symmetric deformation



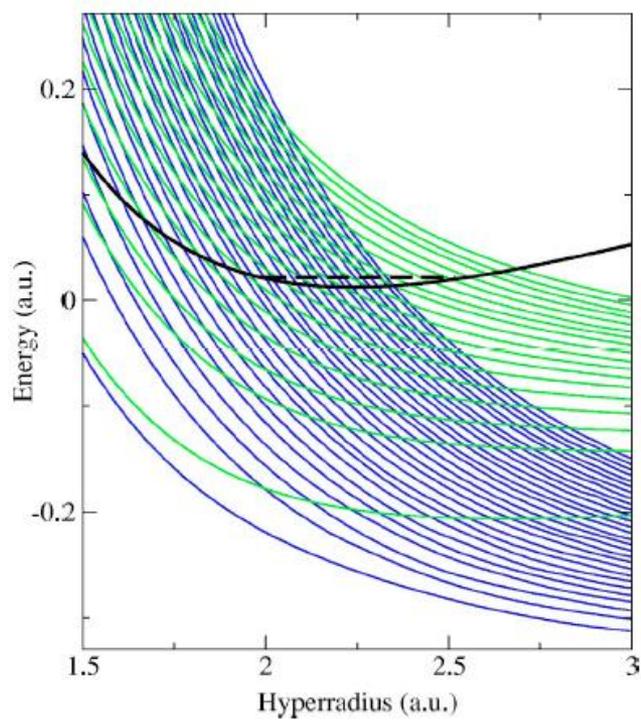


FIG. 1. The problem of DR of  $\text{H}_3^+$  in the hyperspherical adiabatic approximation. The lowest hyperspherical adiabatic potential (thick full line) of the  $\text{H}_3^+$  and number of hyperspherical adiabatic potentials of the neutral molecule (thin lines). Lower family of lines (darker lines) dissociate to the  $\text{H}_2 + \text{H}$  channel; the upper family (lighter lines) dissociate to the  $\text{H} + \text{H} + \text{H}$  channel. To calculate hyperspherical adiabatic curves we used the three-dimensional  $\text{H}_3^+$  potential from Ref. [48] and the  $\text{H}_3$  potential from Refs. [35–37]. Since the density of hyperspherical states is high, only every tenth  $\text{H}_3$  potential curve is shown in the figure. The dashed line shows the position of the ground vibrational level of the ion, which is the only one populated in the relevant experiments.

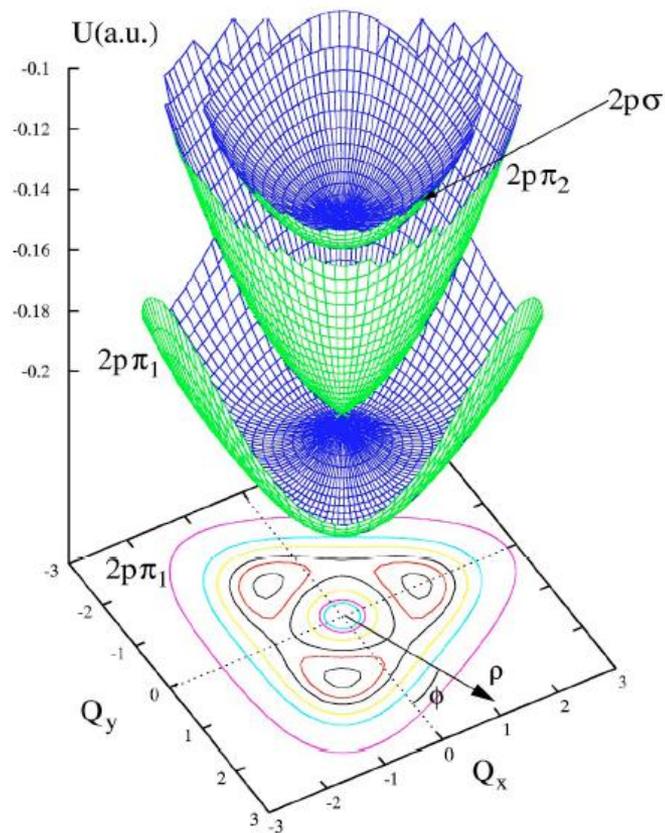


FIG. 4. The figure demonstrates how the Jahn-Teller effect produces a high rate of dissociative recombination. One  $2p\sigma$  potential surface and two  $2p\pi$  potential surfaces [47] of the neutral molecule are shown. The conical intersection is produced by Jahn-Teller coupling. When an electron arrives, it scatters first into a low-lying vibrationally excited Rydberg state  $\{01^1\}$ . Then, after the nuclei vibrate, the system finds its way with high probability into a  $2p\pi$  state having high vibrational excitation, near the point of conical intersection. The contour plot at the bottom of the figure represents the lowest  $2p\pi_1$  surface. All three potential surfaces are shown in the reduced 2D space of dimensionless normal coordinates. The coordinates used here are the normal asymmetric  $Q_x$ ,  $Q_y$  coordinate, with  $\rho$  and  $\phi$  their polar components [17,18]. The third vibrational coordinate—the symmetric stretch coordinate  $Q_1$ —is kept constant for this graph.



Capture

Autoionization

$H_3^*$  resonant state(s)

predissociation

To get high recombination rate, we need

(a) efficient capture

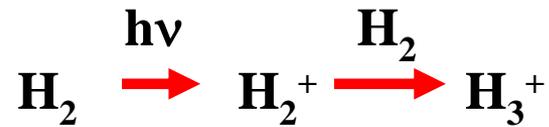
(b) predissociation faster than auto-ionization

## Dense Clouds



Barnard 68 (João Alves)

## Formation

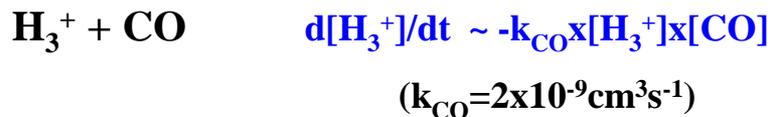


$$d[\text{H}_3^+]/dt \sim \gamma \cdot [\text{H}_2]$$

## Diffuse Clouds



Cygnus OB2 (POSS)

a) DENSE CLOUDS:

$$[\text{H}_3^+] = \gamma / k_{\text{CO}} \cdot [\text{H}_2] / [\text{CO}] = \underline{\sim 1 \times 10^{-4} \text{cm}^{-3}}$$

~OK with observation

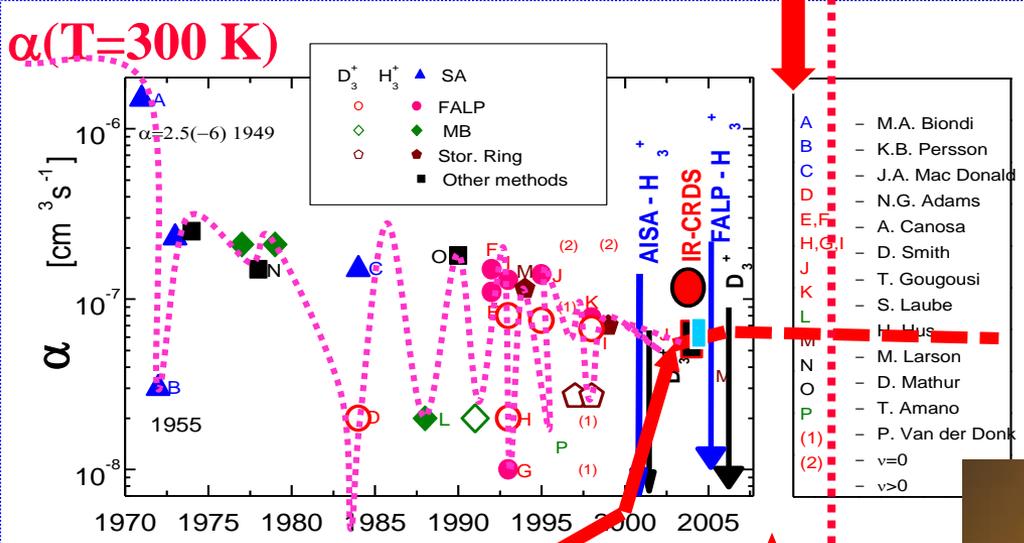
b) DIFFUSE CLOUDS:

$$\alpha_{\text{DR}} = 2 \times 10^{-7} \text{cm}^3 \text{s}^{-1} \times (T/300)^{-0.65} \quad (\text{the value from 2005})$$

$$[\text{H}_3^+] = \gamma / \alpha_{\text{DR}} \cdot [\text{H}_2] / [\text{C}] = \underline{\sim 1 \times 10^{-7} \text{cm}^{-3}}$$

~NO with observation

... history is repeating itself ....



**THEORY OF DR**

**Doubts 2011**

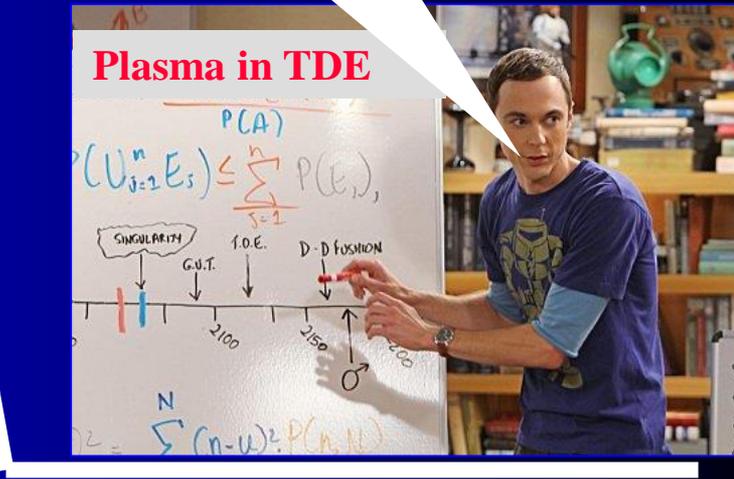
“Presently no rate coefficient measurement with a confirmed temperature below 300 K exists“.

Petrignani *et al.* Phys. Rev. A (2011)

*and ... history repeated itself.*

M. Larsson *et al.*, CP Letters (2008)

... One remaining problem is to understand the plasma afterglow experiments.



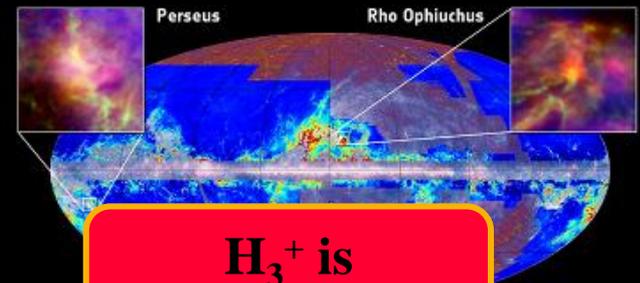
.... many times it was concluded, that the task was finished....



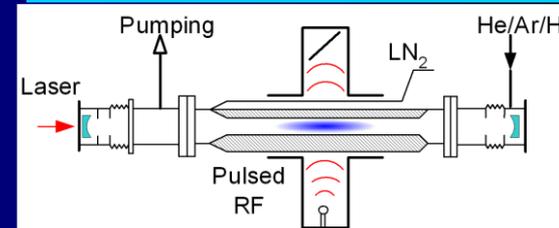
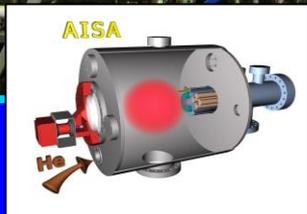
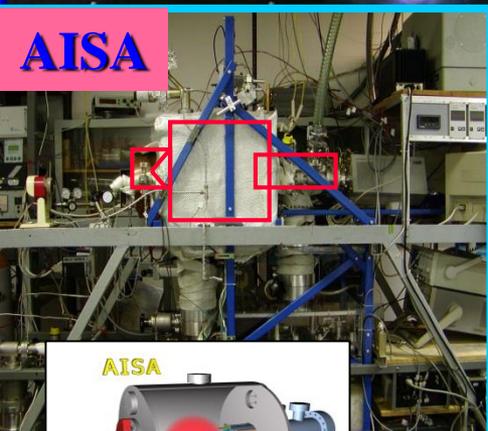
... and the caravan is on its way

The battle ship enters the stage

Πλασμα



$H_3^+$  is fundamental

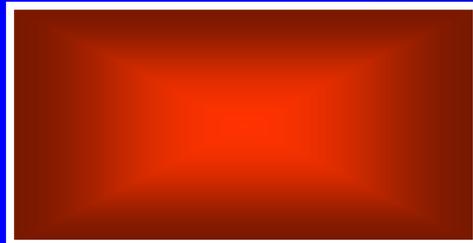
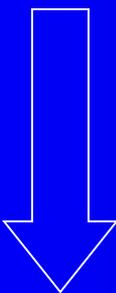


University Prag

Pressure dependence

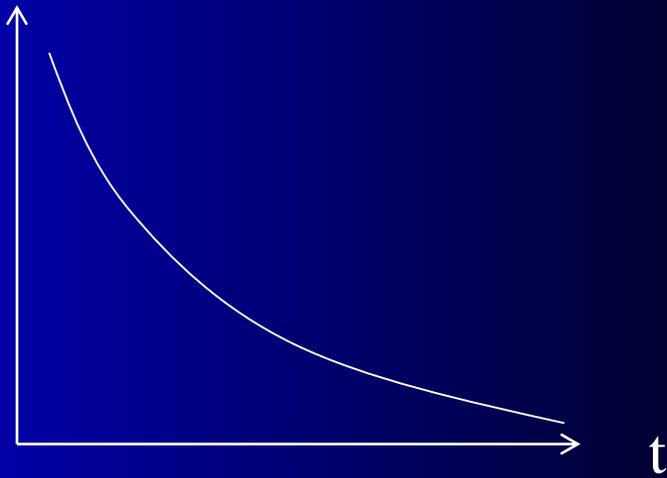
# Pulsed (stationary) afterglow

Discharge pulse  
microwave, UV, x-ray, e-beam



Plasma chamber  
He: ~ 1 –20 Torr  
Ar: 10 to 30 %  
+ molecules

Measure  $n_e(t)$



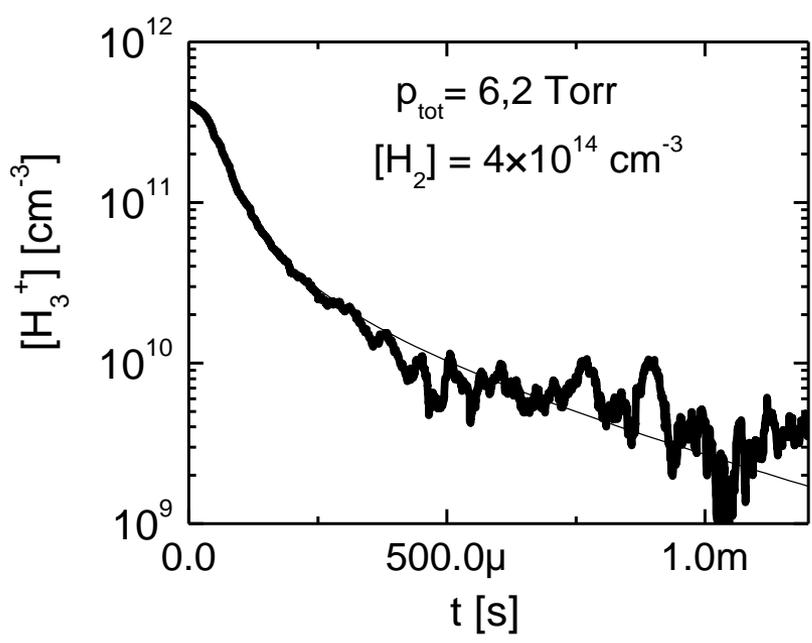
Get:

$$\frac{dn_e}{dt} = -\alpha n_e^2 + (\text{diffusion})$$

$$n_e(t) = \frac{n_{e0}}{1 + \alpha n_{e0} t}$$

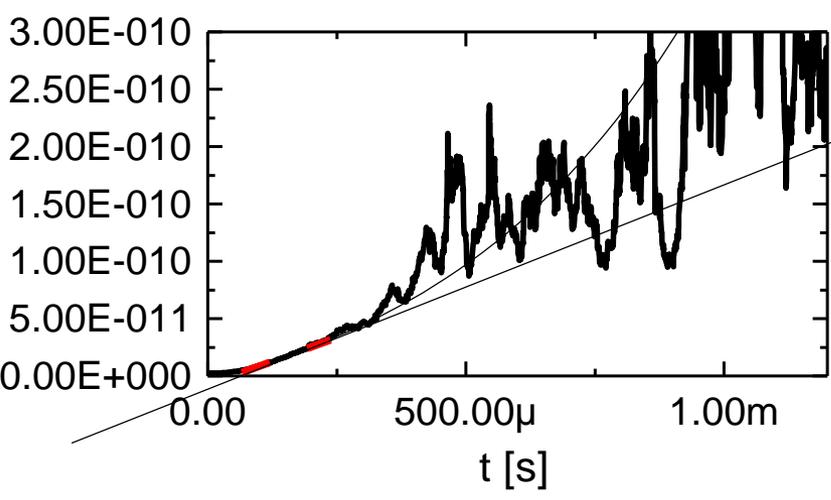
# We measure effective – apparent binary recombination rate coefficient

## Quasineutral $H_3^+$ dominated plasma

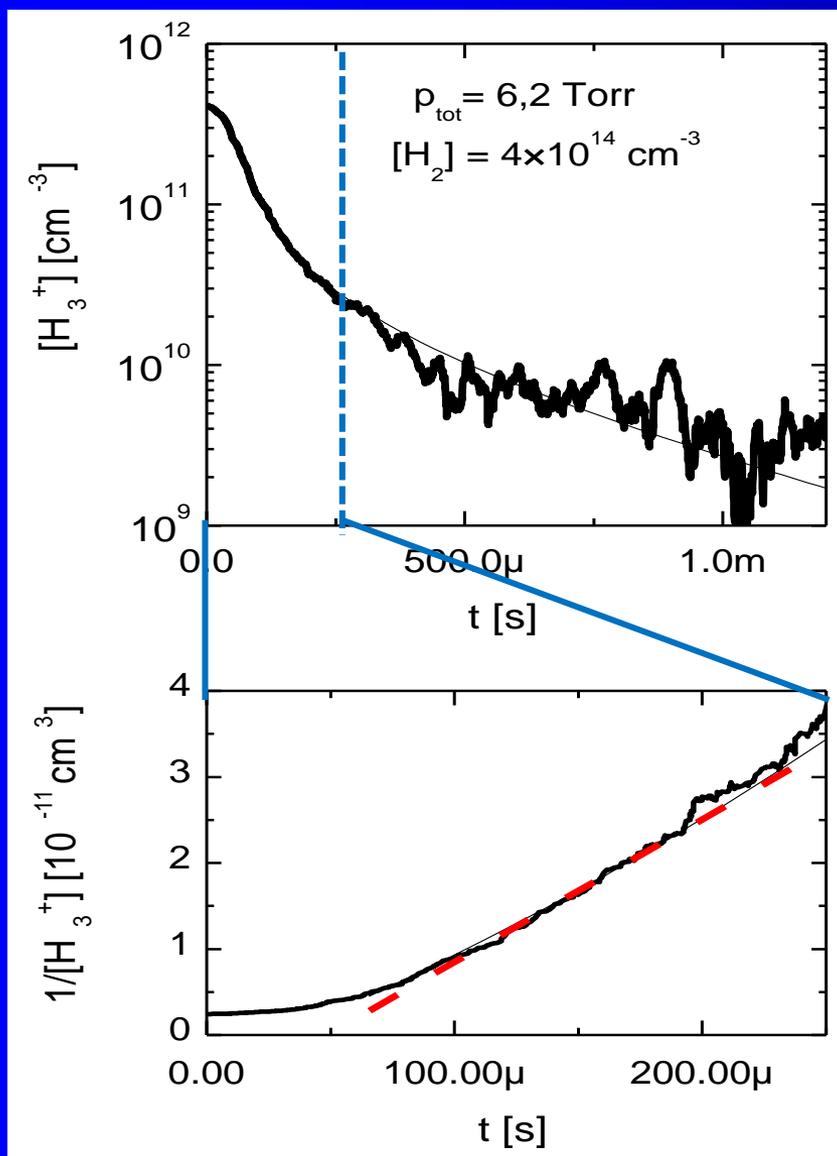


$$\frac{dn_e}{dt} = -\alpha_{\text{eff}} n_e^2 - \frac{n_e}{\tau_L}$$

$$\frac{1}{[H_3^+]} = \frac{1}{[H_3^+]_0} + \alpha t$$



# We measure effective – apparent binary recombination rate coefficient



## Quasineutral $H_3^+$ dominated plasma

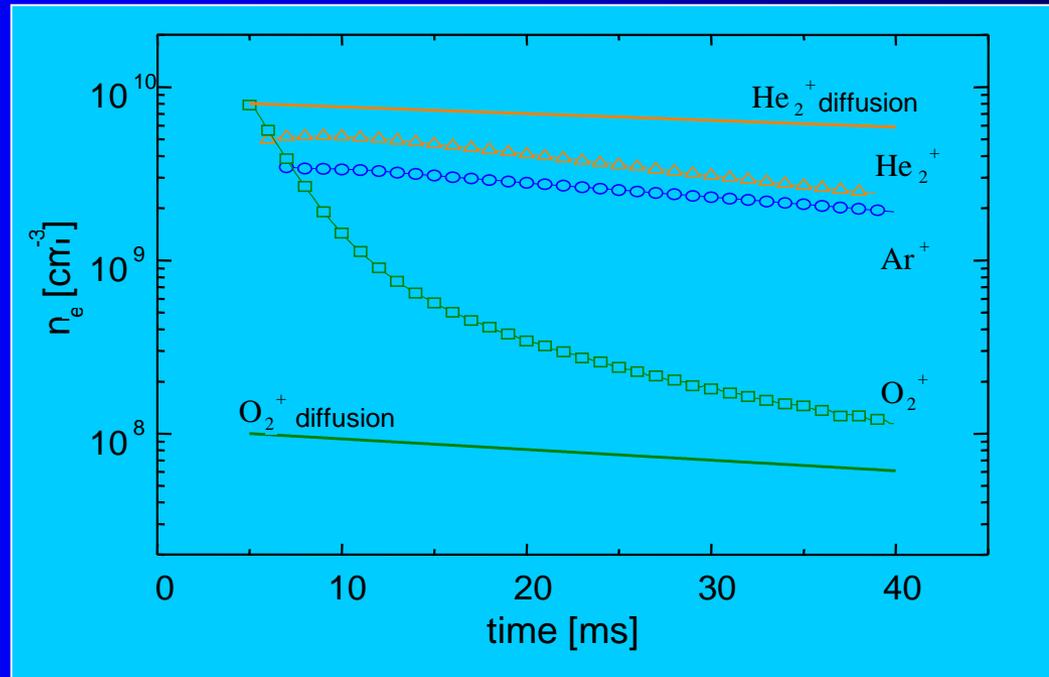
$$\frac{dn_e}{dt} = -\alpha_{\text{eff}} n_e^2 - \frac{n_e}{\tau_L}$$

$$\frac{1}{[H_3^+]} = \frac{1}{[H_3^+]_0} + \alpha t$$

# Decay in diffusion and recombination governed plasma

$$\frac{dn_e}{dt} = -\alpha n_e^2 - \frac{D_a}{\Lambda^2} n_e$$

$$\frac{1}{n_e} = \alpha \frac{\exp(\nu t) - 1}{\nu_D} + \frac{1}{n_0} \exp(\nu_D t)$$



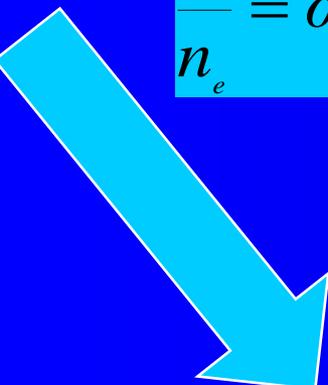
# Decay in diffusion and recombination governed plasma

$$\frac{dn_e}{dt} = -\alpha n_e^2 - \frac{D_a}{\Lambda^2} n_e$$

$$\frac{1}{n_e} = \alpha \frac{\exp(\nu t) - 1}{\nu_D} + \frac{1}{n_0} \exp(\nu_D t)$$

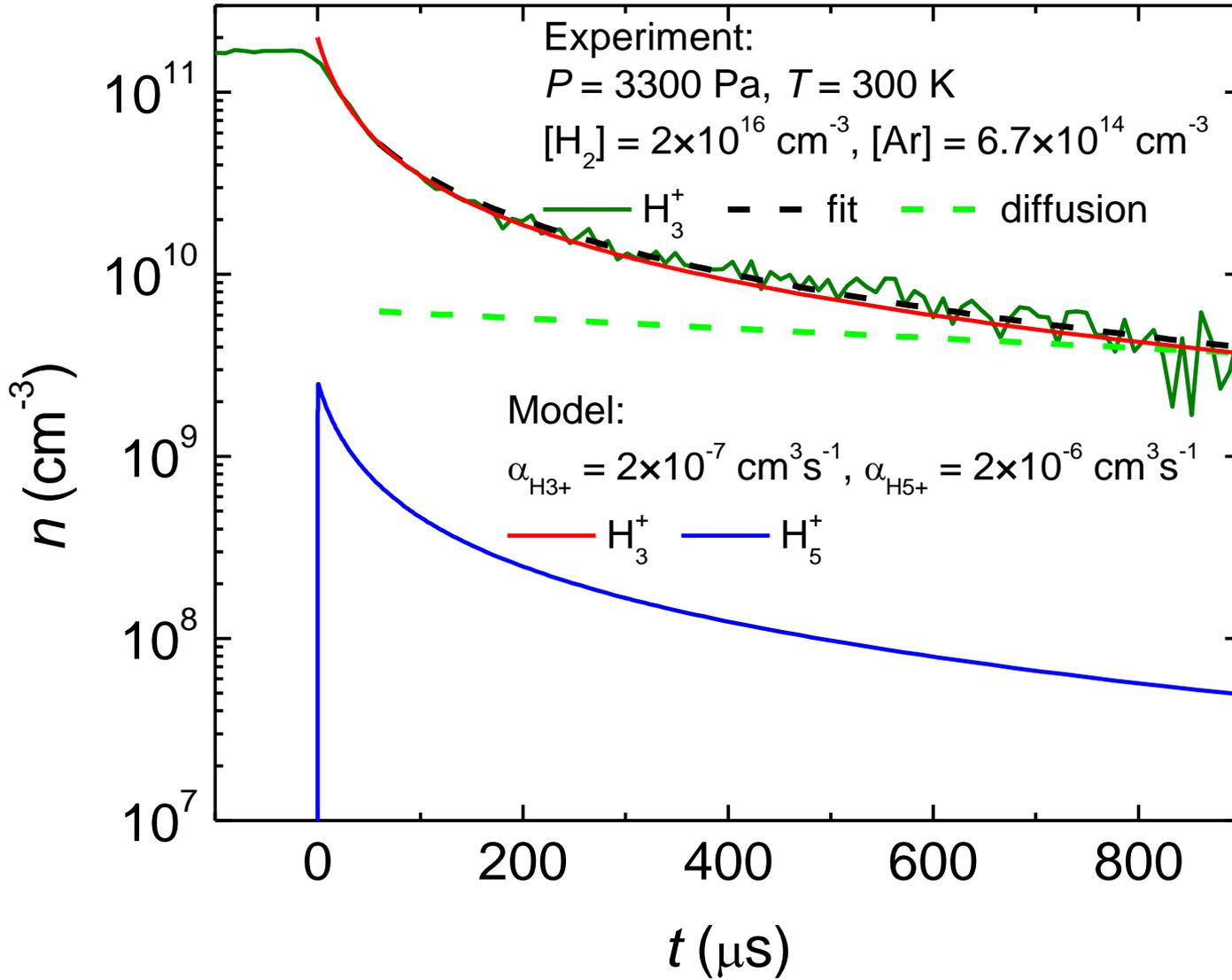
Limit for  $t \rightarrow 0$

$$\frac{1}{n_e} = \alpha \frac{(1 + \nu_D t) - 1}{\nu_D} + \frac{1}{n_0} (1 + \nu_D t)$$

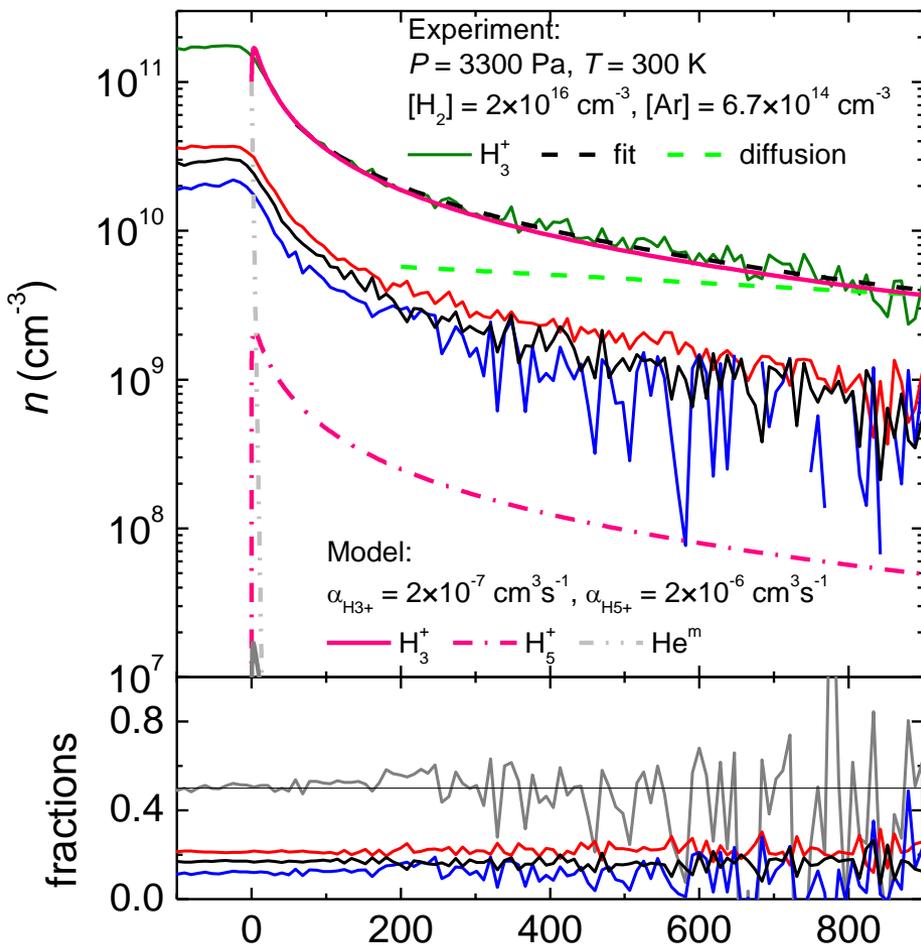

$$\frac{1}{n_e} = \alpha t + \frac{1}{n_0} \quad (1)$$

Limit for large  $t$

$$\frac{1}{n_e} = \left( \frac{\alpha}{\nu_D} + \frac{1}{n_0} \right) \exp(\nu_D t)$$



Srovnani modelu a experimentu. Pocatecni podminka:  $[\text{H}_3^+] = n_e = 2 \times 10^{11} \text{ cm}^{-3}$ .



$$\frac{dn_e}{dt} = -[\alpha_1 n_1(t) + \alpha_2 n_2(t)] n_e$$

$$\Rightarrow \alpha_{\text{eff}}(t) = [\alpha_1 f_1(t) + \alpha_2 f_2(t)]$$

$$f_1 + f_2 = 1$$

Model + data. Počatční podmínka:  $n_e = \text{He}^m = [\text{H}_3^+]$ .

Poznámka. Namerené  $\tau$  difuzních ztrát 1.6 ms. Teoretické  $\tau$  při daném tlaku je 1.8 ms (odpovídá cca  $4 \times 10^{10} \text{ cm}^{-3}$  koncentraci nečistot (při  $2 \times 10^{-9} \text{ cm}^3 \text{ s}^{-1}$  rychlosti reakce  $\text{H}_3^+$  s nečistotami). Namerená koncentrace vody  $[\text{H}_2\text{O}] = 5 \times 10^{10} \text{ cm}^{-3}$  ( $[\text{He}] = 8 \times 10^{17} \text{ cm}^{-3}$ ).

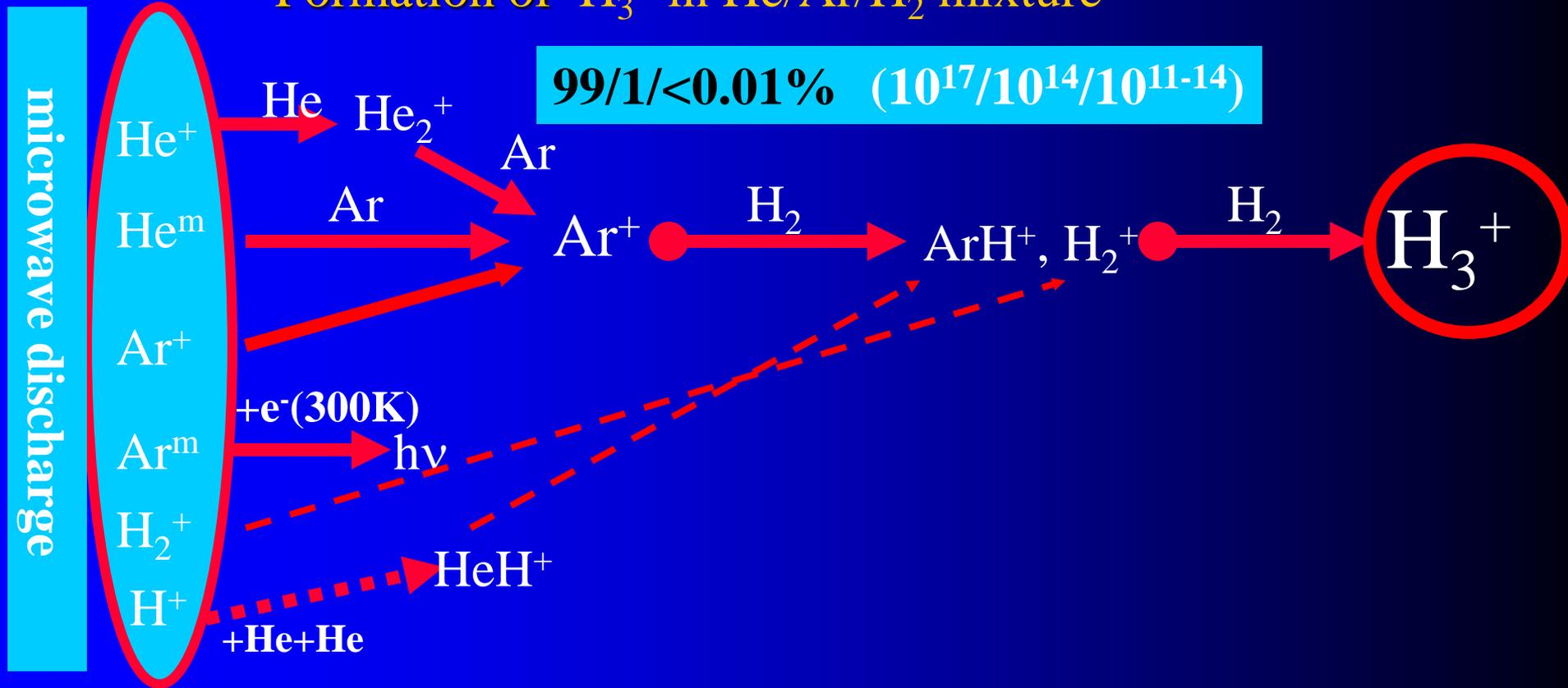
If there are 2 or more ion species, the fast recombining species disappears first

$$\frac{dn_e}{dt} = -[\alpha_1 n_1(t) + \alpha_2 n_2(t)] n_e$$

$$\Rightarrow \underline{\alpha_{eff}(t) = [\alpha_1 f_1(t) + \alpha_2 f_2(t)]}$$

$$f_1 + f_2 = 1$$

# Formation of $H_3^+$ in He/Ar/ $H_2$ mixture



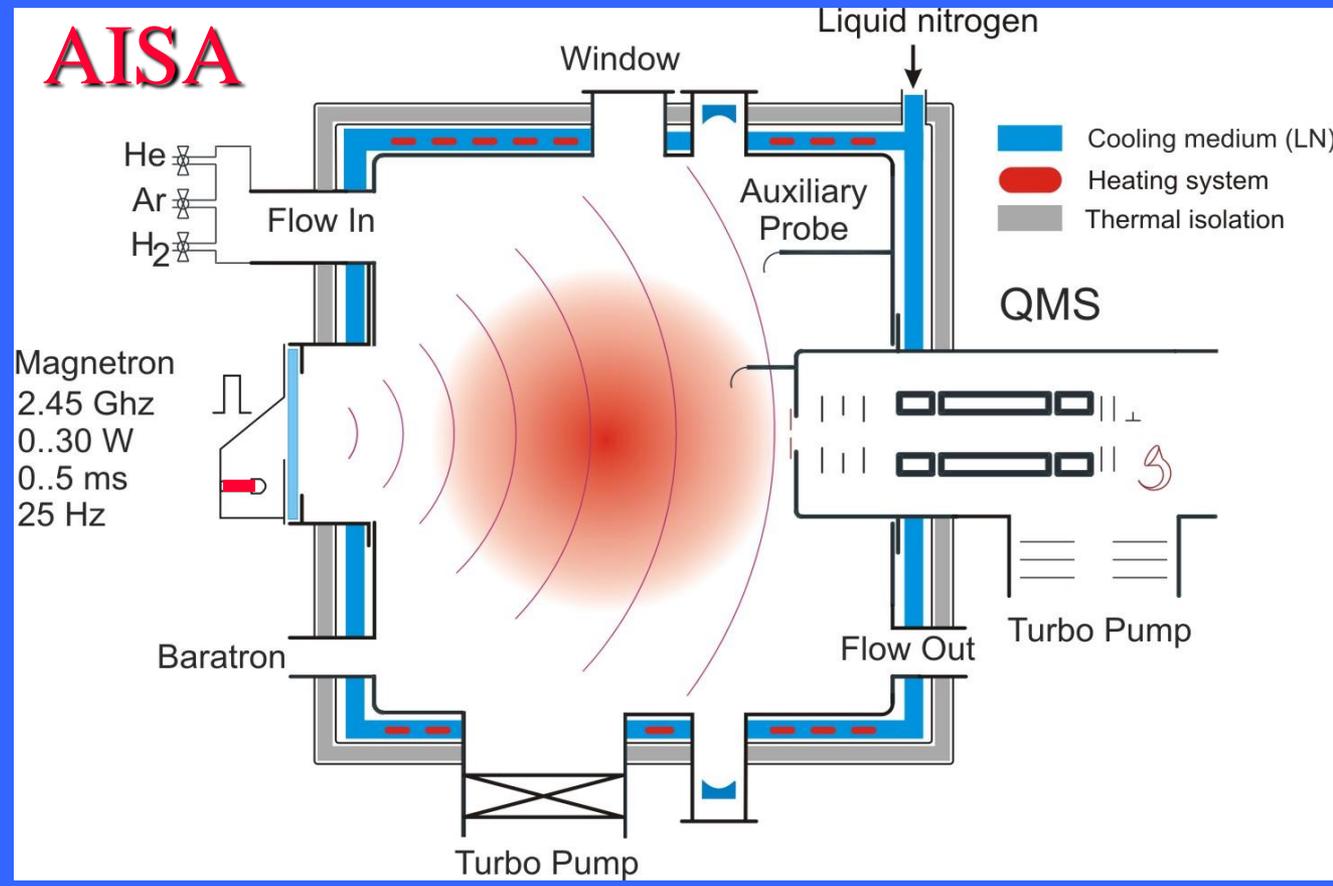
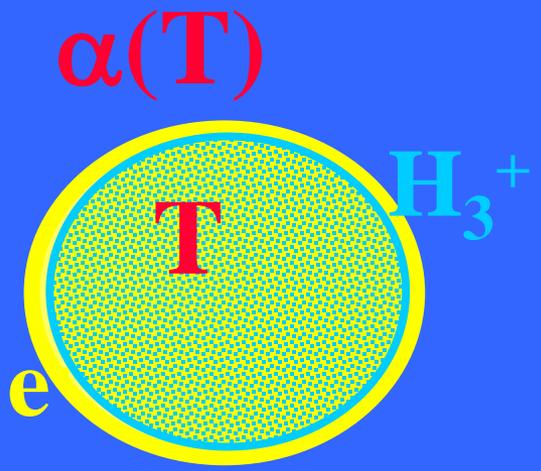
## FORMATION:

Ion molecule reactions during the early afterglow

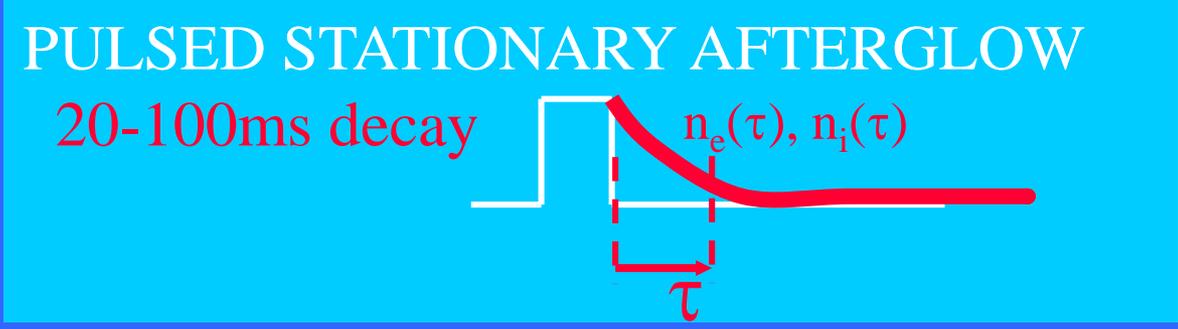
# VT - AISA

$$\frac{dn_i}{dt} = -\alpha n_i n_e$$

# He/Ar/H<sub>2</sub>



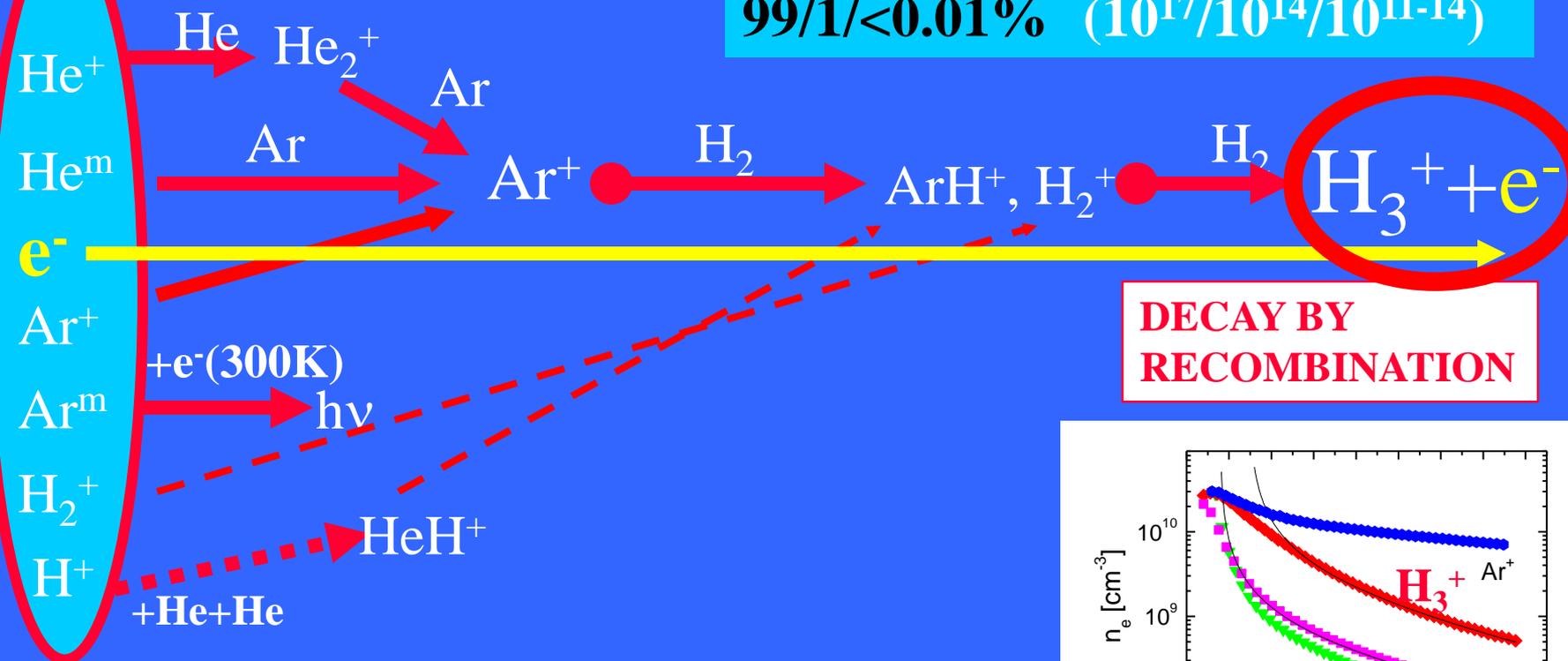
**40 cm diameter**  
**UHV - 10<sup>-9</sup> Torr**  
**External magnetron**  
**2 Torr of He/Ar/H<sub>2</sub>**



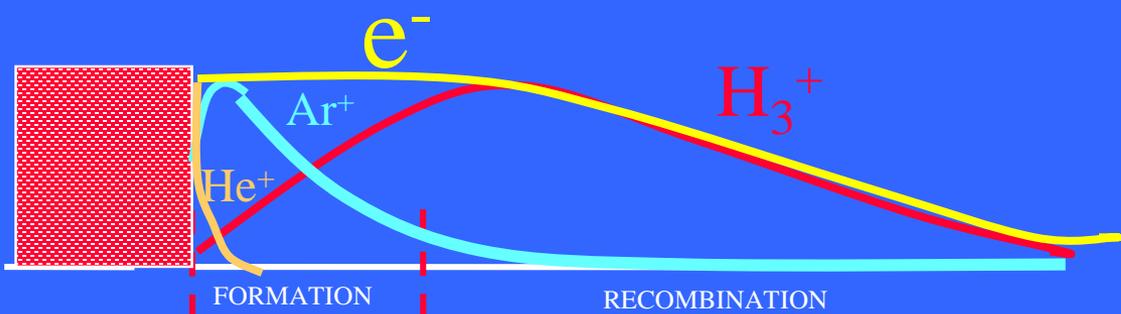
# Formation of $H_3^+$ in He/Ar/ $H_2$

99/1/<0.01% ( $10^{17}/10^{14}/10^{11-14}$ )

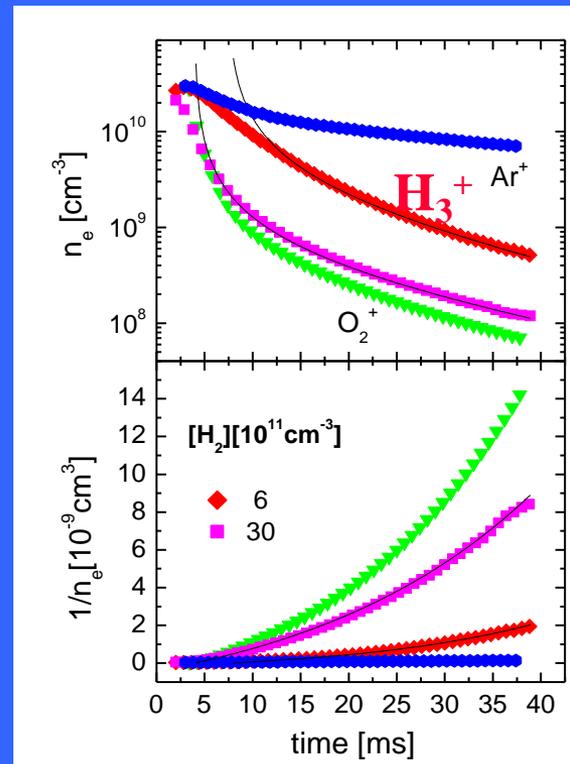
microwave discharge

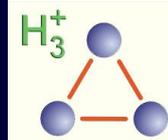


**DECAY BY RECOMBINATION**



Time resolved mass spectra



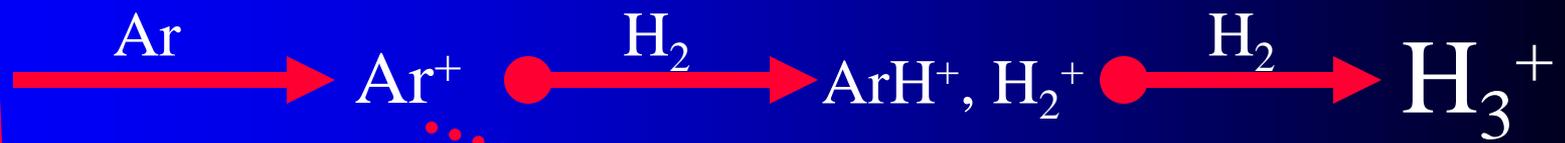


# Formation of $H_3^+$ in He/Ar/ $H_2$ mixture

$10^{17}/10^{14}/10^{11}$

microwave discharge

- $He^+$
- $He^m$
- $Ar^+$
- $Ar^m$
- $H_2^+$

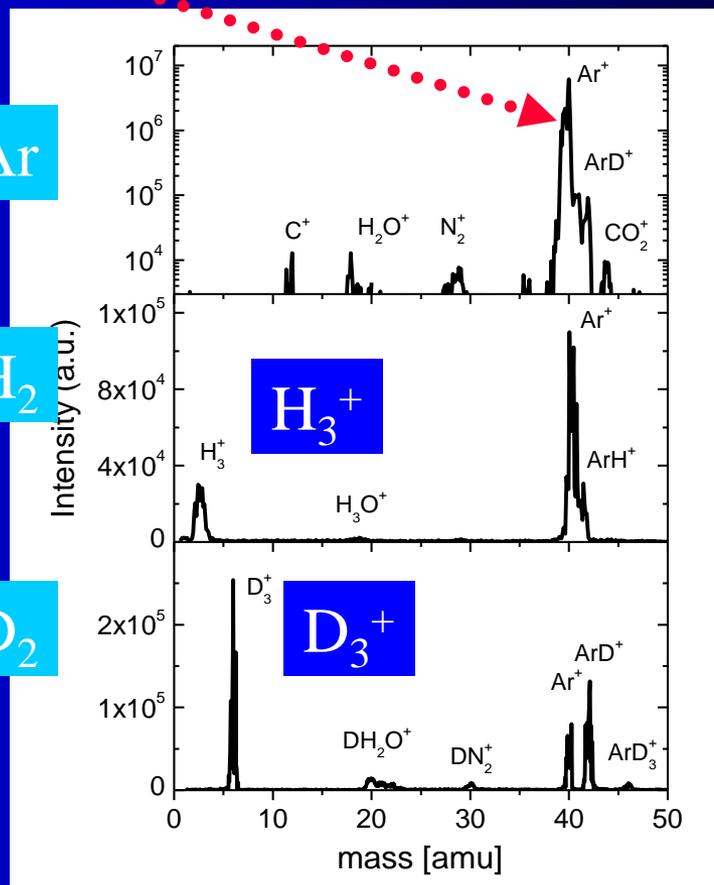


Changes due to the ion molecule reactions during the early afterglow

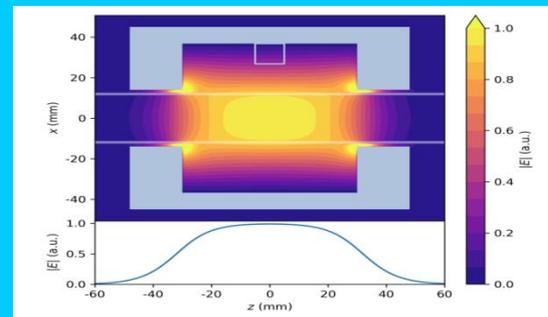
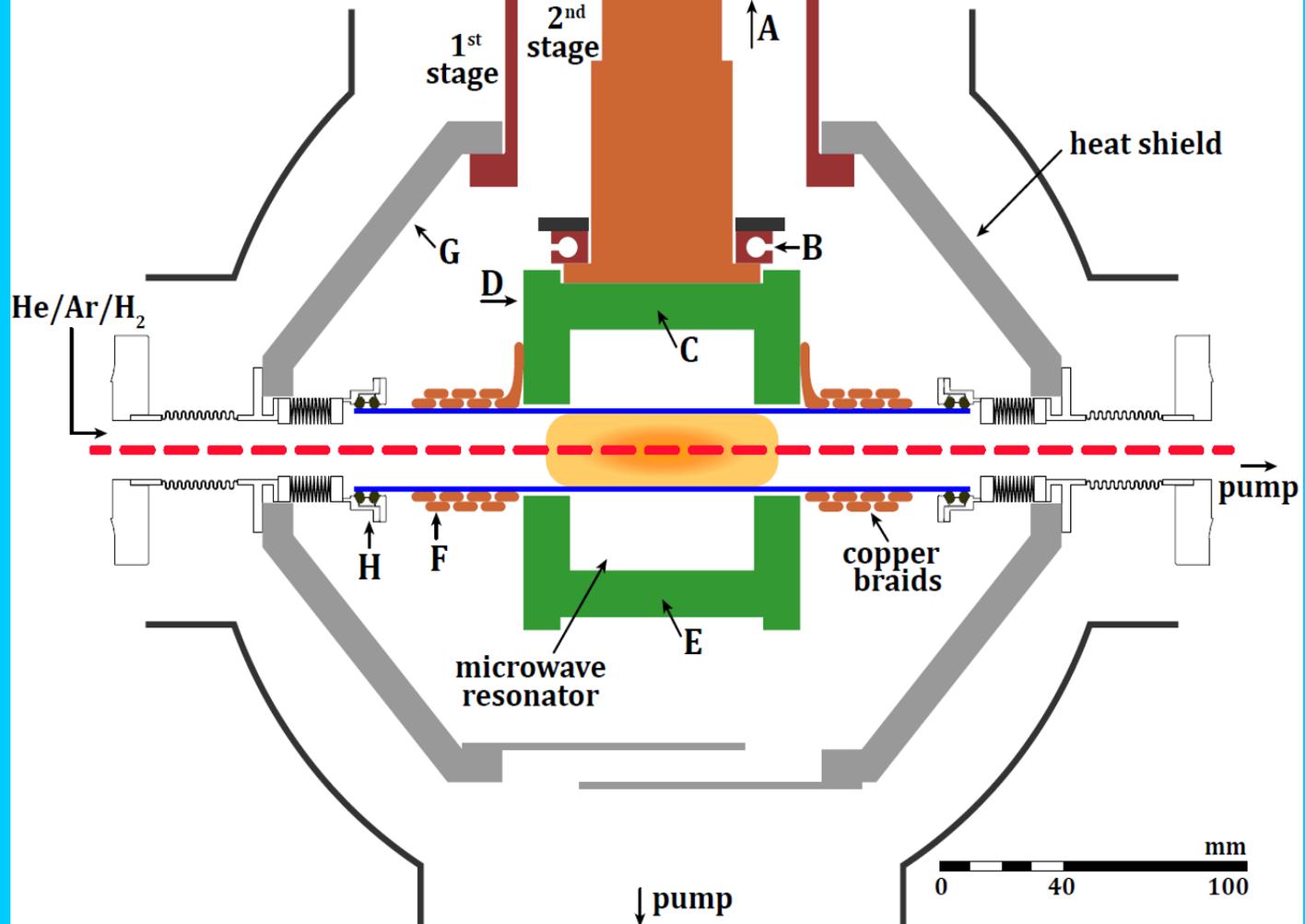
He/Ar

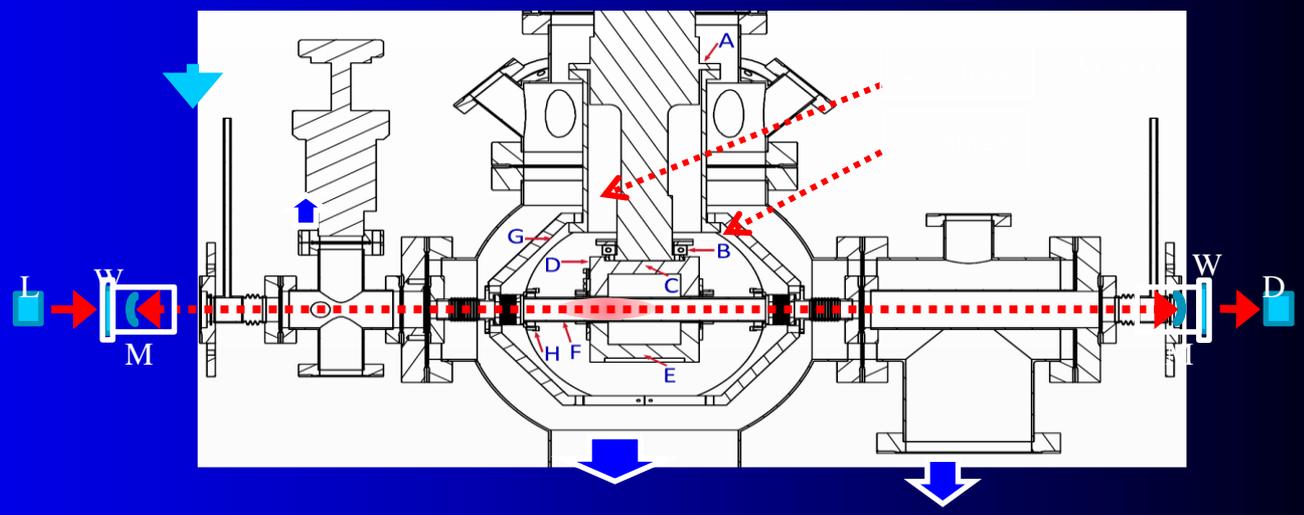
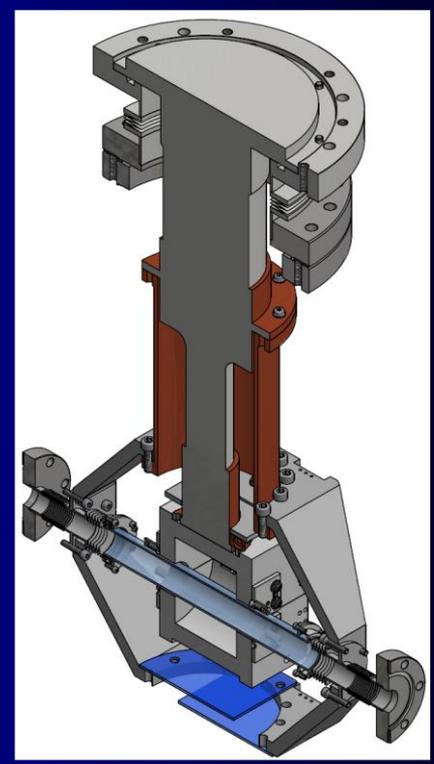
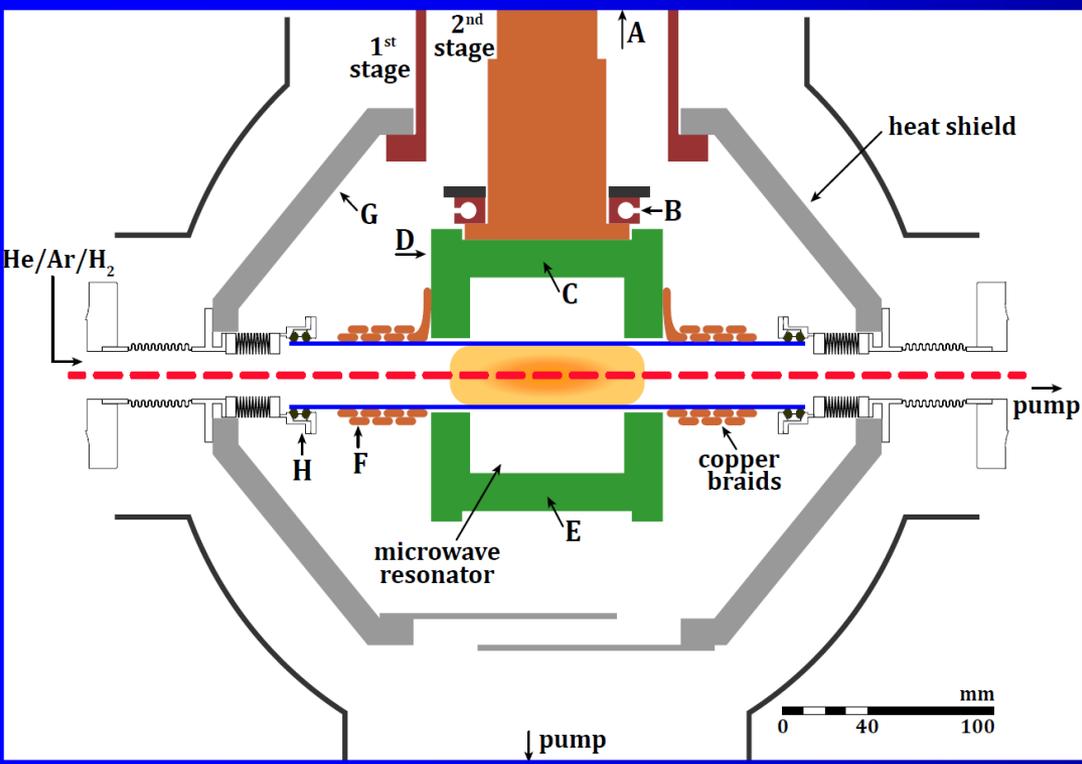
He/Ar/ $H_2$

He/Ar/ $D_2$

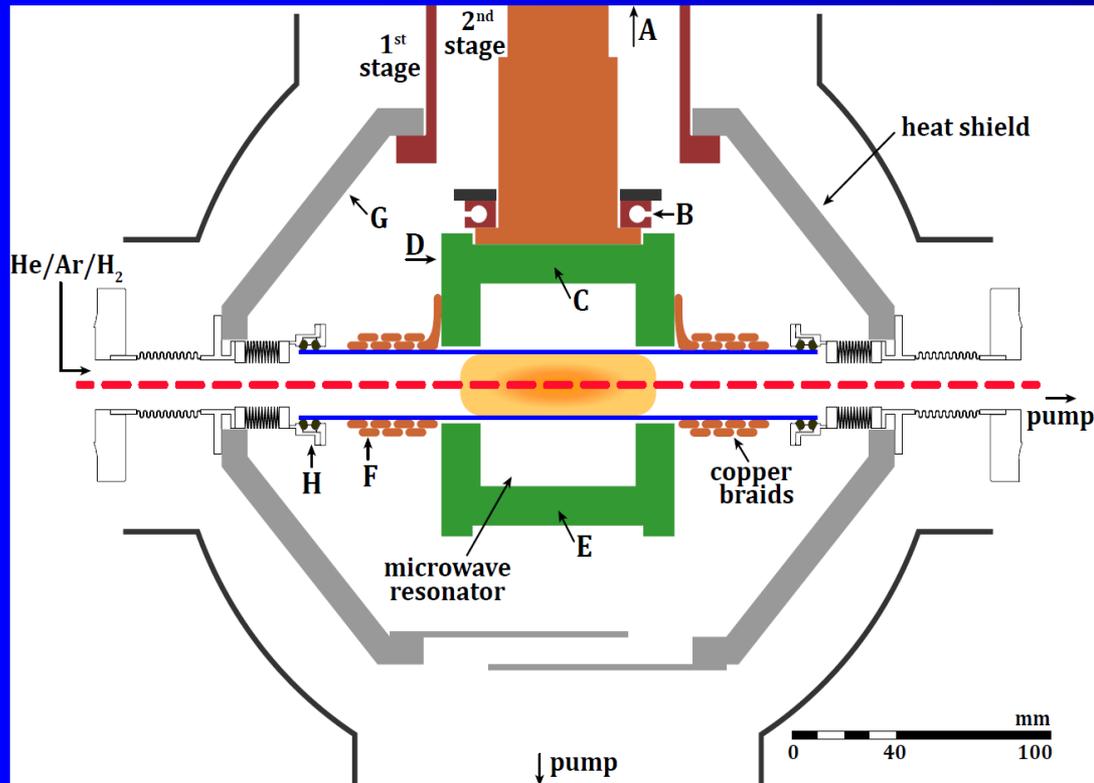


# Recombination

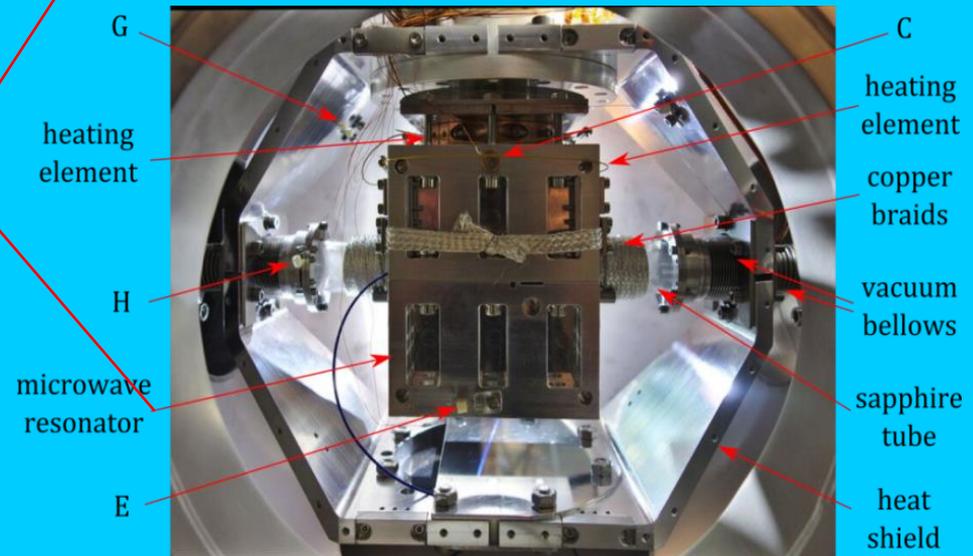
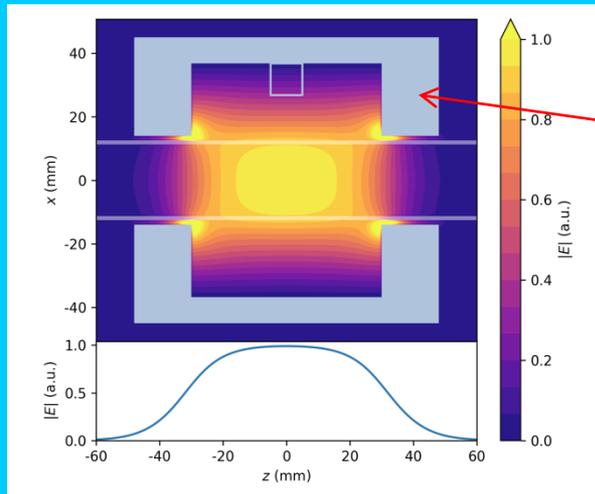
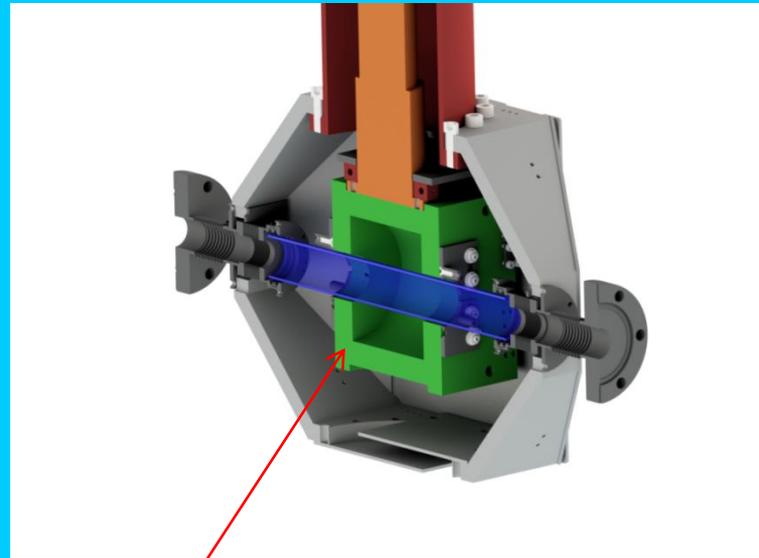
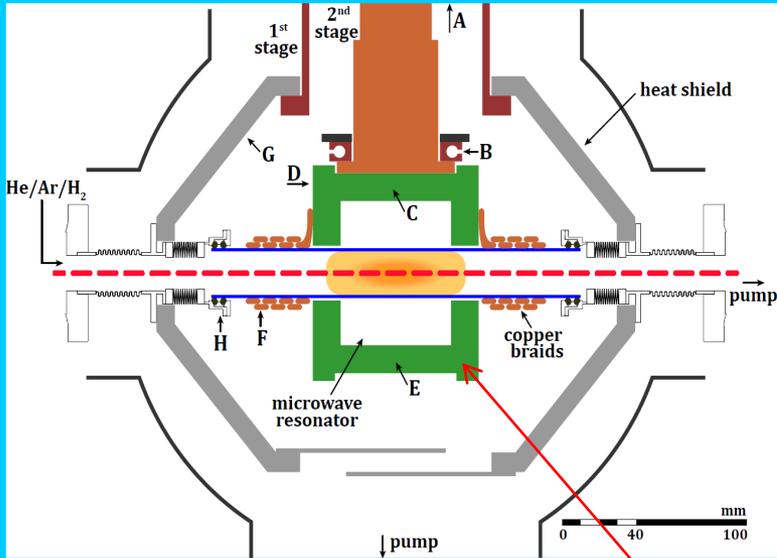




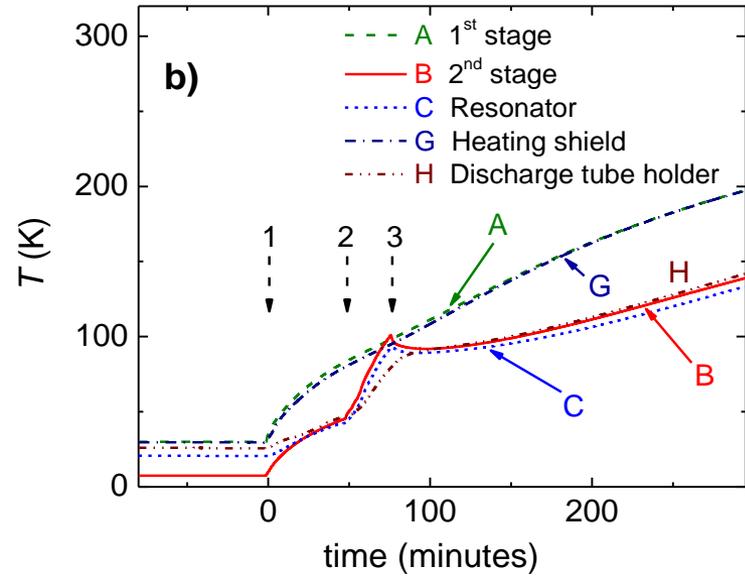
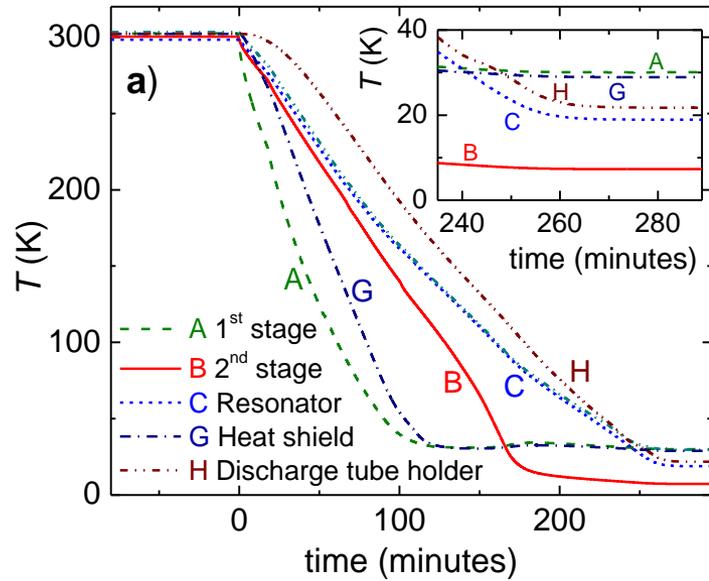
# Recombination



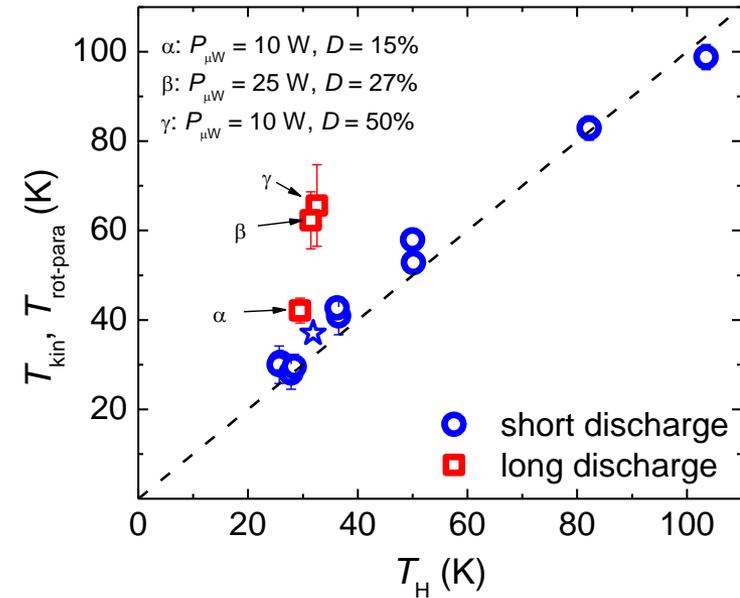
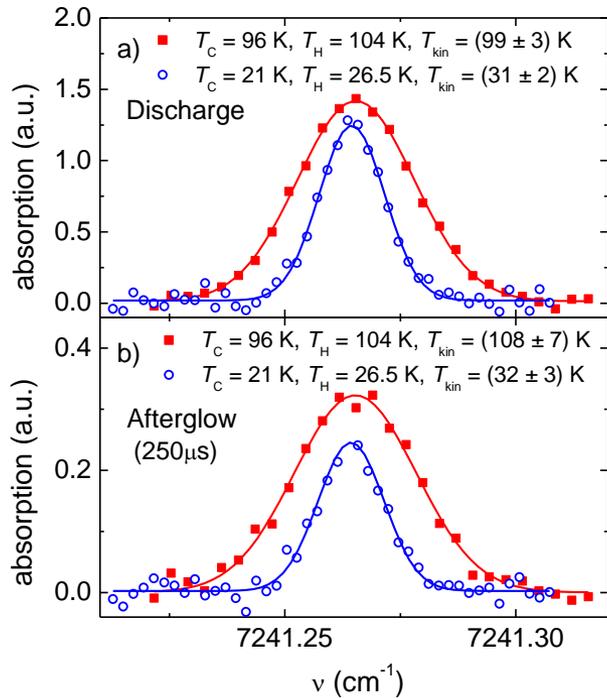
# Recombination



# Recombination



# Recombination



Examples of  $\text{H}_3^+$  absorption line profiles

The dependence of the kinetic temperature ( $T_{\text{kin}}$ ) of  $\text{H}_3^+$  ions on the temperature  $T_H$  (temperature of the discharge tube holder).

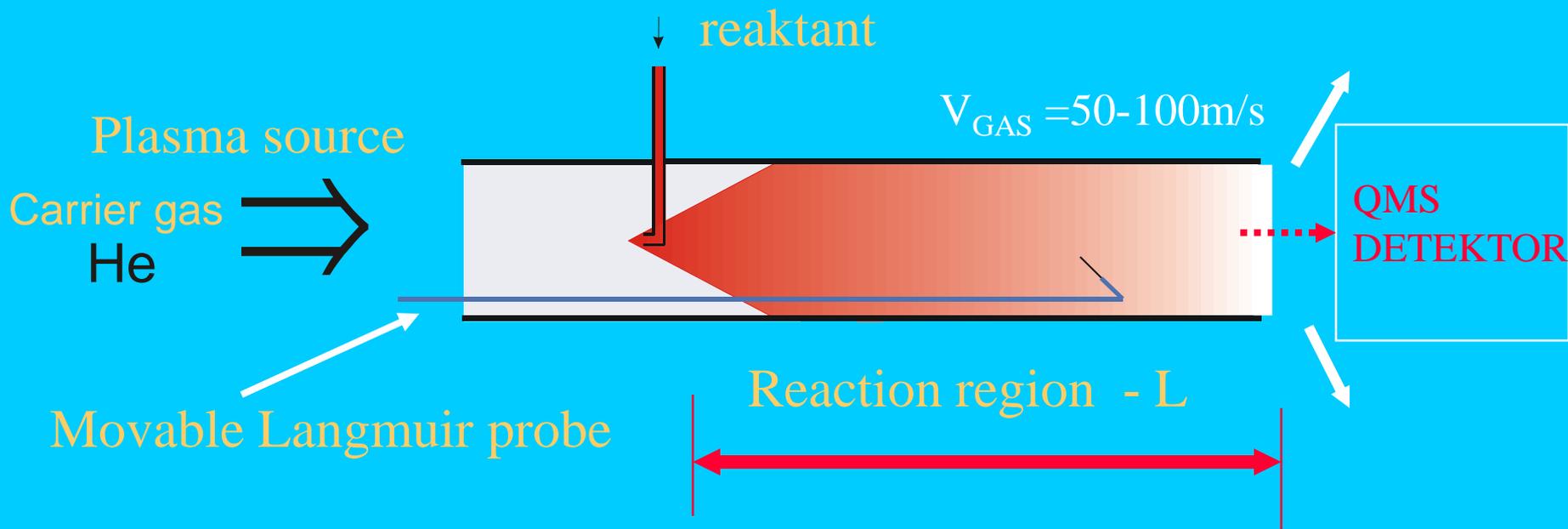
**RECOMBINATION**

**FLOWING AFTERGLOW**

# Diffusion in FA

Diffusion losses  
Ambipolar diffusion

$$[A^+] = [A^+]_0 \exp(-Dt / \Lambda^2) = [A^+]_0 \exp(-Dpt / p\Lambda^2) = [A^+]_0 \exp(-D_0 p_0 L / \nu p \Lambda^2)$$
$$\sim [A^+]_0 \exp(-D_0 p_0 L / \nu p \Lambda^2) \sim [A^+]_0 \exp(-const.L / Q)$$



$$[A^+] \sim [A^+]_0 \exp(-const.L / Q)$$

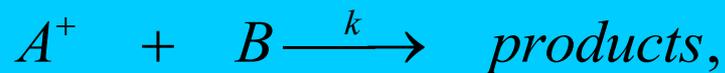
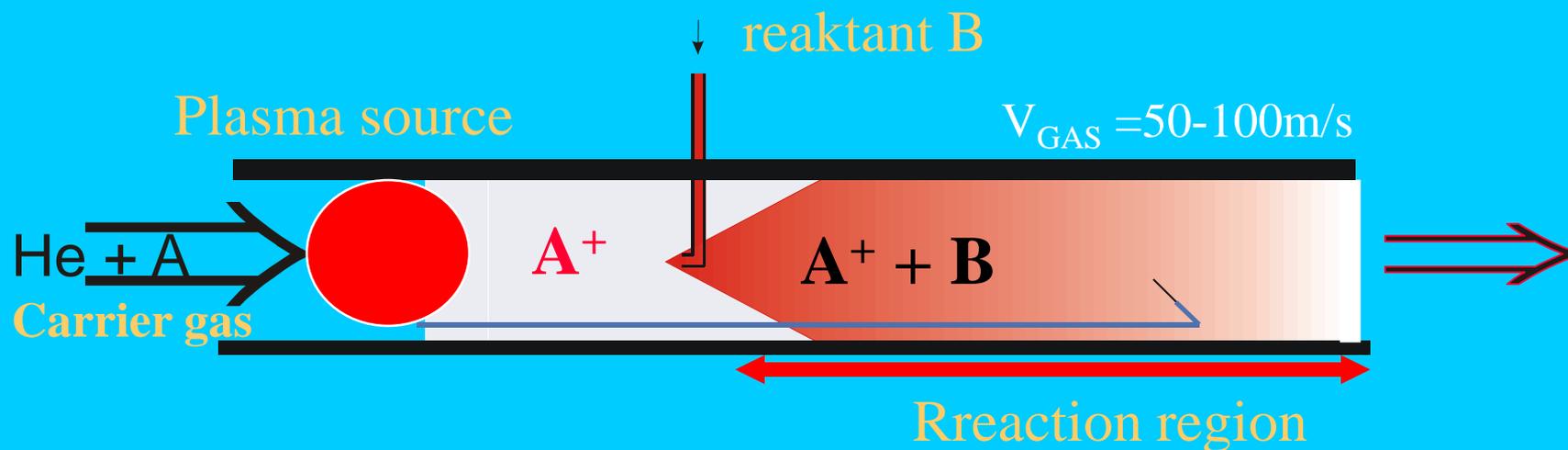
# FLOWING AFTERGLOW

Ion-molecule reactions

FA

FA  
FALP

E.E.Ferguson, Fehsenfeld, ~1965  
J. Hasted, D. Smith, N. Adams, ...



$$d[A^+] / dt = -k[B][A^+], \quad \text{at } [A^+] \ll [B]$$

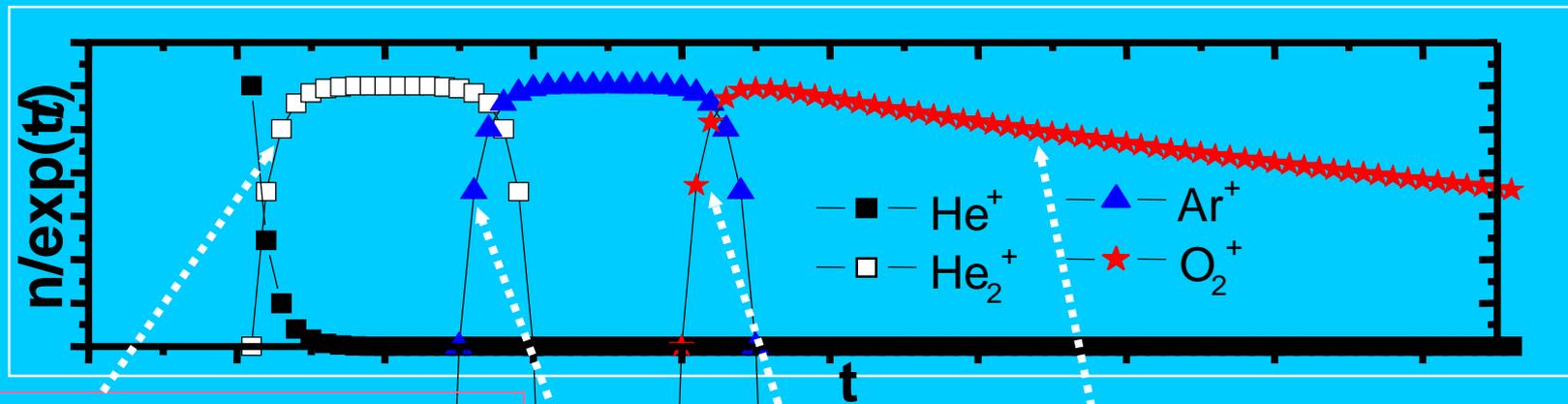
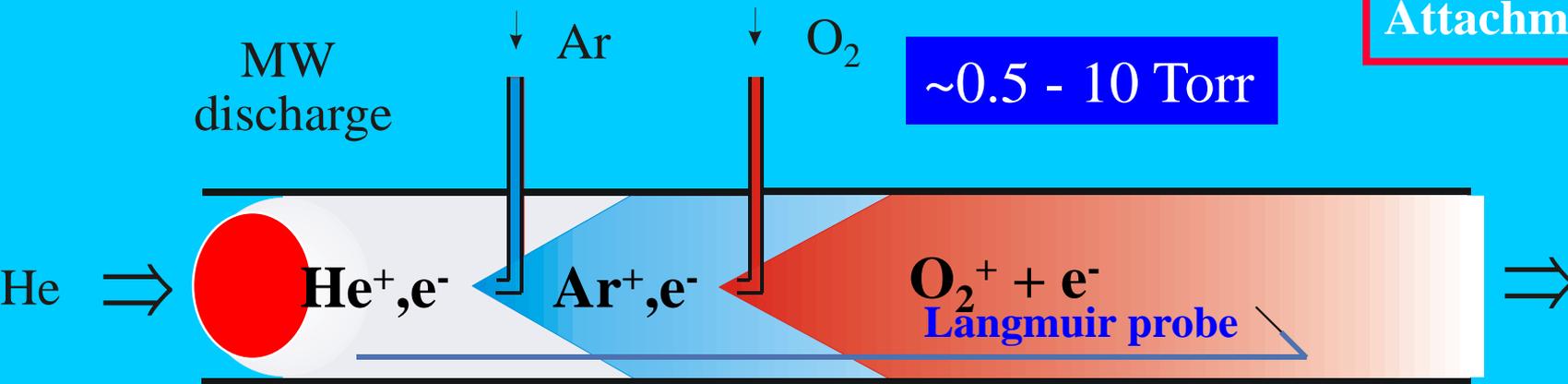
$$[A^+] = [A^+]_0 \exp(-k[B]t) = [A^+]_0 \exp(-k[B]L_0 / v)$$

SIFT

, D. Smith, N. Adams, ...

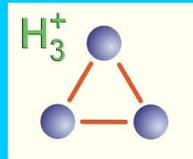
# Flowing Afterglow Langmuir Probe - FALP

Recombination Attachment

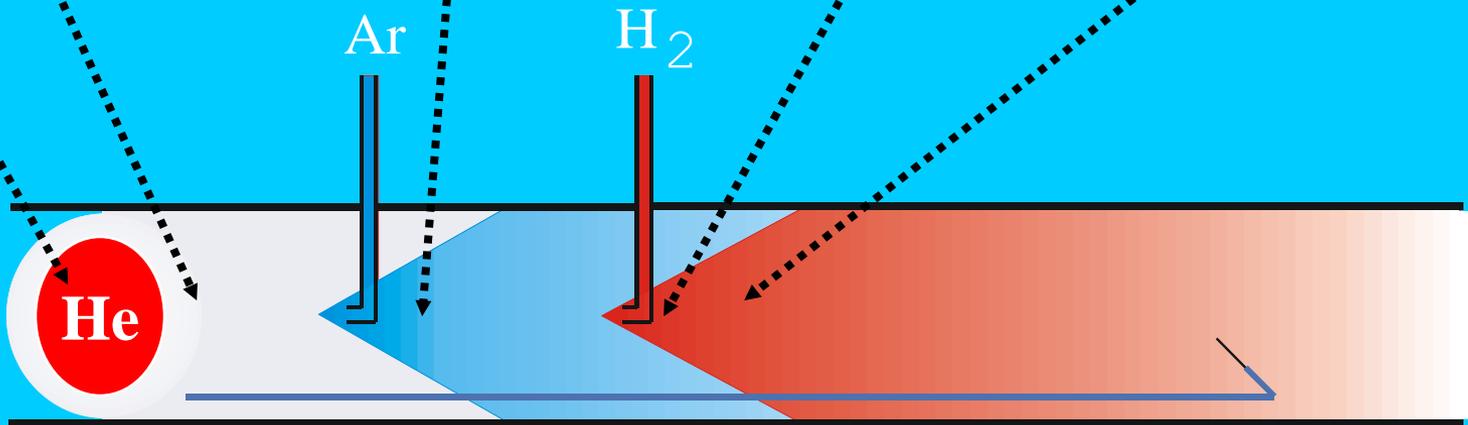
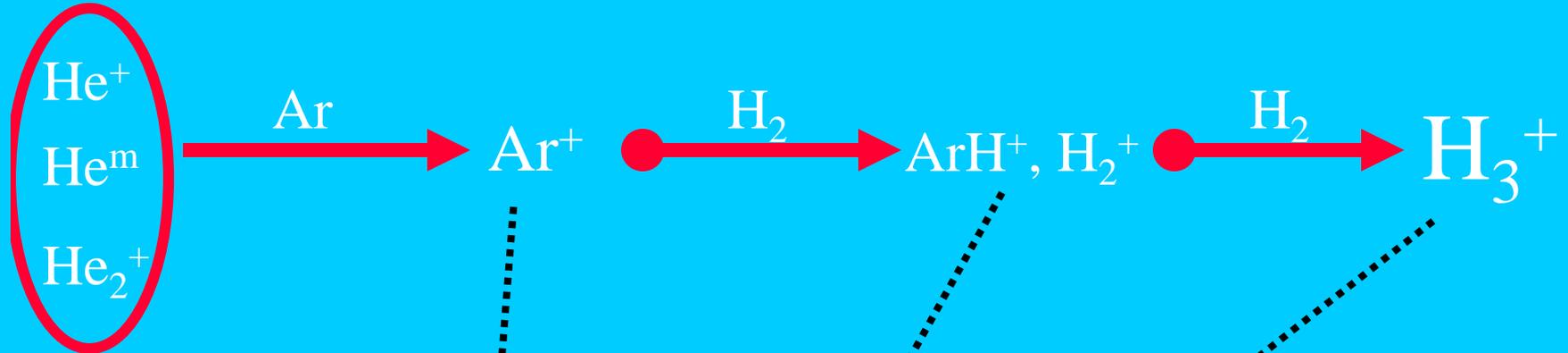


Diffusion, IMR  
Recombination

# FALP - Formation of $H_3^+$ in He/Ar/ $H_2$ mixture



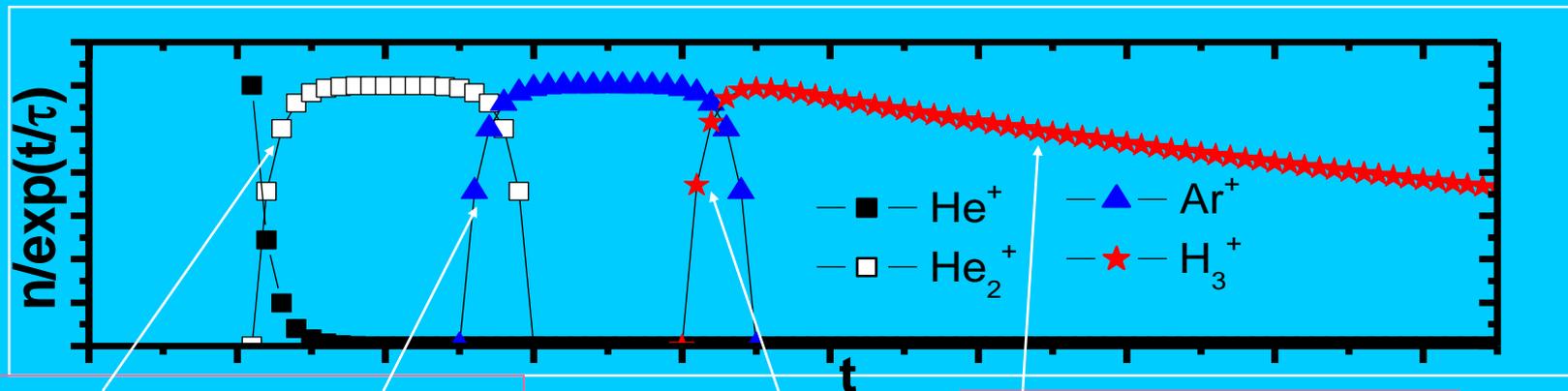
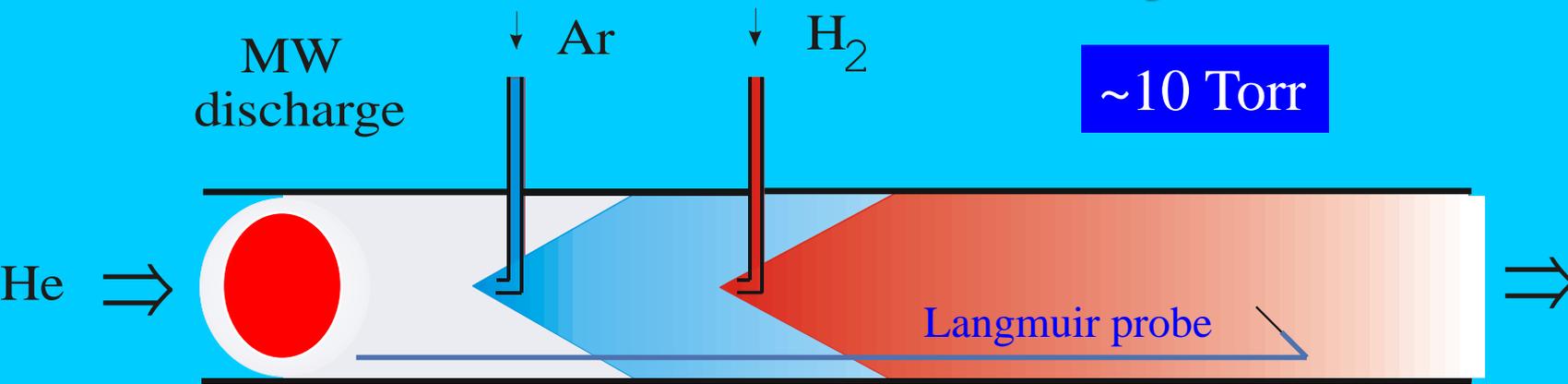
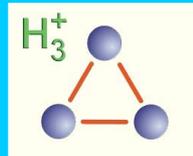
microwave discharge



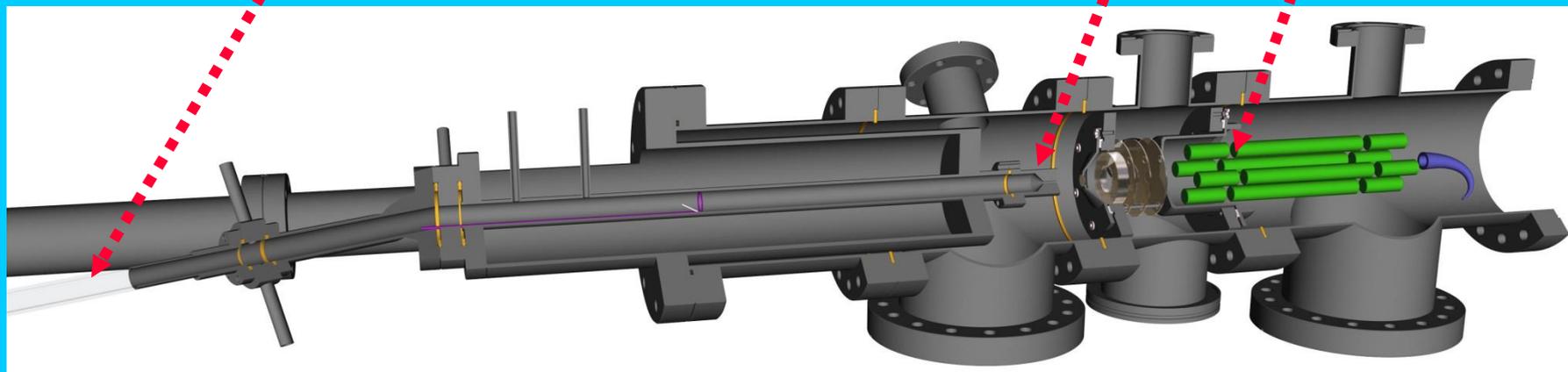
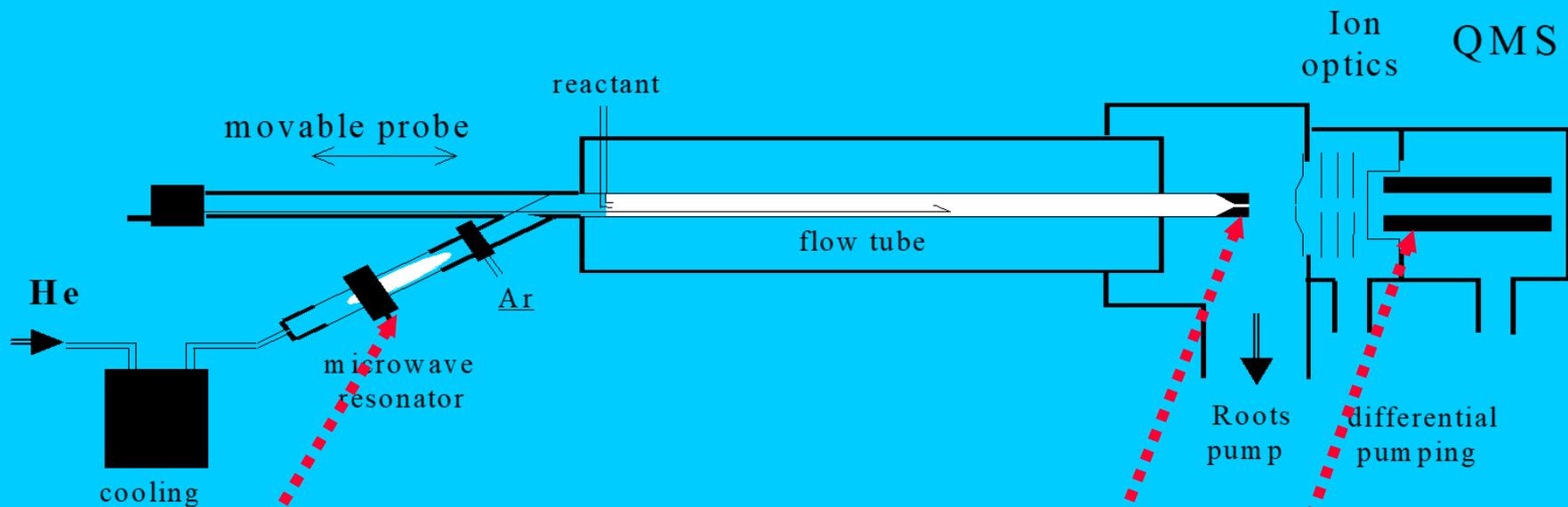
$T_e \sim 2eV$

$T_e = T_i = T_G = 300K$

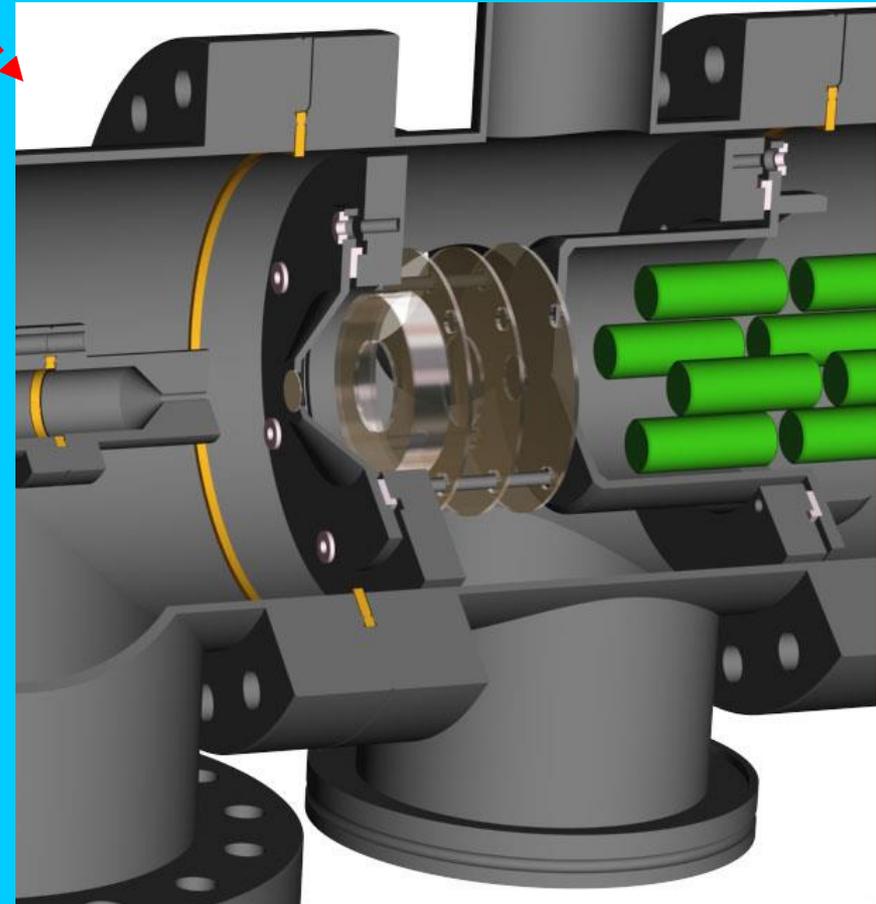
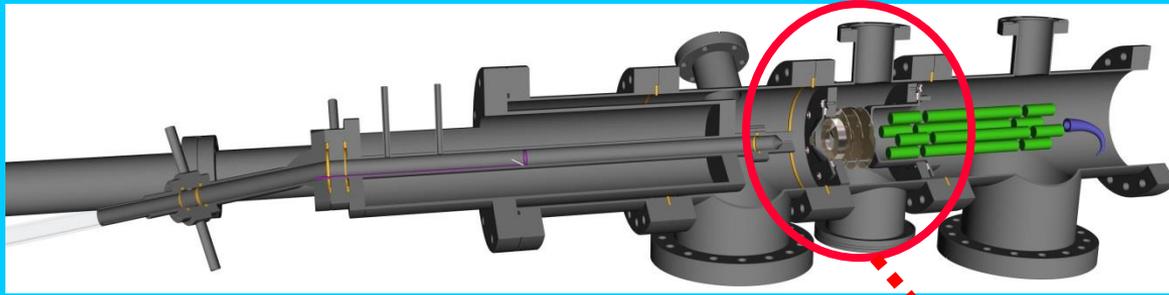
# FALP - RECOMBINATION OF H<sub>3</sub><sup>+</sup>



# FALP High pressure UHV version - PRAGUE



# FALP – Ion detection system

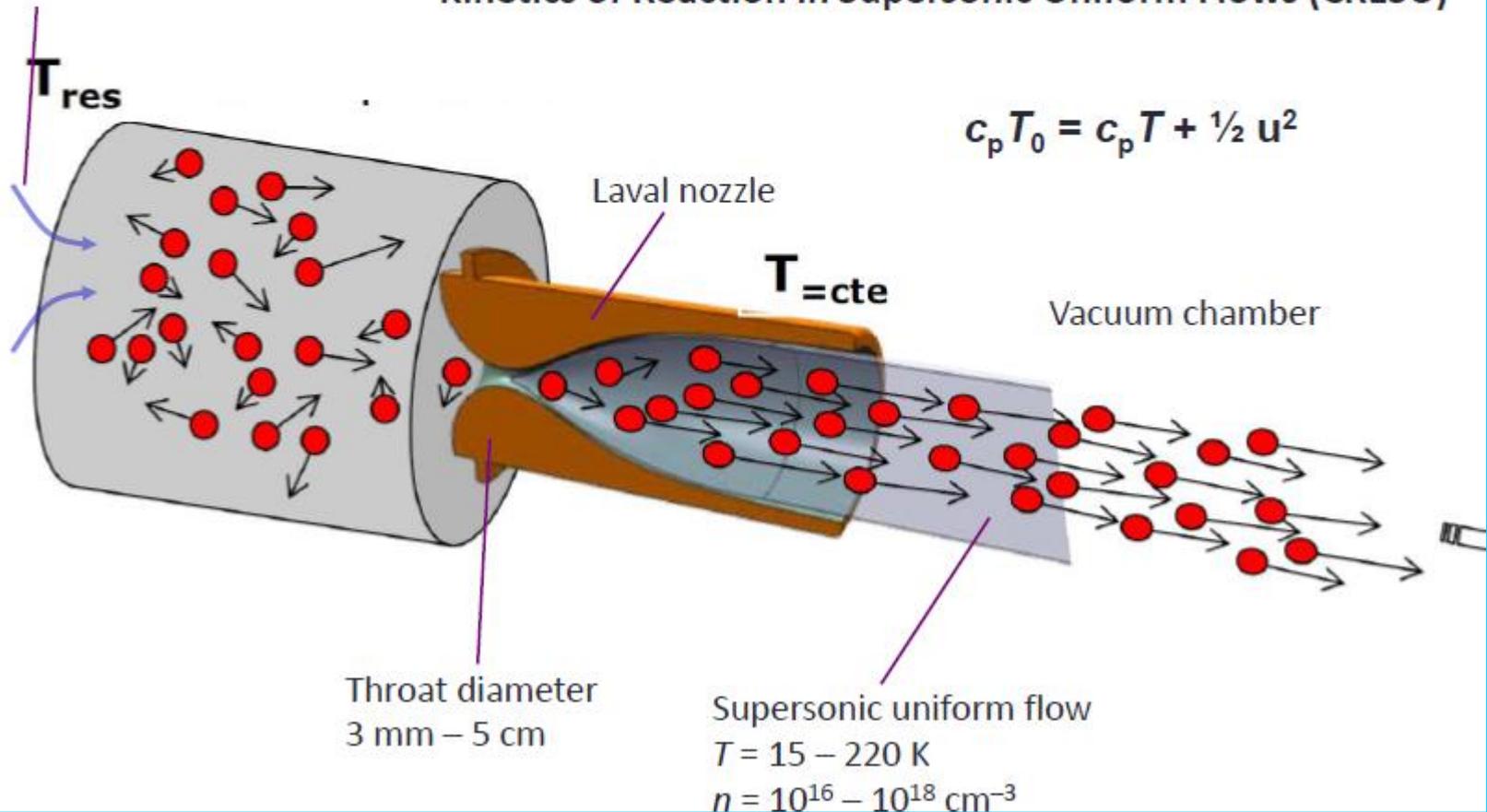


CRESU

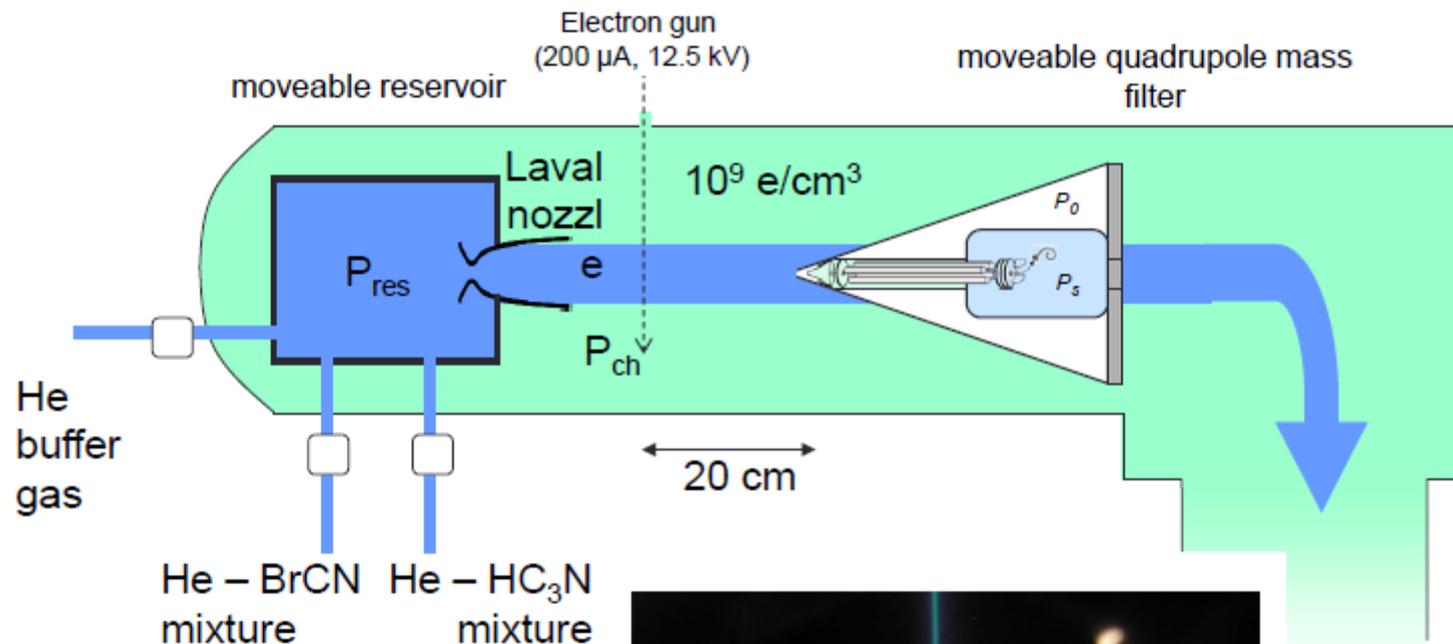
# The CRESU technique at Rennes

Carrier gas (He, Ar or N<sub>2</sub>) + reactants

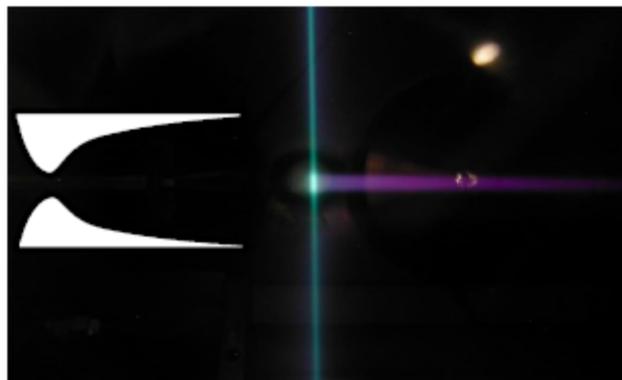
## Kinetics of Reaction in Supersonic Uniform Flows (CRESU)

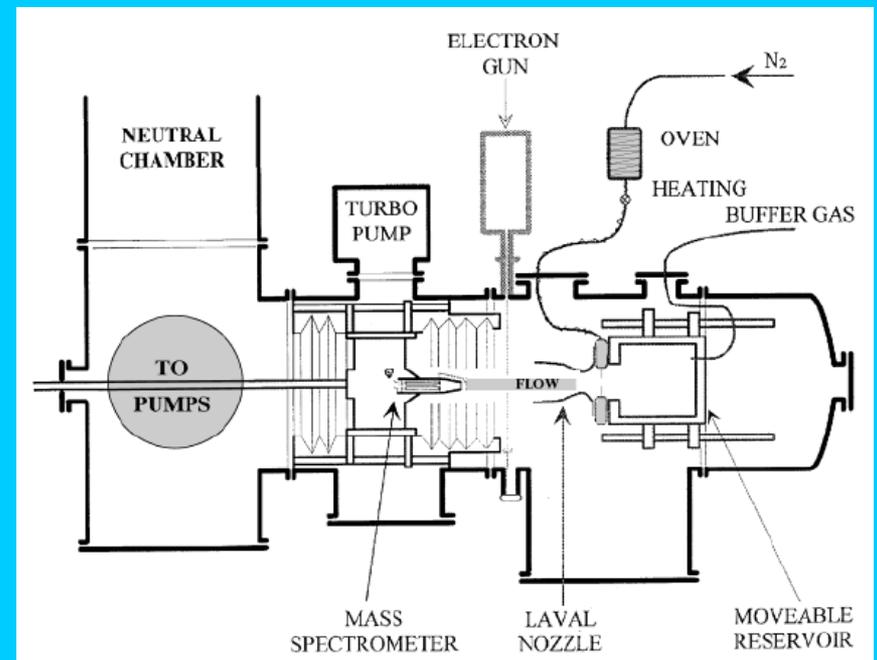
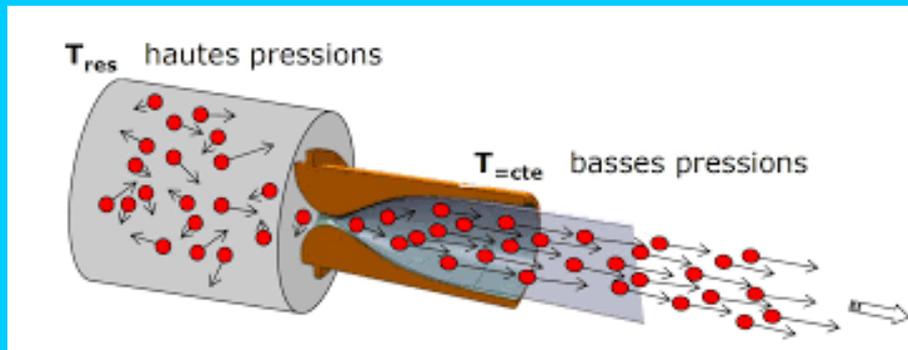
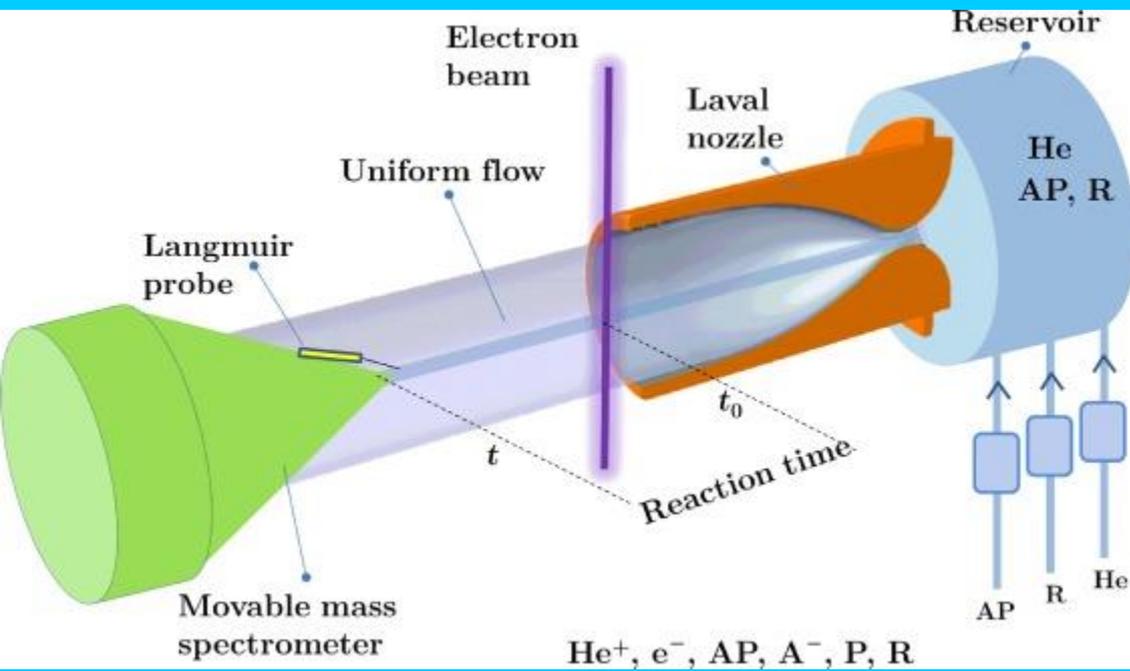


## Kinetics of anion-molecule reactions at low temperature



- CN<sup>-</sup> + HC<sub>3</sub>N ( L. Biennier, S. Carles, J-C Guillemin et al. Icarus, 227, 123, 2014)
- C<sub>3</sub>N<sup>-</sup> + HC<sub>3</sub>N (in progress)
- Collaboration with C. Alcaraz and co-workers (Orsay and Prague)

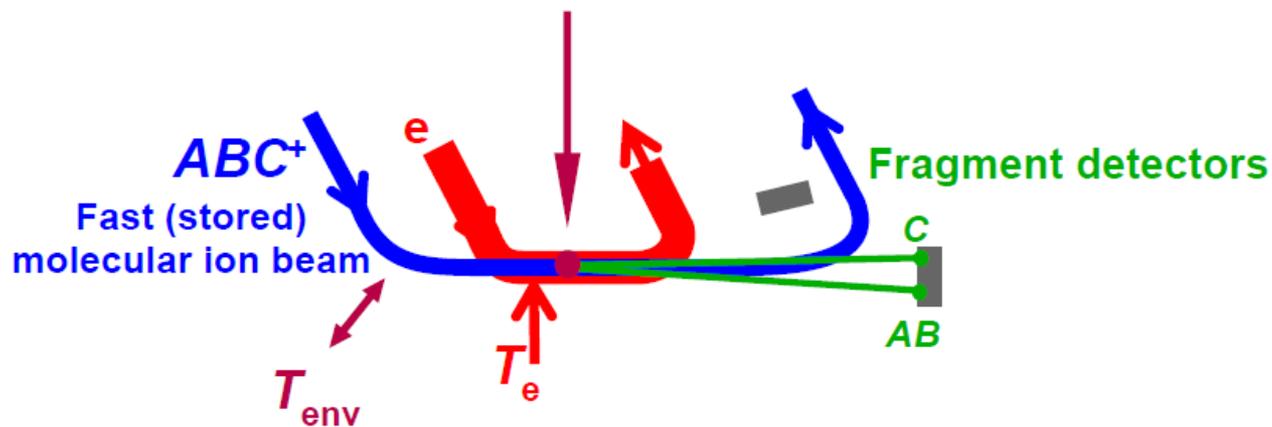




TSR

# Outlook: Electron-beam collision studies

## Electron capture and dissociation Dissociative recombination



$$E_{coll} = \frac{1}{2} m_e (v_e - v_i)^2$$

can be scanned from  $\sim 1$  meV ... 50 eV

# Experiments

PLASMA experiments SA and FA

Crossed beam experiments

Marched beam, Storage rings - TSR, Crying, Astrid

- multi collisions

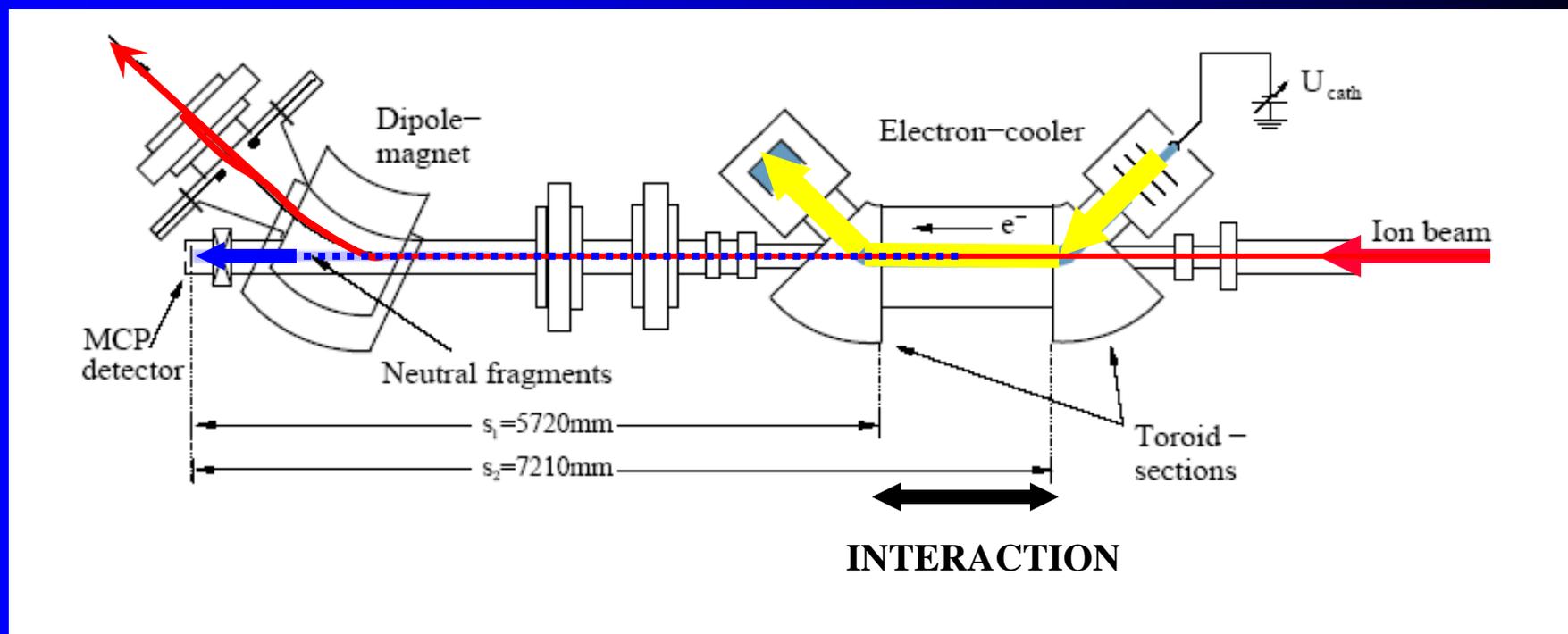
$\{\alpha(T)\}$

- single collisions

$\{\sigma(v_r)\}$

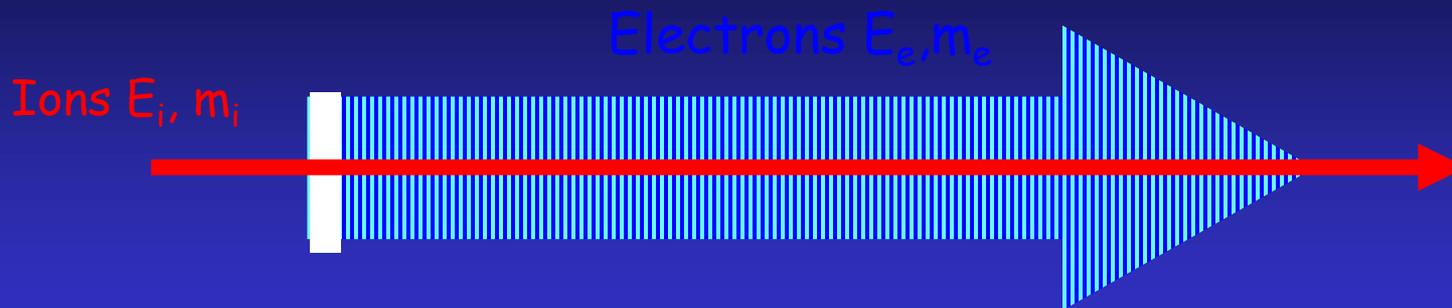
- single collisions

$\{\sigma(v_r)\}$



Electron-cold molecular ion reaction:  
Dissociative Recombination

Merged Beam Kinematics



$$E_{\text{cm}} = \frac{1}{2} m_e v_{\text{cm}}^2 \approx \left[ \sqrt{\frac{m_e}{m_i}} E_i - \sqrt{E_e} \right]^2$$

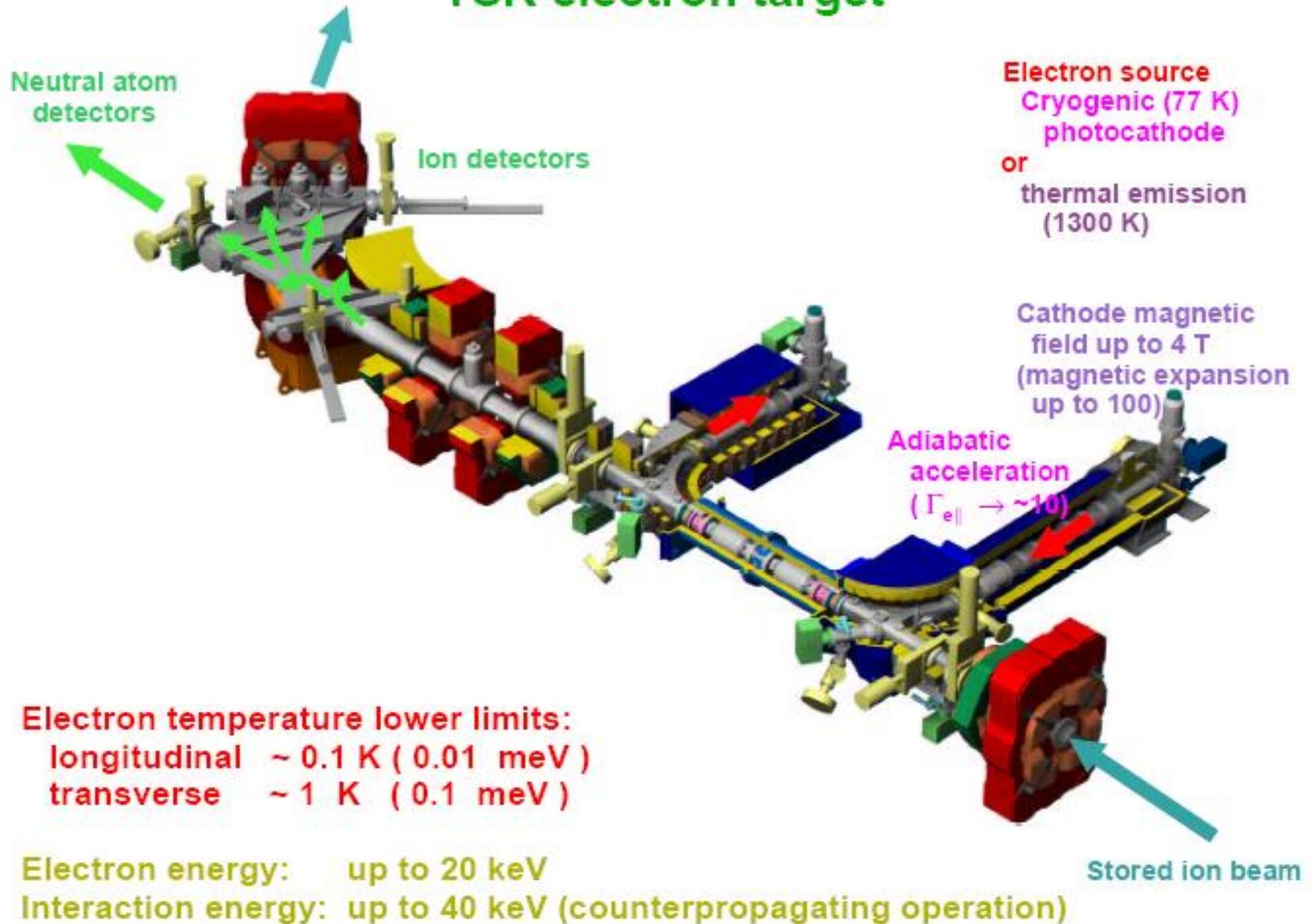
Center of mass resolution:

$$\Delta E_{\text{cm}} = \left\{ \left[ \left( 1 - \frac{v_e}{v_i} \right) \frac{m_e}{m_i} \Delta E_i \right]^2 + \left[ \left( 1 - \frac{v_i}{v_e} \right) \Delta E_e \right]^2 \right\}^{1/2}$$

~ meV resolution for zero relative kinetic energy!

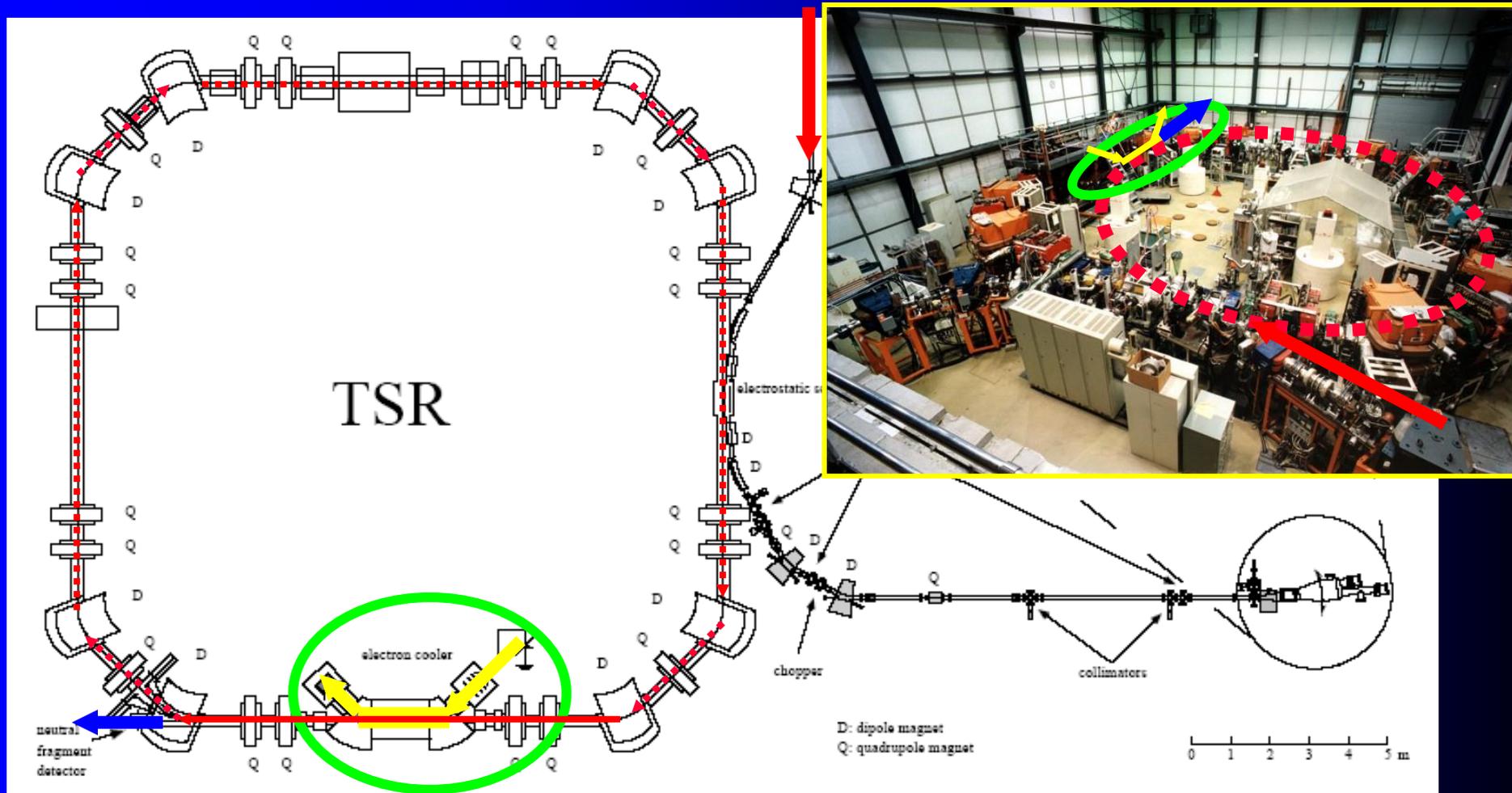
# TSR electron target

## TSR electron target



# Reality - TSR (MPIK Heidelberg)

Injection of INTERNALLY COLD  $H_3^+$  IONS(12-50K) with kinetic energy 1-2 MeV



Detection of neutrals

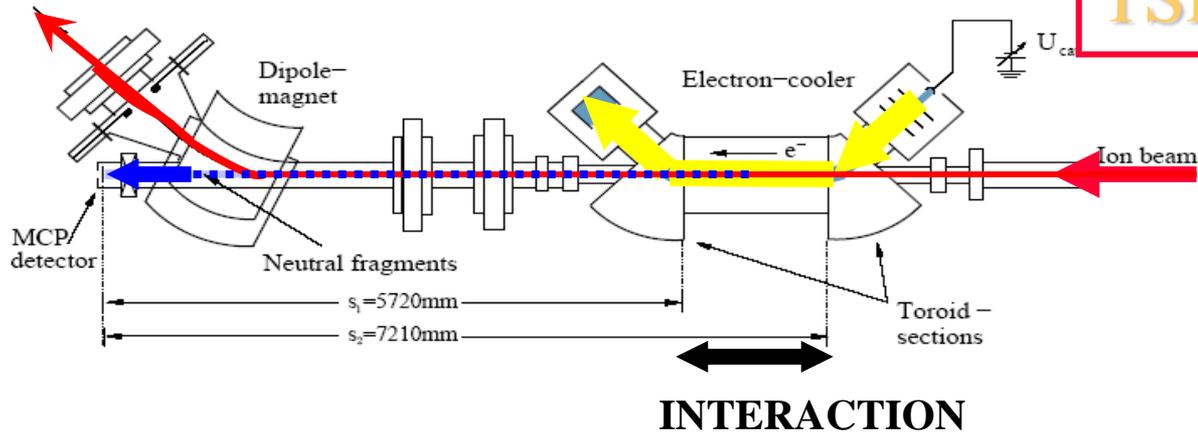
INTERACTION at meV collision energies

Detection of  $H_3^+(v,j)$

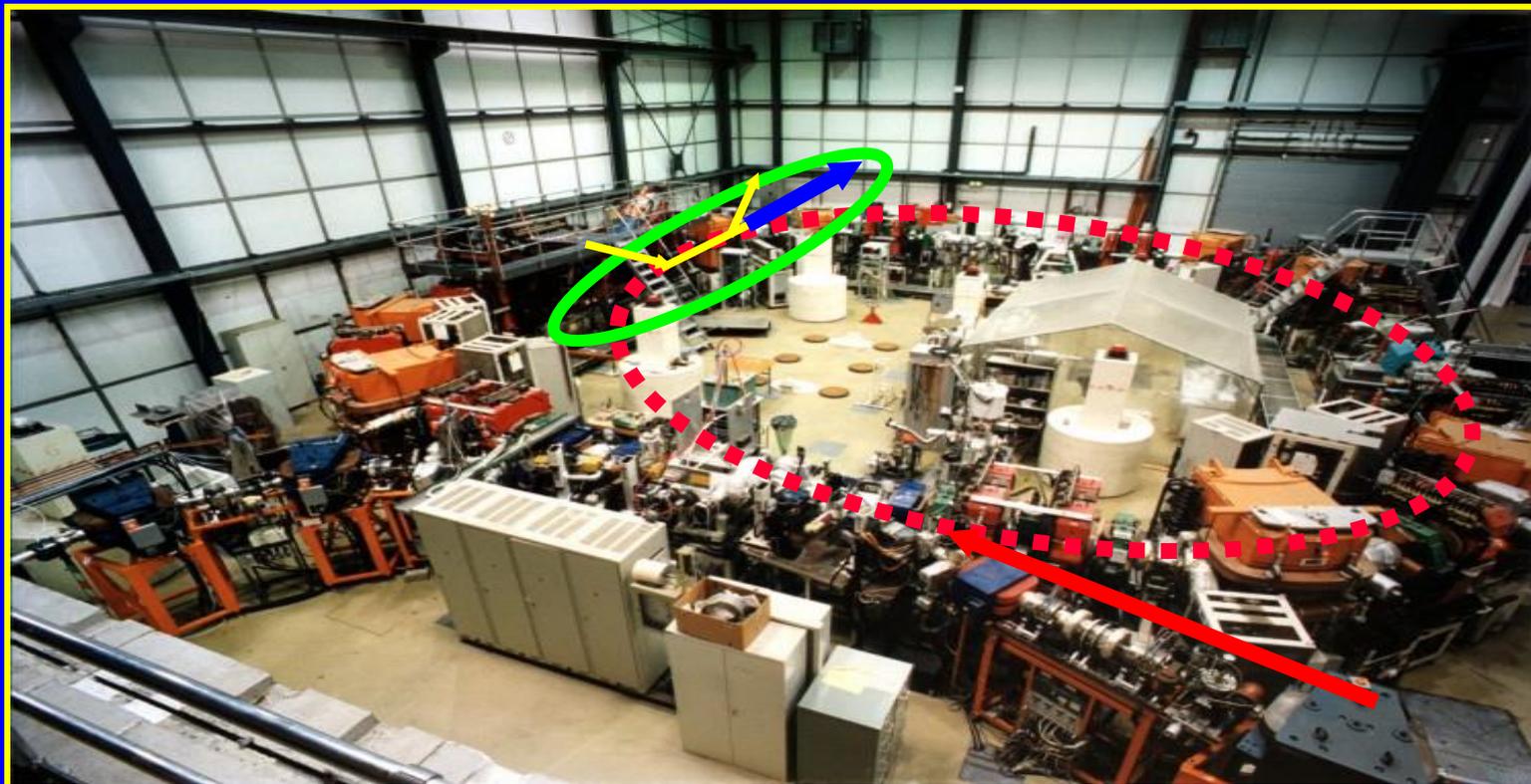
# PLASMA PHYSICS I/7

## Recombination

### TSR (MPIK Heidelberg)



Kumulativní prsteneč



# TSR Heidelberg, ion injection and ion source

## Ion storage rings

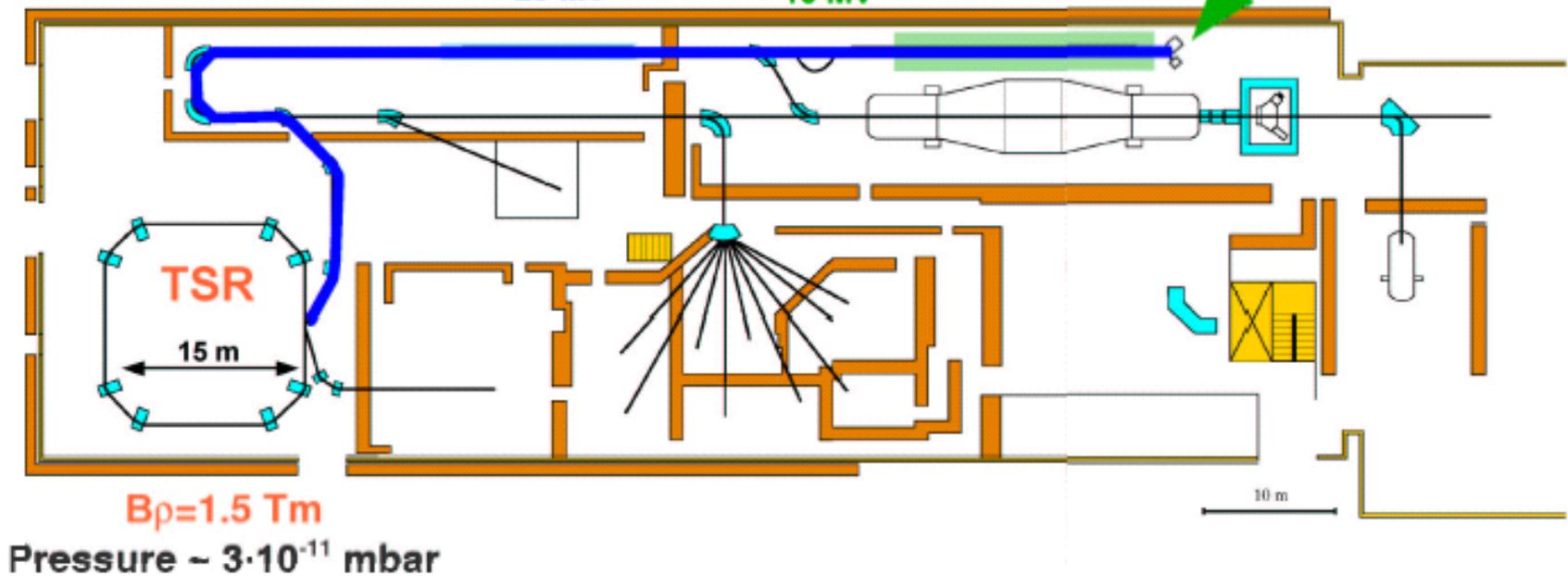
TSR, Heidelberg

Mass limit  
RFQ:  $q/A \leq 9$

$H_2^+$ ,  $HD^+$ ,  $D$ ,  
 $H_3^+$ ,  $H_2D^+$ ,  $D_2H^+$ ,  $D_3^+$ ,  
 $He_2^+$ ,  
 $LiH_2^+$ , ...

Post Accelerator  
~ 25 MV

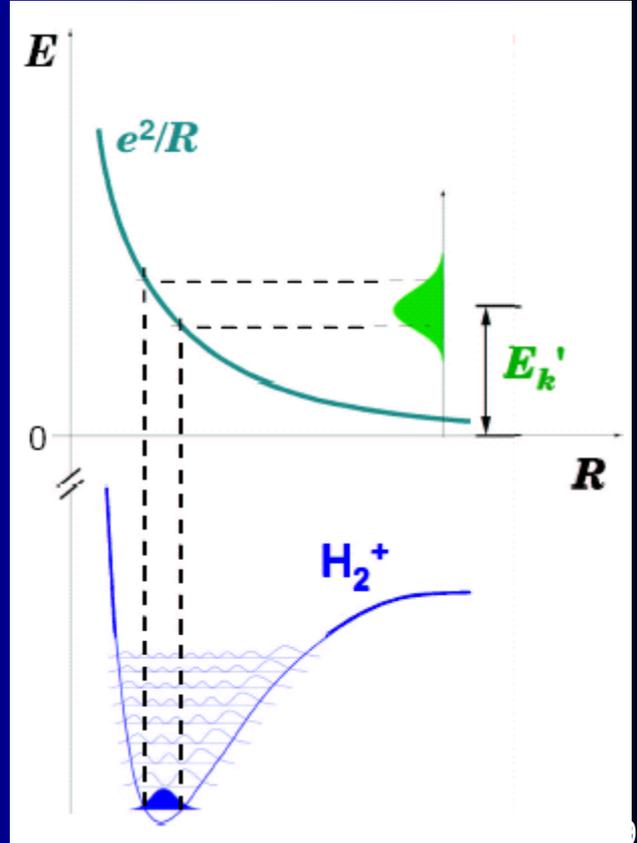
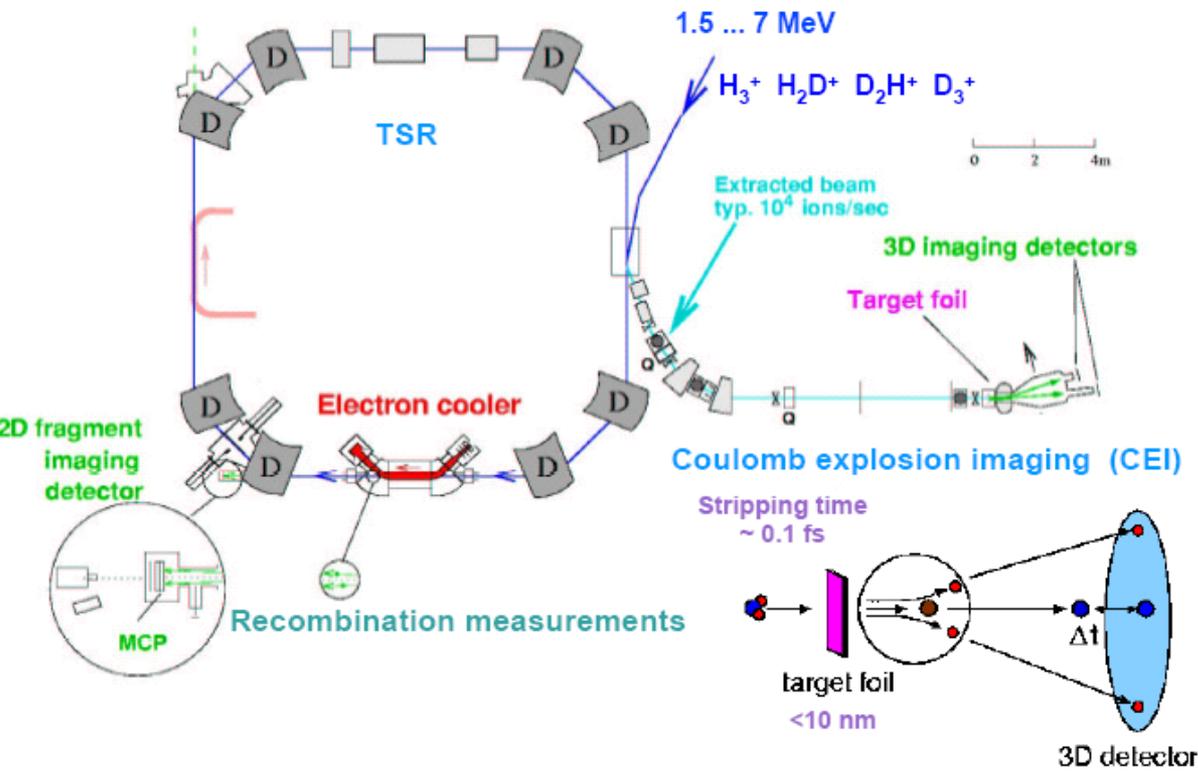
High current injector  
~ 10 MV Linac RFQ



$B\rho = 1.5 \text{ Tm}$   
Pressure  $\sim 3 \cdot 10^{-11} \text{ mbar}$

# State diagnostics

## State diagnostics methods at the TSR



Thanks for your attention!



A. Becker  
K. Blaum  
C. Breitenfeldt  
F. Fellenberger  
S. George  
J. Göck  
M. Grieser  
F. Grussie  
R. von Hahn  
P. Herwig  
J. Karthein

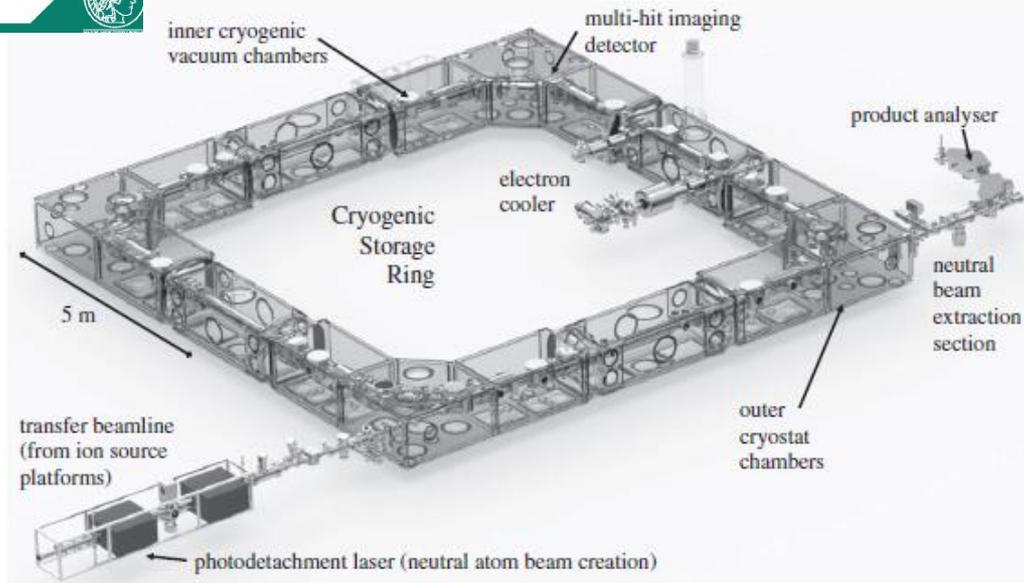
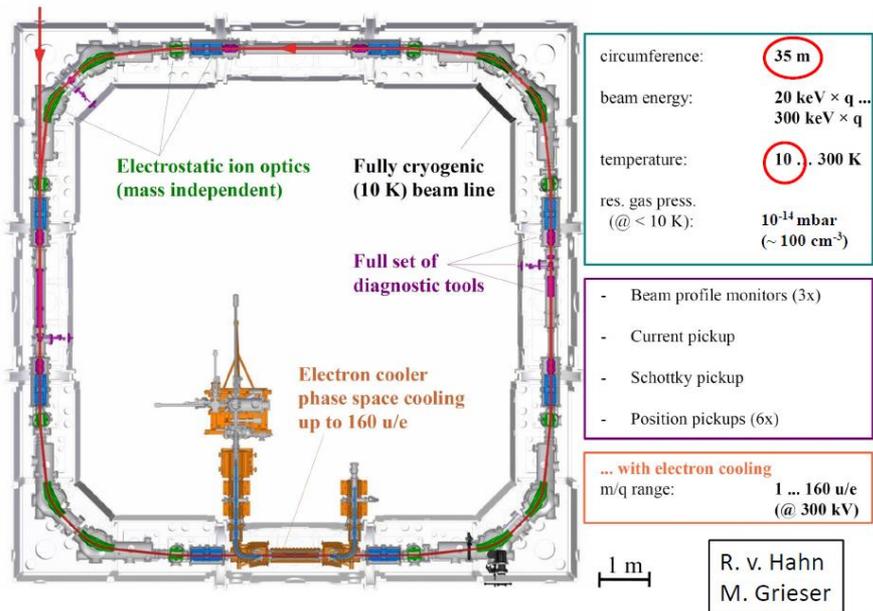
C. Krantz  
H. Kreckel  
S. Kumar S.  
M. Lange  
J. Lion  
S. Lohmann  
C. Meyer  
P. M. Mishra  
O. Novotný  
P. O'Connor  
R. Repnow

S. Saurabh  
S. Schippers  
C. D. Schröter  
D. Schwalm  
L. Schweikhard  
K. Spruck  
X. Urbain  
S. Vogel  
A. Wolf  
D. Zajfnan



CSR

# The CSR – overview



PHILOSOPHICAL  
TRANSACTIONS A

royalsocietypublishing.org/journal/rsta

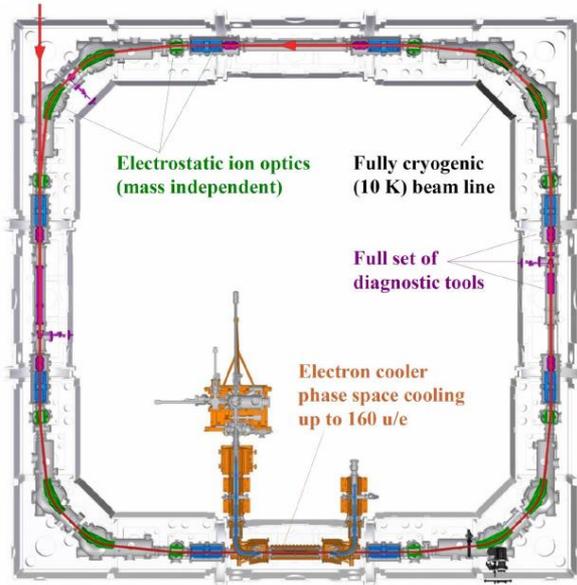
## Astrochemical studies at the Cryogenic Storage Ring

H. Kreckel, O. Novotný and A. Wolf

Max Planck Institut für Kernphysik, 69117 Heidelberg, Germany

**Figure 1.** Overview of the CSR. The experimental set-ups relevant for astrochemical studies are labelled in the insets. The image includes the new low-energy electron cooler as well as the photodetachment section for the neutral beam creation in the injection beamline, the neutral beam extraction and some of the corresponding detector units.

# The CSR – overview



circumference: **35 m**  
beam energy:  $20 \text{ keV} \times q \dots$   
 $300 \text{ keV} \times q$   
temperature: **10** .. 300 K  
res. gas press.  
(@ < 10 K):  $10^{-14} \text{ mbar}$   
( $\sim 100 \text{ cm}^{-3}$ )

- Beam profile monitors (3x)
- Current pickup
- Schottky pickup
- Position pickups (6x)

... with electron cooling  
m/q range: 1 .. 160 u/e  
(@ 300 kV)

R. v. Hahn  
M. Grieser



