POLS 201: Data Analysis and Politics Professor Elena Llaudet



Lecture 13 | Estimating Causal Effects with Observational Data and the Problem of Confounders



 EXPLAIN: To estimate the causal effect of a treatment on an outcome
 what is the effect of small classrooms on student performance?

BOOK OUTLINE							
Ch	apter	Goal					
2.	Estimating Causal Effects with Randomized Experiments	EXPLAIN					
3.	Inferring Population Characteristics via Survey Research	MEASURE					
4.	Predicting Outcomes Using Linear Regression	PREDICT					
5.	Estimating Causal Effects with Observational Data	EXPLAIN					

Plan for Today

- Review: Causation and Randomized Experiments
- Observational Studies
- Confounding Variables or Confounders
 - Why Are Confounders a Problem?
- Why Don't We Worry About Confounders in Randomized Experiments?
- How Can We Estimate Causal Effects with Observational Data?
 - Interpretation of $\widehat{\beta}$ When X Is the Treatment Variable and Y Is the Outcome Variable

Review: Causation

- To measure causal effects, we need to compare the factual outcome with the counterfactual outcome
 - Fundamental problem: We can never observe the counterfactual outcome
- To estimate causal effects, we must find or create a situation in which the treatment and control groups are comparable with respect to all the variables that might affect the outcome other than the treatment variable itself
- Only when that assumption is satisfied can we use the factual outcome of one group as a good proxy for the counterfactual outcome of the other, and vice versa, thus, bypassing the fundamental problem of causal inference

Review: Randomized Experiments

- In randomized experiments, we can rely on the random assignment of treatment to make treatment and control groups, on average, identical to each other in terms of all observed and unobserved pre-treatment characteristics
- Thus, we can estimate the average treatment effect with the difference-in-means estimator

 $\overline{Y}_{\text{treatment group}} - \overline{Y}_{\text{control group}}$

Observational Data

- But, what happens when we cannot conduct a randomized experiment and have to analyze observational data?
 - Observational data: data collected about naturally occurring events (i.e., researchers do not get to assign the treatment)
- We can no longer assume that treatment and control groups are comparable
- We have to identify any relevant differences between treatment and control groups (known as confounding variables or confounders)
- Then, we have to statistically control for them so that we can make the two groups comparable

Confounders or Confounding Variables

- A confounding variable, or confounder, is a variable that affects both
 - (i) the likelihood to receive the treatment X and
 - ► (ii) the outcome Y
- In mathematical notation, we represent a potential confounding variable as Z



Why Are Confounders a Problem?

- ▶ They obscure the causal relationship between X and Y
- In the example above, if we observed that, on average, private school students perform better than public school students, we would not know whether it is
 - because they attended a private school or
 - because they came from wealthier families that could afford to provide them with after-school help
- We would not know what portion of the observed differences in test score performance (the difference-in-means estimator), if any, could be attributed to the causal effect of the treatment (attending a private school) and what portion could be attributed to the confounding variable (coming from a wealthy family)



- In the presence of confounders, correlation does not necessarily imply causation
- Just because we observe two variables highly correlated with each other—when we observe one increase, we usually observe the other increase or decrease—it does not automatically mean that one causes the other
 - There could be a third variable that causes both
- For example, ice cream sales and shark attacks are highly correlated with each other. Does this mean that eating ice cream increases the probability that a shark attacks you?



in the average causal effect of attending a private school, as opposed to a public one, on students test performance What is the treatment variable X?

▶ Let's look at a simple example. Suppose we are interested

- What is the outcome variable Y?
- Can you think of a potential confounder Z?

family wealth \checkmark private school \rightarrow test scores

IN THE PRESENCE OF CONFOUNDERS

- correlation does not imply causation
- the treatment and control groups are not comparable

- the difference-in-means estimator does NOT provide a valid estimate of the average causal effect

Why Don't We Worry About Confounders in Randomized Experiments?

- Randomization of treatment assignment eliminates all potential confounders
- It ensures that treatment and control groups are comparable by breaking the link between any potential confounder and the treatment
- If we assign who attends a private school at random, we ensure that nothing related to the outcome is also related to the likelihood of receiving the treatment

family wealth \land lottery \longrightarrow private school \rightarrow test scores

How Can We Estimate Causal Effects with Observational Data?

- We cannot rely on random treatment assignment to eliminate potential confounders
- We must identify all potential confounding variables and statistically control for them using a multiple linear regression model
- Before we learn how to do that, we should learn how to fit a simple linear regression model to produce an estimated coefficient equivalent to the difference-in-means estimator

Using the Simple Linear Model to Compute the Difference-in-Means Estimator

When X is the treatment variable and Y is the outcome variable of interest, the estimated slope coefficient ($\hat{\beta}$) is equivalent to the difference-in-means estimator.

- Let's return to the exercise from Lecture 6: Does Social Pressure Affect Turnout?
- We answer it by analyzing data from a randomized experiment where registered voters were randomly assigned to either (a) receive a message designed to induce social pressure, or (b) receive nothing

Does Social Pressure Affect Turnout?



(Based on Alan S. Gerber, Donald P. Green, and Christopher W. Larimer. 2008. "Social Pressure and Voter Turnout: Evidence from a Large-Scale Field Experiment." *American Political Science Review*, 102 (1): 33-48.)

1. Load and look at the data

voting <- read.csv("voting.csv") # loads and stores data

head	(v	oting)	# shows	s first	six	observations
##		birth	message	voted		
##	1	1981	no	0		
##	2	1959	no	1		
11 11	0	1050		-1		

TTTT	4	1000	110	-
##	3	1956	no	1
##	4	1939	yes	1
##	5	1968	no	0
##	6	1967	no	0

2. Create treatment variable

 3. Compute difference-in-means estimator directly

```
mean(voting$voted[voting$pressure==1]) -
    mean(voting$voted[voting$pressure==0])
## [1] 0.08130991
```

4. Alternatively, we can fit a linear model where X is the treatment variable and Y is the outcome variable

Recall: the R function to fit a linear model is lm()
 required argument: a formula of the type Y ~ X

 $Im(voting\$voted \sim voting\$pressure) \# or$

Im(voted ~ pressure, data=voting)
##
Call:
Im(formula = voted ~ pressure, data = voting)
##
Coefficients:
(Intercept) pressure
0.29664 0.08131

- Fitted model: $\widehat{voted} = 0.30 + 0.08$ pressure
- Note that β has the same value as the difference-in-means estimator above (both equal 0.08)

Interpretation of $\hat{\beta}$ When X Is the Treatment Variable and Y Is the Outcome Variable

- Start same as in predictive models
 - definition: $\widehat{\beta}$ is the $\bigtriangleup \widehat{Y}$ associated with $\bigtriangleup X=1$
 - ▶ here: $\hat{\beta} = 0.08$ is the $\triangle voted$ associated with $\triangle pressure=1$
 - in words: receiving the message inducing social pressure (i.e., an increase in *pressure* of 1 by going from pressure=0 to pressure=1) is associated with a predicted increase in the probability of voting of 8 percentage points, on average
- Init of measurement of β̂? same as △Ȳ; here, Y is binary so △Ȳ is measured in p.p and so is β̂ (after x 100)

- As a result, we can interpret $\hat{\beta}$ using causal langauge
- Predictive language: We estimate that receiving the message inducing social pressure *is associated with a predicted increase* in the probability of voting of 8 percentage points, on average
- Causal language: We estimate that receiving the message inducing social pressure *increases* the probability of voting by 8 percentage points, on average

- This should be a valid estimate of the average treatment effect if there are no confounding variables present
 - if registered voters who received the message are comparable to the registered voters who did not
- Since the data come from a randomized experiment there should be no confounding variables
- And thus the difference-in-means estimator should produce a valid estimate of the average treatment effect

- Whether we compute the difference-in-means estimator directly or we fit a simple linear model where Y is the outcome variable and X is the treatment variable, we arrive to the same conclusion
- Conclusion: We estimate that receiving the message inducing social pressure increases the probability of voting by 8 percentage points, on average. This is a valid estimate of the average treatment effect if registered voters who received the message are comparable to the registered voters who did not (that is, if there a no confounding variables). Given that the data come from a randomized experiment, this is a reasonable assumption.
- Note that this is the same conclusion we arrived at in Lecture 6

INTERPRETATION OF THE ESTIMATED SLOPE COEFFICIENT IN THE SIMPLE LINEAR MODEL:

- ▶ By default, we interpret $\hat{\beta}$ using predictive language: It is the $\triangle \hat{Y}$ associated with $\triangle X=1$.
- ▶ When X is the treatment variable, then $\hat{\beta}$ is equivalent to the difference-in-means estimator and, thus, we interpret $\hat{\beta}$ using causal language: It is the $\triangle \hat{Y}$ caused by $\triangle X$ =1 (the presence of the treatment). This causal interpretation is valid if there are no confounding variables present and, thus, the treatment and control groups are comparable.

Today's Class

- Observational Studies
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Next Class

- How to Use Multiple Linear Regression Models to Control for Confounders and Estimate Average Treatment Effects Using Observational Data
- Bring your computers!