



Isaac Newton

RHEOLOGY
RHEOMETRY

Definition of rheology

- Study of the flow and deformation of materials
- All matter deforms when a **stress** is applied, the resulting deformation being the **strain**

Newton's law
liquids

$$\tau = \eta \cdot D \quad \eta = \frac{\tau}{D}$$

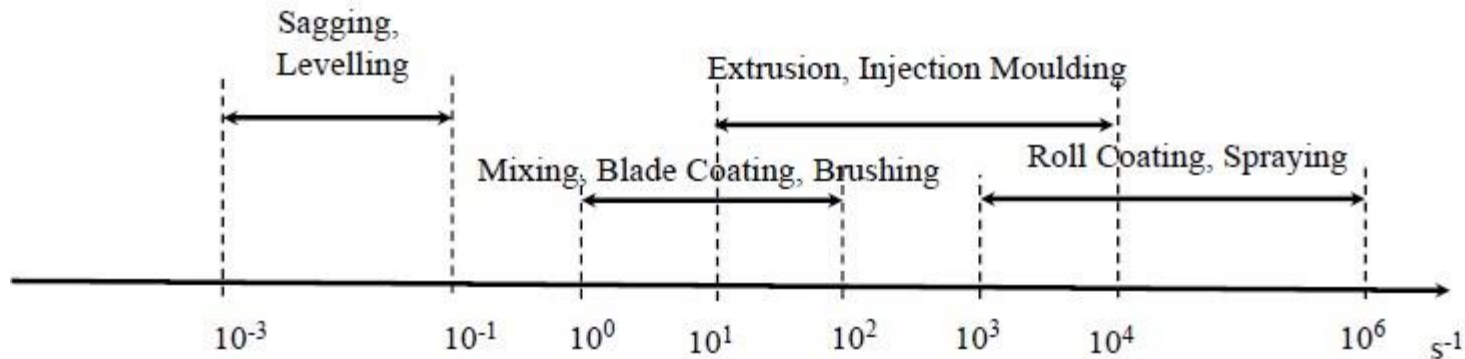
The ratio of stress to strain in liquids is constant

The proportionality constant is **viscosity**

Viscosity is a measure of liquid's resistant to flow

- **Dynamic viscosity** η [Pa.s]
- **Kinematic viscosity** ν [m².s⁻¹]

Typical Shear Rate Ranges



Rotational-Rheometer

Sample: Water up to solids

Results: Shear-Viscosity, Yield Stesses, Visco-Elasticity, Relaxation...

High Pressure Capillary-Rheometer

Sample: Water up to high viscous

Results: Shear-Viscosity, Elongational-Viscosity, Wall Slip...

Typical Shear Viscosities

<u>Material</u>	<u>Shear-Viscosity (Pas)</u>
Air	10^{-6}
Aceton	10^{-4}
Water	10^{-3}
Olive Oil	10^{-1}
Glycerol	10^0
Molten Polymers	10^3
Bitumen	10^8
Glass at 500°C	10^{12}
Glass at ambient	10^{40}

Units:

Pascal second Pas (SI)

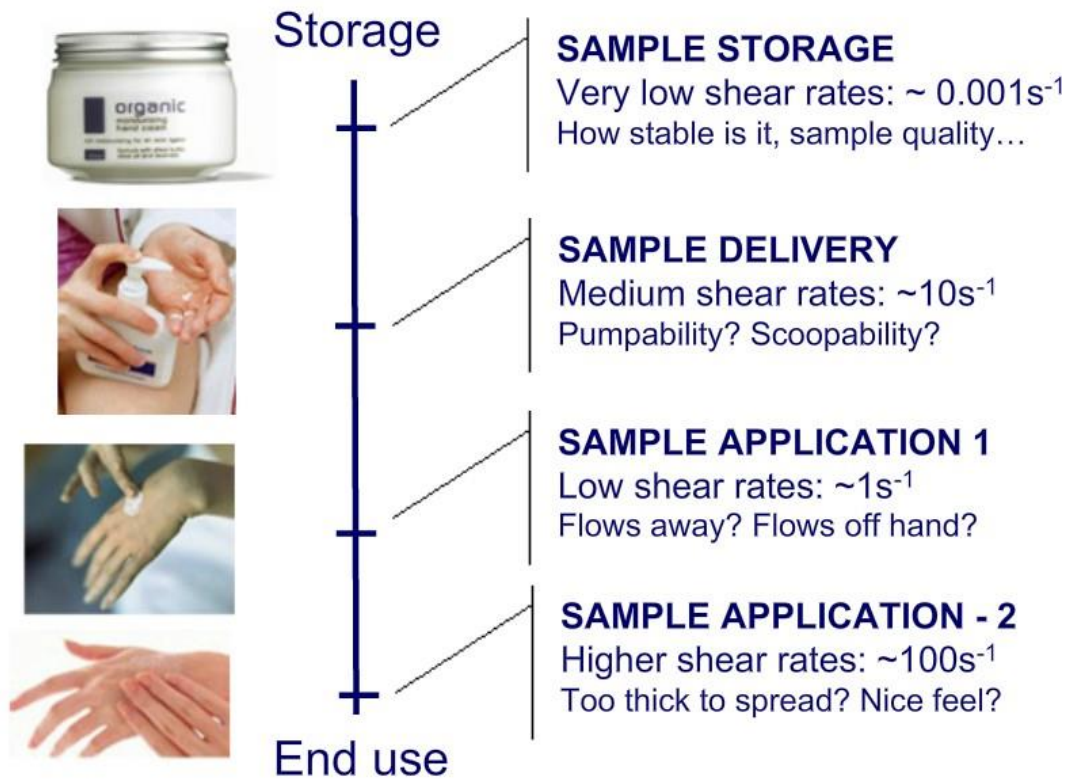
Poise P (CGS)

Remember

1 Pas = 10 P

1 mPas = 1 cP

Match shear rate to processes...



What Affects the Rheological Property?

Temperature

Many materials are quite sensitive to temperature, and a relatively small variation will result in a significant change in viscosity.

Shear Rate

When a material is to be subjected to a variety of shear rates in processing or use, it is essential to know its viscosity at the projected shear rates.

Measuring Conditions

Viscometer model, spindle/speed combination, sample container size, sample temperature, sample preparation technique, etc.

Others

homogeneity of the sample, time, dissolved gases - bubbles, previous history - storage conditions and sample preparation techniques

TYPES OF FLOW BEHAVIOR

Newtonian flow

Non-Newtonian flow

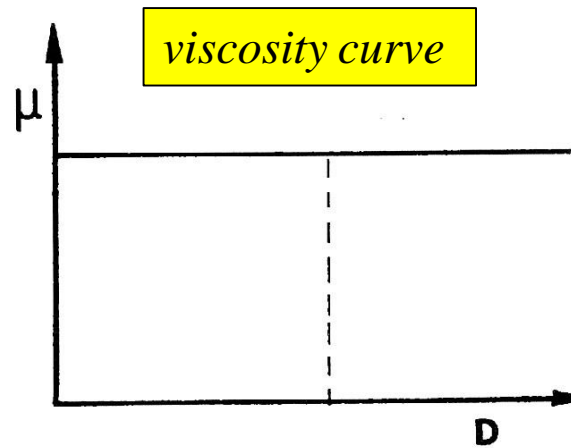
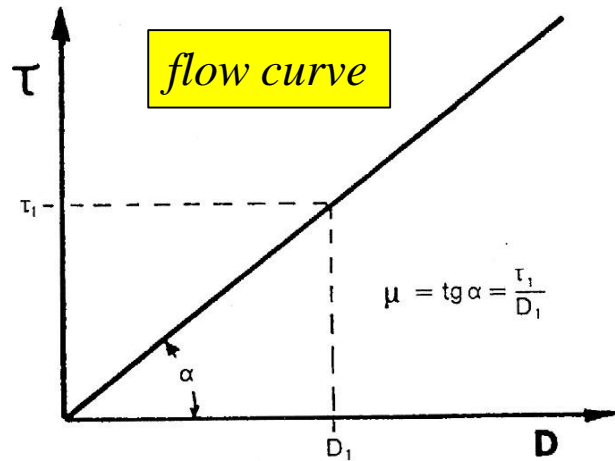
Time independent

- Pseudoplastic = shear thinning
- Plastic = shear thinning with yield
- Dilatant = shear thickening

Time dependent

- Thixotropy
- Rheopexy

Newtonian flow



- Direct proportionality between shear stress and shear rate
- Viscosity curve is straight line parallel to x-axis (ordinate)
- Viscosity is constant
- Low molecular weight liquids
water, alcohols, glycerin, and thru solutions

Non-newtonian flow

Viscosity is not constant changes with shear rate/shear stress

→ **apparent viscosity**

Power Law (Ostwald-de Waele equation) for liquids

$$\tau = K \cdot D^n \quad \eta_{app} = K \cdot D^{n-1}$$

η_{App}	shear viscosity
D	shear rate
K	Consistency index
n	Power Law Index (Flow index)

Herschel-Bulkely equation for semisolids

$$\tau = \tau_y + K \cdot D^n$$

τ_y yield stress

Consistency index

Viscosity (or stress) at a shear rate of 1 s^{-1}

The point the viscosity/shear rate curve „hangs from“

Power Law Index (Flow index)

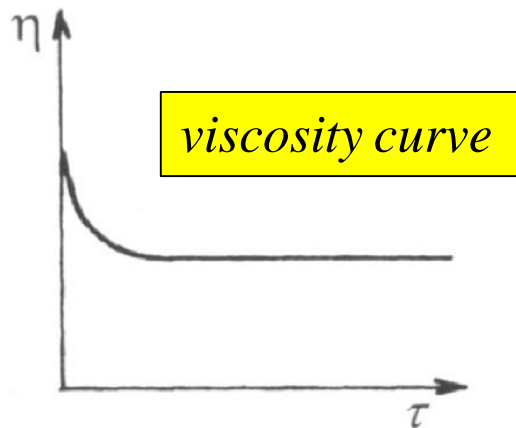
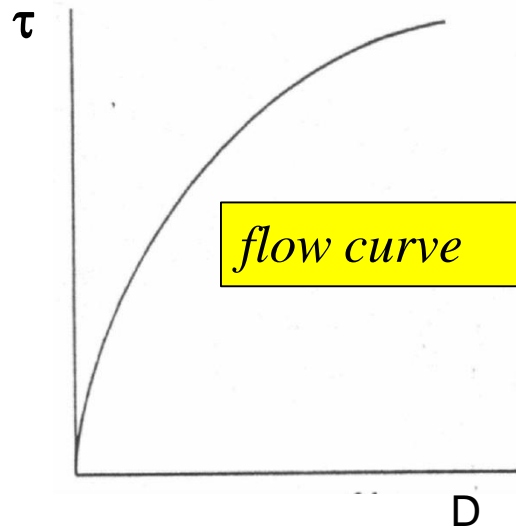
index of the deviation from Newtonian flow
or measure of non-Newtonian-ness

Newtonian flow $n = 1$

Pseudoplastic flow
(shear-thinning) $0 < n < 1$

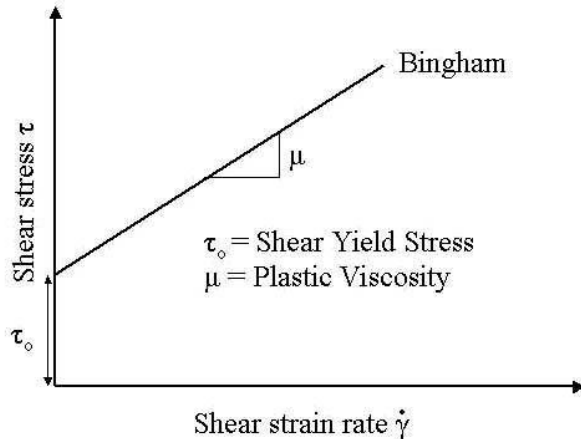
Dilatant flow
(shear-thickening) $n > 1$

Shear-thinning = Pseudoplastic flow

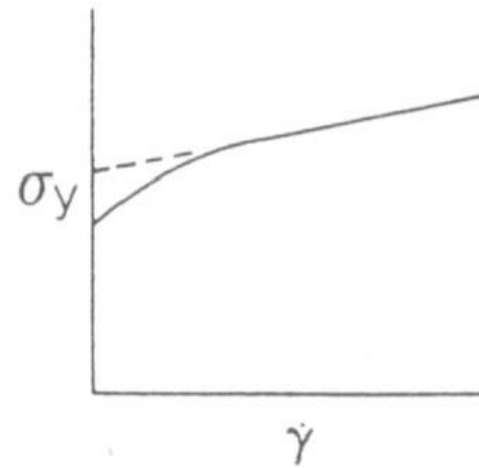


- Rheogram passes through the origin
- Flow curve is concave towards the shear-rate axis
- Apparent viscosity decreases with increasing shear rate
- Shear rate thinning
- *Low concentration solutions of polymers*

Plastic (Bingham) flow shear thinning with yield point



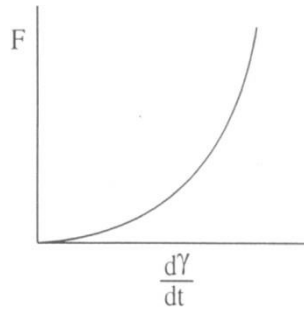
Ideal Bingham flow



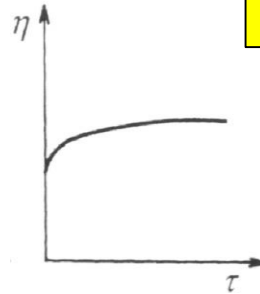
Real Bingham flow

- Rheogram (flow curve) **doesn't lead from the origin**
Yield point - the intercept on the shear stress axis
- Apparent viscosity **decreases** with increasing shear rate
- high concentration solutions of polymers, gels, creams, ointments, pastes... semisolid preparations

Shear rate thickening = Dilatant flow



flow curve



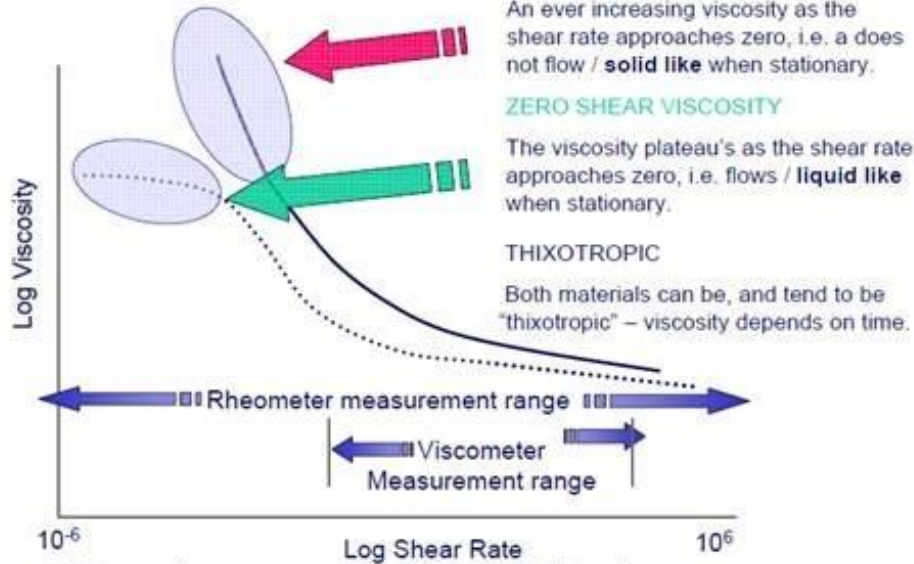
viscosity curve

- Rheogram passes through the origin
- Apparent viscosity increases with increasing shear rate
- Technologically undesirable phenomenon
- *Highly concentrated, deflocculated suspensions*
insufficient liquid to fill completely all the voids between the particles results in a three-phase mixture - solids, liquids, and usually air; due to the presence of air, the mixture is compressible, and therefore, the more you compress it, the greater the resistance to flow
Sand that is completely soaked with water also behaves as a dilatant material. This is the reason why when walking on wet sand, a dry area appears underneath your foot.

<http://en.wikipedia.org/wiki/Dilatant>

http://www.che.udel.edu/research_groups/wagner/stf.html

Relation to Flow Curves



"YIELD STRESS"

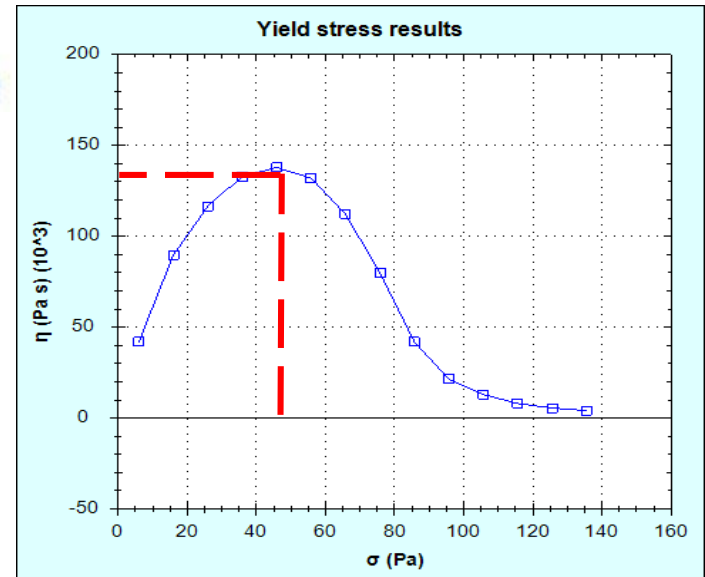
An ever increasing viscosity as the shear rate approaches zero, i.e. a does not flow / **solid like** when stationary.

ZERO SHEAR VISCOSITY

The viscosity plateau's as the shear rate approaches zero, i.e. flows / **liquid like** when stationary.

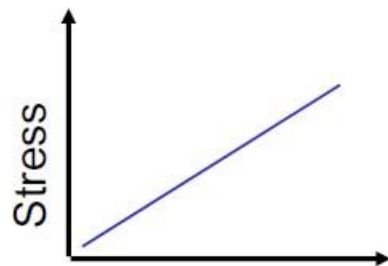
THIXOTROPIC

Both materials can be, and tend to be "thixotropic" – viscosity depends on time.



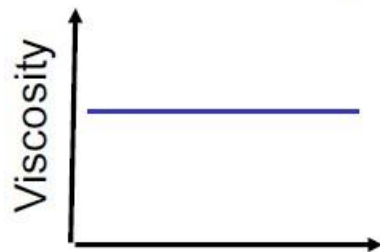
Overview of the flow types

Newtonian



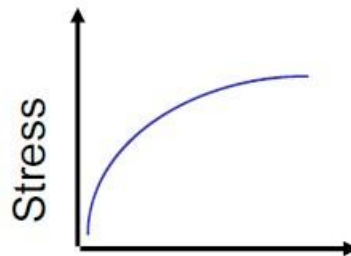
Shear Rate

Silicon Oil, Suspension



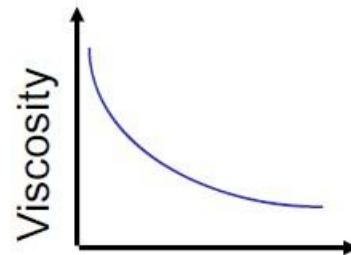
Shear Rate

Shear Thinning



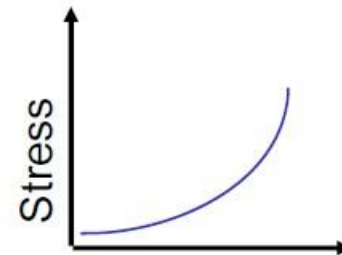
Shear Rate

Inks, Paints



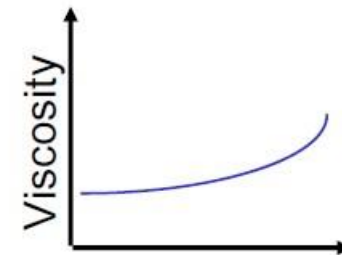
Shear Rate

Shear Thickening



Shear Rate

Cornflower



Shear Rate

Thixotropy

- Time dependent flow
- Reversible loss of viscosity, as a function of time, at a constant shear rate
- Isothermal gel-sol-gel transformation
- The mechanism: breakdown and re-forming of the structure
- Rheogram: thixotropic hysteresis loop
- Very often, and technologically convenient

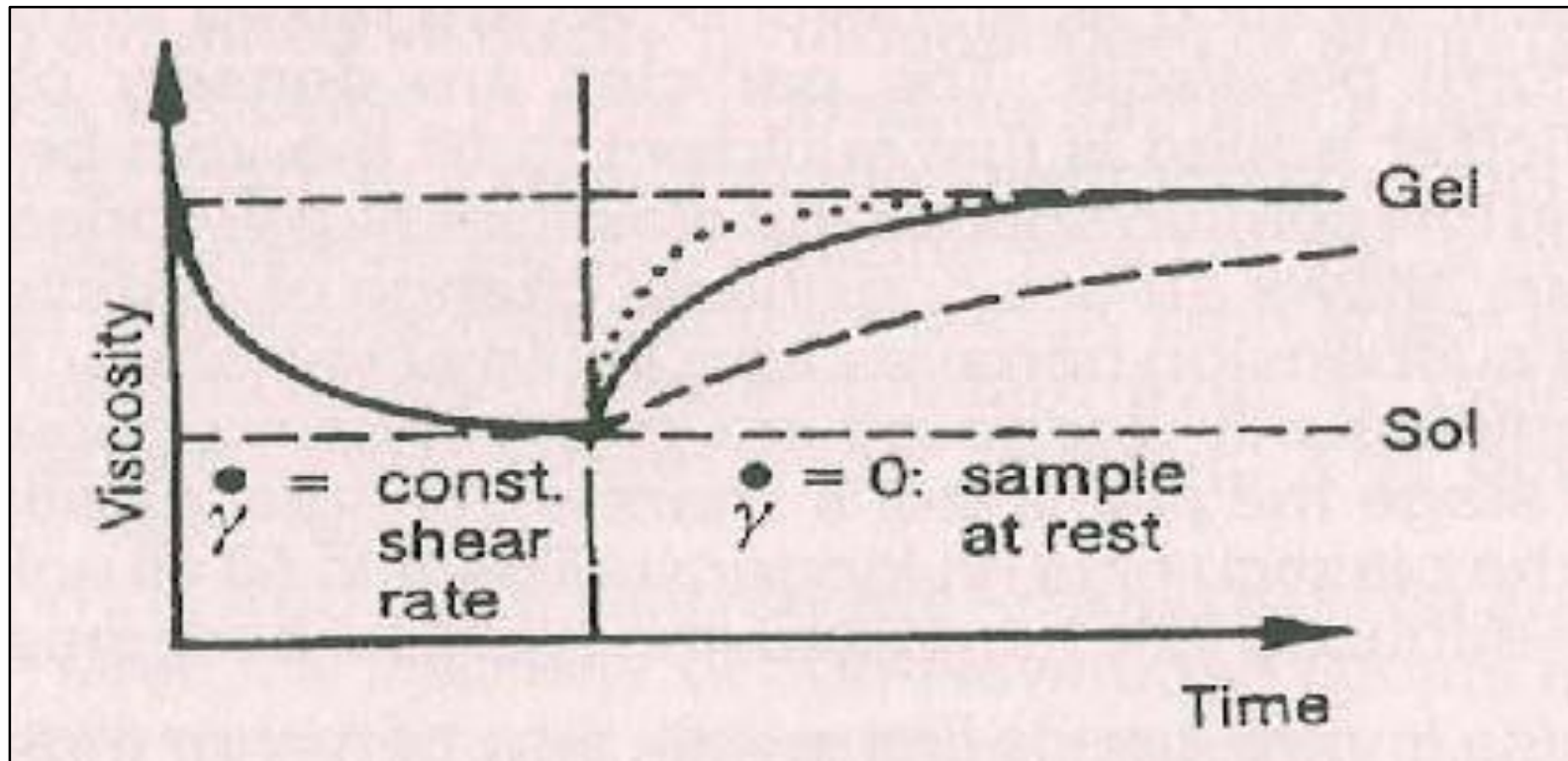
Flow curve(s)



Viscosity curve(s)

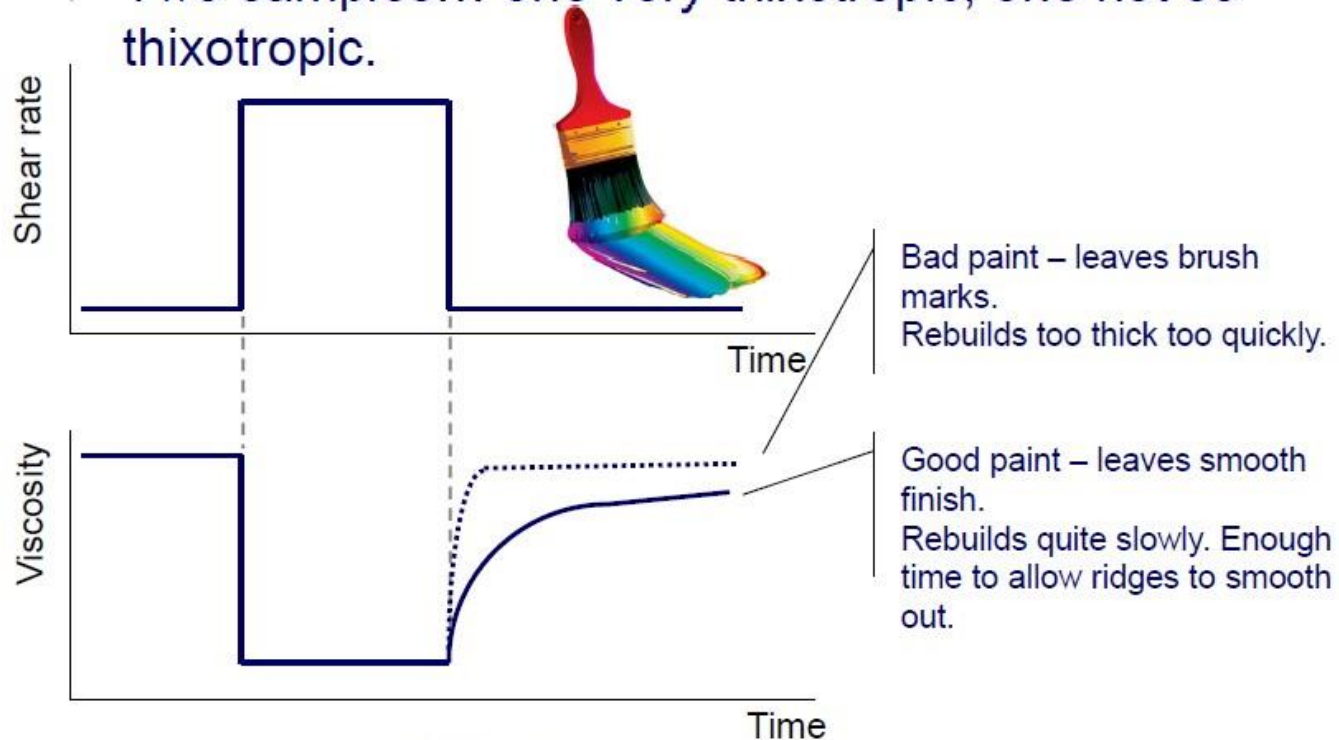


Viscosity – time - curve



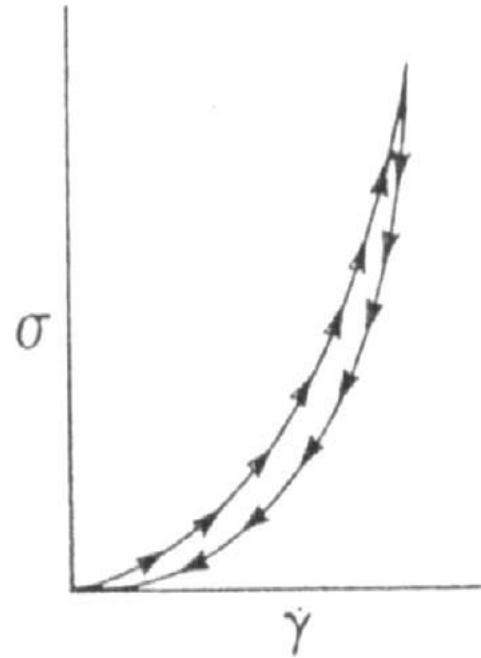
Thixotropic Example

- ▶ Two samples... one very thixotropic, one not so thixotropic.



Rheopexy

- Inverse to thixotropy
- reversible increase of viscosity, as a function of time, at a constant shear rate
- Isothermal transformation sol-gel-sol
- Rare, undesirable phenomenon



Reasons for making rheological measurements

- To quantitate the effects of time, temperature, ingredients, and processing parameters on a formulation
- To describe quantitatively the flow behavior of material for the purpose of quality control
- To measure the ease of product dispensation from a tube, bottle, or jar
- To measure spreadability
- To understand the fundamental nature of the system

Capillary viscometers

- The time taken for a known volume of liquid to flow through a capillary tube is measured
- Precision instruments - good temperature control is essential ($20 \pm 0.01^\circ\text{C}$)

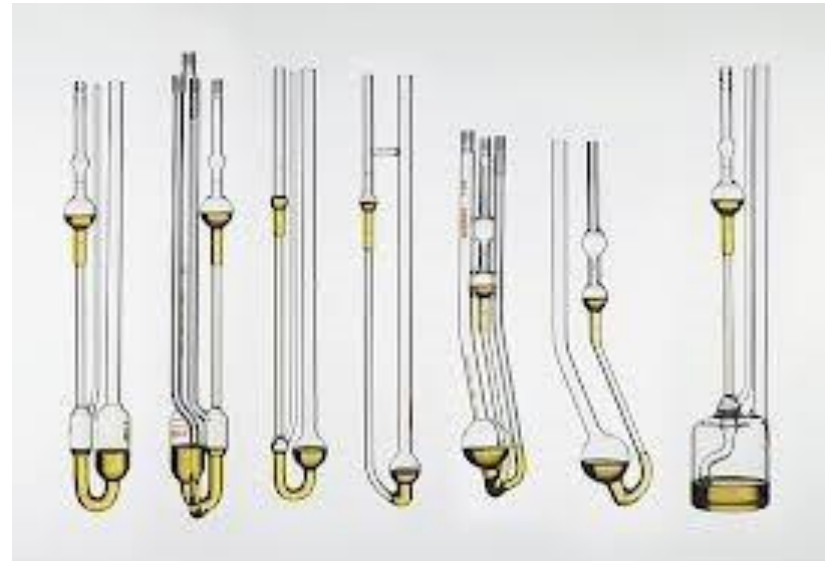
Kinematic viscosity ν [mm^2s^{-1}]

$$\nu = k t$$

Dynamic viscosity η [$\text{mPa}\cdot\text{s}$]

$$\eta = k \rho t$$

k constant of the viscometer
 ρ density of the liquid
 t flow time



Rotational rheometers/viscometers

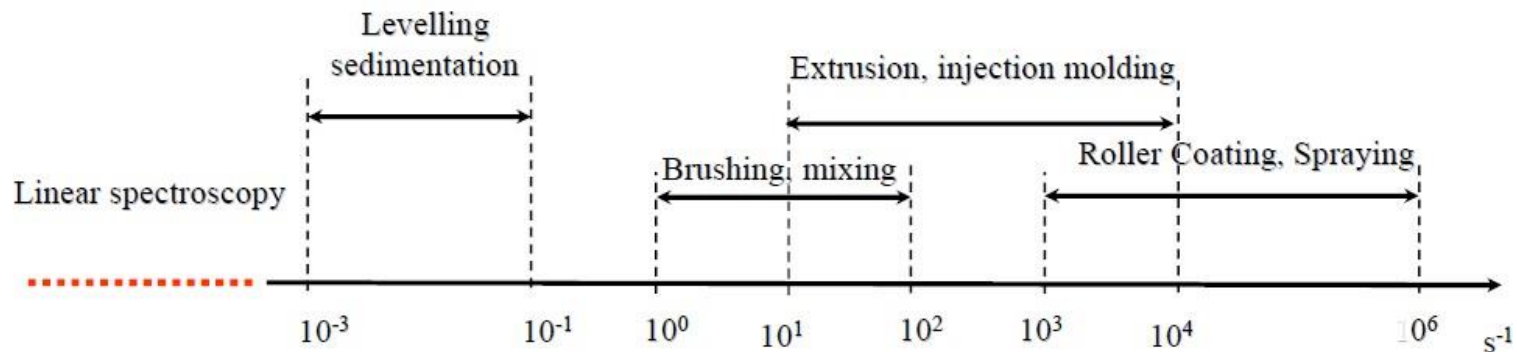
Viscometry: shear rate range from 10^{-1} to 10^1 s^{-1}

Rheometry: shear rate range from 10^{-3} to 10^3 s^{-1}

Viscosity of Newtonian (shear-independent viscosity) or non-Newtonian liquids (shear dependent viscosity or apparent viscosity)

Typical shear rates

Why do we need different rheometers ?



Absolute rotational rheometers

- The flow in the measuring geometry is well defined
- The measurements result in absolute viscosity values, which can be compared with any other absolute values

Relative spindle viscometers

- The flow in the measuring geometry is not defined
- The measurements result in relative viscosity values, which cannot be compared with absolute values or other relative values if not determined by the same relative viscometer method

➤ *CS-rheometers (controlled stress)*
stress is set
and resulting strain is measured

➤ *CR-rheometers (controlled rate)*
shear strain is set and resulting
stress is measured

➤ *Searl's type*
inner (upper) spinning part

➤ *Couett's type*
outer cone or lower plate is
spinning

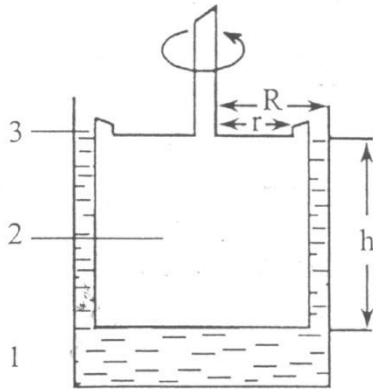
Spindle viscometers (relative viscometers)

- Speed of the spindle from 0.3 to 100 RPM
- 3 types (L, R, H) for various extent of viscosity
- Set of the standard spindles (disc, cylinder, rod) (4 or 6)

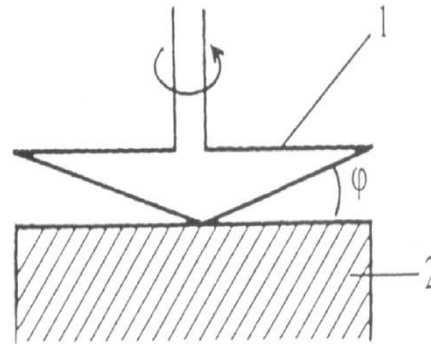


Rotational rheometers

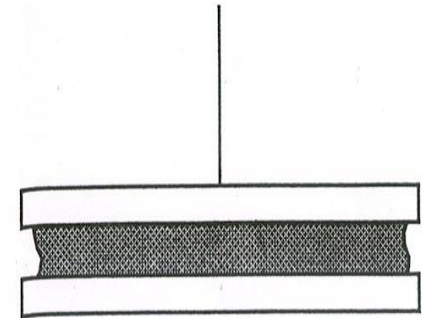
(absolute viscometers arrangement)



*2 concentric cylinders
(cup & bob)*



cone-plate

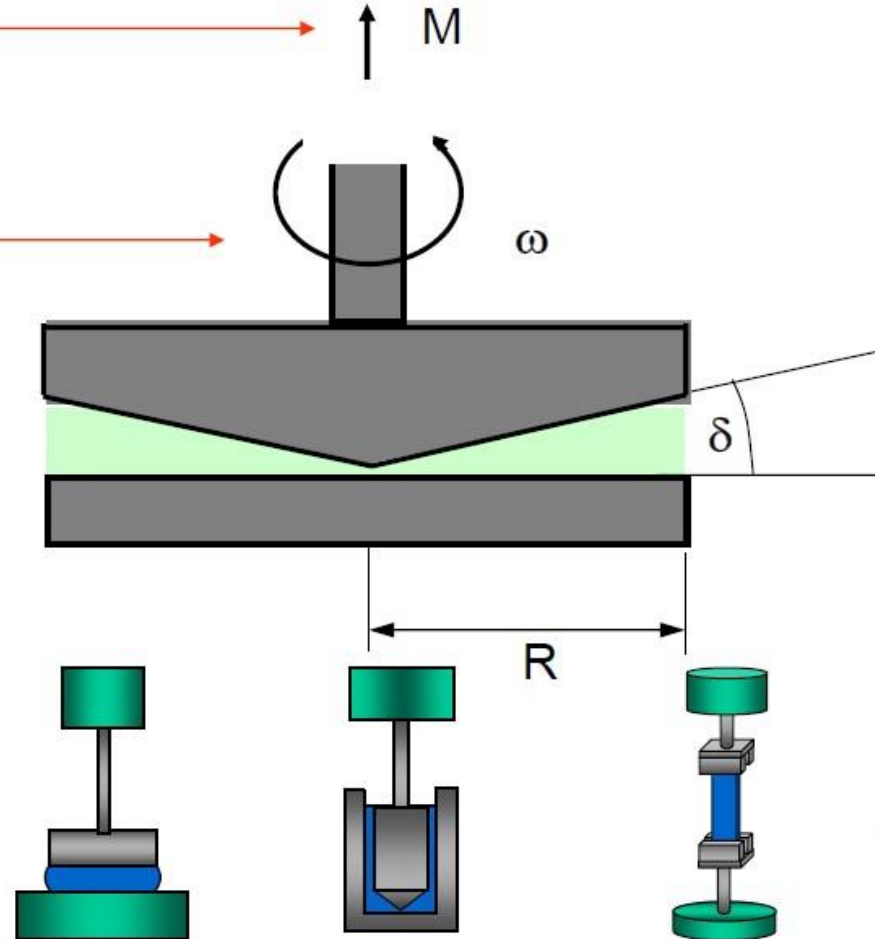


2 parallel plates

Choice of Geometry: From Fluids to Solids

Apply Torque /
Measure Torque

Measure Displ.
Apply Displacement



*Rule of Thumb
for dispersions:
Gap Size > 10 * D90*

- the higher the viscosity, the smaller the geometry
- the higher the shear rate, the smaller the gap.

Parallel Plates

Cup&Bob

Solids Fixture

Rotational rheometers



Penetrometers



- Measuring of the **consistency** of semisolids
- A cone or needle of known weight is allowed to fall through the test material
- The **depth of penetration** in a fixed time is inversely related to the consistency (0.1 mm)
- Consistency (technical quantity, no units)
- $(25 \pm 0,5) ^\circ\text{C}$

Ph. Eur. Paraffin, White Soft

Consistency (2.9.9) 60 to 300

(depth of penetration 6 to 30 mm)

Thank you for your attention

<http://en.wikipedia.org/wiki/Viscosity>

<http://en.academic.ru/dic.nsf/enwiki/415268>

<http://www.medicinescomplete.com/mc/rem/current/c37.htm>