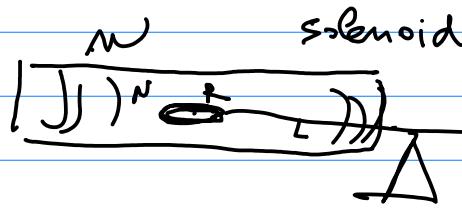


[3.1.7]



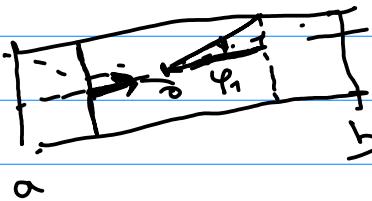
$$I = f(f_g)$$

$$\vec{F} = q \vec{v} \times \vec{B}$$

$$d\vec{F} = I d\vec{l} \times \vec{B}$$

a) pole with solenoid

$$\rightarrow \oint \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{in}} \quad | \text{ z-Achse, osz: } \frac{\mu_0 I}{2} \frac{R^2}{(R^2 + z^2)^{3/2}}$$



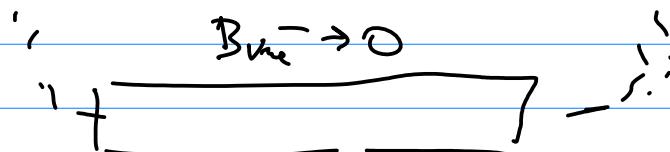
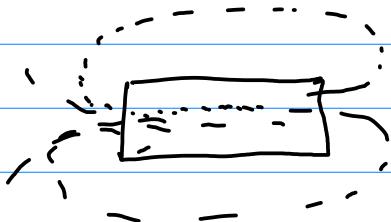
$$B_z = \frac{\mu_0 I}{2} \int_a^L \frac{R^2}{(R^2 + z^2)^{3/2}} dz$$

$\hookrightarrow (\partial B / \partial z)_T$

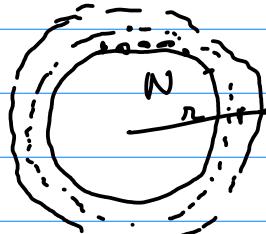
$$B_z = \frac{\mu_0 I}{2} \left[\frac{z}{R^2 + z^2} \right]_a^L$$

$$\frac{z}{\sqrt{R^2 + z^2}}$$

$$\begin{aligned} & \xrightarrow{z \rightarrow -\infty} B_z = \frac{\mu_0 I}{2} \left(1 - (-1) \right) = \underline{\underline{\mu_0 I n}} \\ & \xrightarrow{z \rightarrow \infty} B_z \rightarrow 0 \end{aligned}$$

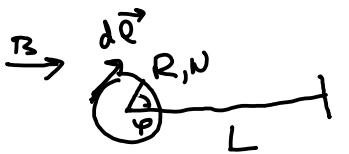


$\Rightarrow B_z \text{ monotonous}$



$$\oint \vec{B} \cdot d\vec{l} = 2\pi r B = \mu_0 I N$$

$$B = \frac{\mu_0 I N}{2\pi r} = \underline{\underline{\mu_0 I n}}$$



$$d\vec{F} = Id\vec{l} \times \vec{B}$$

$$F = N \int_0^{2\pi} I R d\varphi B \cos \varphi = NI R \int_0^{2\pi} \cos \varphi d\varphi = 0$$

$$M = N \int_0^{2\pi} I R d\varphi (L - R \omega \sin \varphi) B \cos \varphi$$

$$= NI R^2 B \int_0^{\pi} \cos^2 \varphi d\varphi = \pi NI R^2 B$$

$$= \mu_{0, M} N I \frac{\pi}{4} R^2$$

$\nabla \times \vec{B} = 0$

$$\vec{B} = \nabla \times \vec{A}$$

$$\nabla \cdot \vec{B} = 0$$

$$\nabla \times \vec{B} = \mu_0 \vec{j}$$

$$\nabla \times \nabla \times \vec{A} = \nabla (\underbrace{\nabla \cdot \vec{A}}_{=0}) - \nabla \times \vec{A}$$

$$= 0 \quad (\text{vs. } \Delta)$$

$$\vec{A} = -(\mu_0 \vec{j})$$

$$\Delta \psi = -\frac{\partial}{\partial z}$$

$$\psi = \frac{1}{4\pi\epsilon_0} \int \frac{\sigma(z)}{R} dV$$

$$A_x = \frac{\mu_0}{4\pi} \int \frac{j_x(z)}{R} dV$$

[3.1.11]



$$\vec{A} = ?$$

$$A_z = \frac{j R^2}{2} \ln \frac{R}{r}$$

analog:



$$E \cdot 2\pi r \cdot L = \frac{\sigma \pi R^2 L}{\epsilon_0}$$

$$E = \frac{1}{2\epsilon_0} \frac{\sigma R^2}{L}$$

$$\psi = -\frac{\sigma \epsilon_0}{2\epsilon_0} \ln \frac{R}{r}$$

$$\vec{B} = \nabla \times \vec{A} = \nabla \times (0, 0, c \ln r) \quad r = \sqrt{x^2 + y^2}$$

$$= \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ 0 & 0 & c \ln r \end{vmatrix} = c \left(-\frac{\partial}{\partial y} \ln r, \frac{\partial}{\partial x} \ln r, 0 \right)$$

$$\frac{\partial}{\partial y} \ln \sqrt{x^2 + y^2} = \frac{1}{\sqrt{x^2 + y^2}} \cdot \frac{1}{2} \frac{1}{\sqrt{x^2 + y^2}} \cdot 2y = \frac{y}{x^2 + y^2}$$

$$= R^2 \frac{\partial A_y}{\partial z} \left(\frac{y}{R^2}, 1 - \frac{x}{R^2}, 0 \right)$$

uplim. $B_y = \frac{\mu_0 I}{2\pi r}$

D.Ú. mag. dipol \approx potenzialen prinzip erst. analogie

$$\vec{A} = ?$$

$$A_x \dots j_x$$

$$A_y \dots j_y$$

$$\vec{B} = ?$$

$$\nu_{\text{Zmm}} \quad \nabla \times \vec{A}$$

$$\int \vec{A} \cdot d\vec{l} = \left(A_x - \frac{\partial A_x}{\partial y} \frac{dy}{2} \right) \cdot dx$$

$$+ \left(A_y + \frac{\partial A_y}{\partial x} \frac{dx}{2} \right) \cdot dy - \left(A_x + \frac{\partial A_x}{\partial y} \frac{dy}{2} \right) \cdot dx$$

$$- \left(A_y - \frac{\partial A_y}{\partial x} \frac{dx}{2} \right) \cdot dy = - \frac{\partial A_x}{\partial y} dy dx + \frac{\partial A_y}{\partial x} dx dy$$

$$-\left(\frac{\partial A_y}{\partial x} - \frac{\partial A_x}{\partial y}\right) dx dy = (\nabla \times \vec{A}) \cdot d\vec{S}$$

$$T(\vec{r} + d\vec{r}) = T(\vec{r}) + \nabla T \cdot d\vec{r}$$